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minuunt. ut post ea ligb. Si u i reg. viii. sufficientes ad infini-  
ta multiplicatione. quæ noia singlis se supiecta.

colentes. Zementis. Zenis. chalcus. auunos. arbas. orrus. andras. 101.11.

6 0 V L h B M T I

Veru minutie sunt. xxiii. subscriptæ cū nominib; suis.

deunx. dextans. dodrans. bisse. septunx. semis. quæux. triens. quadrans.

¶ ¶ ¶ ¶ ¶ ¶ ¶ ¶ ¶

sixtans. sexcuncia. vncia. semuncia. duella. sicilacus. sexrula. dragma.

3 £ 1 £ 0 9 0 \*

emissosela tremissis seripulus. obulus. cerates. filiqua. chalcus.

¶ H ¶ ¶ ¶ ccc 3

**H**is characterib; firmiter memorie <sup>com</sup>mandatis; & quasi oculis  
cordis subiacentib; misteris eor. diuide potis & multipli-

*The Society of Antiquaries of Scotland  
From the Edition*

# Rara Mathematica;

OR,

A COLLECTION

OF

## TREATISES ON THE MATHEMATICS

AND

SUBJECTS CONNECTED WITH THEM,

*From ancient unedited Manuscripts.*

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EDITED BY

JAMES ORCHARD HALLIWELL, Esq., F.R.S., F.S.A.,  
&c. &c. &c.

OF JESUS COLLEGE, CAMBRIDGE.

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“I see not how the history of any science is to be conducted through the middle-age period, but by the assistance of the works of science of the middle-age writers, though the contents of them, as works of science, may have now become of little value.”

*Rev. J. Hunter's Monastic Libraries, Pref. p. xi.*

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THE SECOND EDITION.

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## P R E F A C E.

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THIS is a new impression rather than a new edition of a work which has been so favourably received, that the editor is induced to submit it once more to the notice of the reading public. The following notes on some of the tracts here printed, remain nearly the same as in the other edition.

I. *Johannes de Sacro-Bosco de Arithmetica*. Often occurs in MSS. without his name; MSS. Harl. 3647. 3843. 4350; Bib. Reg. 12 C. xvii; Arund. 343. Cott. Cleop. B. vi. f. 234; Publ. Cantab. li. I. 15. (1692). An English translation—Ashm. 396. The present text is taken from a manuscript formerly in the Library of the Abbate Canonici of Venice.

III. *A Treatise on the Numeration of Algorism*.—This is taken from a single leaf of vellum, found loose in an old MS. on astronomy, formerly in Dr. Clarke's library.

IV. *Bourne's Treatise on Optical Glasses*.—The other work he mentions in his dedication, as having been inscribed to Lord Burghley, is in the British Museum.—MS. Sloan. 3651.

V. *Johannes Robyns de Cometis*.—From a MS. in my own library. Other copies, Bib. Reg. 12 B. xv. and Trin. Coll. Cantab. inter MSS. Gal. O. I. 11.

VIII. *A Merchant's Account Table*.—This table is exceedingly curious, conducted partly similar to an abacus, the cyphers at the bottom being used to guide the manual calculator.

IX. *Carmen de Algorismo*. — A MS. of the Massa Compoti in the British Museum (Harl. 3902), by Alexander de Villa Dei, possesses an introduction to the work by some other author: it is there stated that the same author composed *Doctrinale et Algorismum Metricum*. M. Chasles informs me that a MS. of this tract in the French King's Library (7420. A.) has the following colophon at the end: *Explicit Algorismus editus a Magistro Alexandro de Villa Dei*. This is, I think, quite sufficient to prove him to be the author.

MSS. of it are very numerous: I will mention a few for guidance. MSS. Bib. Reg. 8 C. iv. 12 E. i. Cot. Vitell. A. i. (first chapter). Trin. Coll. Cant. O. v. 4. ii. 45. i. 31. S. Joh. F. 18. Publ. Mm. iii. 11. (2310). Ii. i. 13. (1690.) i. 15. (1692). Bodl. 57. Fairf. 27. Digb. 15. 22. 81. 97. 98 & 104. 190. Bodl. 4to. D. 21. Jur.

*Fragments* MSS. Sloan. 513. 1620. 2397.—Many copies of it occur in the Catalogue of the Library of the Dover Monastery (MS. Bodl. 920.) made in 1389.—*Vid.* Monast. iv. p. 532.

MS. Digb. 104, has Ambrosinus for Algorismus in the first line. MS. Sloan. 513, has the following colophon—

“Explicit tractatus algorismi tum satis breve et bono commento secundum Saxton.

Qui scripsit carmen sit benedictus. Amen!

Nomen scriptoris Galfridus plenus Amoris.”

Whose name is here latinized I know not, but I am not inclined to give much credit to it.

XII. *The Preface to an Almanac for 1430*.—It was pointed out to me by Professor De Morgan, that some portions of this are evidently plagiarized from Chaucer's preface to his tract on the Astrolabe.

35, Alfred Place, London, Jan. 1st, 1840.

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## CORRECTIONS AND ADDITIONS.

P. 2, l. 31.—*For idem, read eandem.*

P. 3, l. 13.—*For muneri, read numeri.*

P. 6, l. 20.—*For nonenarii, read novenarii, and in other places.*

P. 7, l. 18.—*For supponatur, read supraonatur.*

P. 11, l. 25, 29.—*For vide, read vid.*

P. 12, l. 22.—*For quinam, read quando.*

P. 15, l. 21.—*For perdictis, read prædictis.*

P. 19, l. 11.—*For quidenarius, read quindenarius.*

P. 19, l. 25.—*For perambulium, read præambulium.*

P. 26, l. 15.—*Sibi; so in the manuscript, but evidently sub.*

P. 29, l. 4.—*For 14, read 15.*

P. 30, l. 2, 6, 7; P. 31. l. 1, 13.—It will be readily seen that *y* is inserted in these places for *th*, the Saxon character having been mistaken by the printer.

P. 51, l. 17.—*For ince, read vice.* I may mention here, that it was pointed out to me by G. S. Venables, Esq., that a portion of this preface is plagiarised from Cicero.

P. 54, l. 18.—*Cædere; so in the manuscript, but evidently cedere.*

P. 55.—This table has been previously noticed, and in part printed by J. W. Lubbock, Esq., in *Phil. Trans.*

P. 55, Second table, l. 1.—*For 10, read 0.*

P. 56. The poem quoted in the note has since been printed in my "Early History of Freemasonry in England."

P. 57, l. 17.—*For Bathoniensum, read Bathoniensem.*

P. 73, l. 21.—*For nihil, read in his.*

P. 73, l. 22.—*For potuit, read patuit.*

P. 84, l. 12.—*For descriptos, read desuper.*

P. 85, l. 16.—*For principem, read patrem.*



#### NOTE.

The following volume was originally published at three several times : the first part (pp. 1—48) appeared on the 1st of June, 1838 ; the second (pp. 49—96) on the 1st of October, 1838 ; and the remainder on the 1st of June, 1839. It ought to be particularly remarked, that in no instance has the regular correction of the errors in the MSS. from which these tracts are printed been attempted.

# JOANNIS DE SACRO-BOSCO

## TRACTATUS

### DE ARTE NUMERANDI.

---

OMNIA quæ a primæva rerum origine processerunt ratione numerorum formata sunt,<sup>1</sup> et quemadmodum sunt, sic cognosci habent: unde in universa rerum cognitione, ars numerandi est operativa. Hanc igitur scientiam numerandi compendiosam edidit philosophus nomine Albus,<sup>2</sup> unde algorismus nuncupatur, vel ars numerandi,

<sup>1</sup> "Omnia quæcunque a primæva rerum natura constructa sunt, numerorum videntur ratione formata."—*Boetii Arith.* lib. i. cap. 2, *Edit. Par.* 1521, fol. 8. Vid. Hen. Welpii *Arith. Practica*, 4to. *Colon.* 1543. *Enchiridion Algorismi per Joannem Huswirt*, 4to. *Colon.* 1501. *Licht de Algorismo*, 4to. *Leip.* 1500.

<sup>2</sup> "Rex quondam Castellæ." *Johannis Norfolk progressionis summula*, MS. Harl. Mus. Brit. 3742. "Cum hæc scientia de numeris quæ algorismus ab inventore vel ab Algo, quæ est inductio et rismus, quæ est numerus quasi inductio in numeros appellatur."—*Tractatus de Algorismo*, MS. Arundel. M.B. 332, fol. 68. Vid. Pref. a "Œuvre tresubtile et profitable de Arithmetique et Geom." 4to. *Par.* 1515, Sig. B. 2.

vel introductio in numerum. Numerus quidem dupliciter notificatur, formaliter et materialiter: formaliter ut numerus est multitudo ex unitatibus aggregata: materialiter ut numerus est unitates collectæ. Unitas autem est qua unaquæque res una dicitur. Numerorum alius digitus;<sup>3</sup> alius articulus; alius numerus compositus sive mixtus. Digitus quidem dicitur omnis numerus minor denario; articulus vero est omnis numerus qui potest dividi in decem partes æquales, ita quod nihil residuum sit; compositus vero sive mixtus est qui constat ex digito et articulo. Et sciendum est quod omnis numerus inter duos articulos proximos est numerus compositus. Hujus autem artis novem<sup>4</sup> sunt species; scilicet, numeratio, additio, subtractio, mediatio, duplatio, multiplicatio, divisio, progressio, et radicum extractio; et hæc dupliciter in cubicis et quadratis; inter

<sup>3</sup> "Digitus est omnis numerus minor decem. Articulus est omnis numerus qui digitum decuplat, aut digiti decuplum, aut decupli decuplum, et sic in infinitum. Separantur autem digiti et articuli in limites. Limes est collectio numerorum, qui aut digiti sunt, aut digitorum æquæmultiplices, quilibet sui relativi. Limes itaque primus digitorum, secundus primorum articulorum. Tertius est secundorum articulorum. Et sic in infinitum. Numerus compositus est qui constat ex numeris diversorum limitum. Item numerus compositus est qui pluribus figuris significativis representatur."—*Algorismus demonstratus Regiomontani*, edit. 1534, Sig. A. iv.

<sup>4</sup> Prodocimus de Beldemando de Padua facit idem divisionem, sed Lucas Paciulus de Burgo Sancti Sepulchri omittit duplationem et mediationem. Vid. Wallisii Opera, tom. iii. Art. *Alg.*

quas primo de numeratione et postea de aliis per ordinem dicetur.

### I.—*Numeratio.*

Est autem numeratio cujuslibet numeri per figuras competentes artificialis representatio. Figura vero differentia locus et limes idem supponunt, sed diversis rationibus imponuntur. Figura dicitur quantum ad lineæ pertractionem. Differentia vero quantum per illam ostenditur qualiter figura precedens differat a subsequenti. Locus vero dicitur ratione spatii in quo scribitur. Limes<sup>5</sup> quia est via ordinata ad cujuslibet numeri representationem. Juxta igitur novem limites inveniantur novem figuræ, novem digitos representantes; quæ tales sunt, 9 . 8 . 7 . 6 . 5 . 4 . 3 . 2 . 1. Decima figura dicitur theta,<sup>6</sup> vel circulus, vel cifra,<sup>7</sup> vel figura nihili quia nihil significat, sed locum tenens dat aliis significare: nam sine cifra vel cifris purus non potest scribi articulus. Cum igitur

<sup>5</sup> “Numerorum diversi sunt limites. Primus enim limes restat ab unitate usque ad denarium; a denario in centenarium: a centenarium in millenarium: et sic per decuplum. Secundus limes a binario usque ad vigenarium: a vigenario usque ad ducenta; a ducentis usque ad duo millia. Similiter et cæteri per cæteros digitos sumuntur. Sunt autem tot limites quot digiti.”—*MS. de Algorismo*, Bib. Trin. Col. Cant. Gal. Collect. O 2. 45, fol. 37.

<sup>6</sup> In multis MSS. *teca* et *theca*.

<sup>7</sup> Vid. Noviomagus de Numeris, 12mo. *Par.* 1539, p. 40. Vossius de Scien. Math. et Wallisii Algebra, Angl. edit. p. 9.



per has novem figuras significativas adjunctas quandoque cifrae quandoque cifris contingat quemlibet numerum representare, non fuit necesse plures invenire figuras significativas. Notandum igitur quod quilibet digitus una sola figura sibi appropriata habet scribi. Omnis vero articulus per cifram primo positam et per figuram digiti a quo denominatur, ille articulus habet representari vel denominari. Quilibet articulus ab aliquo digito denominatur, ut denarius ab unitate, vigenarius a binario, et sic de aliis. Omnis numerus in eo quod digitus habet poni in prima differentia: omnis articulus in secunda. Omnis vero numerus a decem usque ad centum, ut centenarius excludatur, scribatur duabus figuris; si sit articulus, per cifram primo loco positam et figuram scriptam versus sinistram quæ significat digitum a quo denominatur ille articulus; si sit numerus compositus, scribatur digitus qui est pars illius numeri compositi et sinistretur articulus. Item omnis numerus a centum usque ad mille, ut millenarius excludatur, per tres figuras habet scribi. Item omnis numerus a mille usque ad decem millia, per quatuor figuras habet scribi, et sic deinceps. Notandum quod quælibet figura primo loco posita significat suum digitum: secundo decies suum digitum: tertio centies suum digitum; quarto loco millesies; quinto loco decies millesies; sexto loco centies millesies; septimo loco millesies millesies,



et sic usque ad infinitum multiplicando per hæc tria, decem, centum, mille: quæ tamen omnes continentur in hac maxima; quælibet figura in sequenti loco posita decies tantum significat quantum in præcedenti. Item sciendum est quod supra quamlibet figuram loco millenarii positam componenter possunt poni quidam punctus ad denotandum quod tot millenarios debet ultima figura representare, quot fuerunt puncta pertransita. Sinistrorsum autem scribimus in hac arte more Arabum hujus scientiæ inventorum, vel hac ratione ut in legendo, consuetum ordinem observantes numerum majorem proponamus.

## II.—*Additio.*

Additio<sup>8</sup> est numeri vel numerorum aggregatio, ut videatur summa excrescens. In additione duo ordines figurarum et duo numeri adminus sunt necessarii, numerus cui debet fieri additio, et numerus qui recipit additionem alterius et debet superscribi. Numerus vero addendus est ille qui debet addi ad alium, debet subscribi, et competentius est ut minor numerus subscribatur et majori addatur. Si igitur velis numerum

<sup>8</sup> “Additio est numeri ad numerum aggregatio, ut videatur summa excrescens: vel aliter: additio est duorum numerorum tertii inventio qui ambos contineat. In additione duo sunt ordines et duo numeri sunt necessarii; scilicet, numerus addendus et numerus cui debet fieri additio.”—*MS. de Arithmetica*, Mus. Brit. Arundel. 332, fol. 68, b.

addere numero, scribe numerum cui debet fieri additio in superiori ordine per suas differentias ; numerum vero addendum in inferiori ordine per suas differentias, ita quod prima inferioris ordinis sit sub prima superioris ordinis, secunda sub secunda, et sic de aliis. Hoc facto, addatur prima inferioris ordinis primæ superioris ordinis ; ex tali ergo additione aut excrescat digitus, aut articulus, aut numerus compositus. Si digitus, loco superioris deletæ scribatur digitus excrescens. Si articulus, loco superioris deletæ scribatur cifra et transferatur digitus a quo denominatur ille articulus versus sinistram partem, et addatur proximæ figuræ sequenti, si sit figura sequens ; si nulla, sit figura ponatur in loco vacuo. Si autem contingat quod figura sequens cui debet fieri additio articuli sit cifra, loco illius deletæ scribatur digitus articuli. Si vero contingat quod sit figura nonenarii, et ei debeat fieri additio unitatis ; loco illius nonenarii deletæ scribatur cifra, et sinistretur articulus ut prius. Si autem excrescat numerus compositus, loco superioris deletæ scribatur digitus, pars illius numeri compositi, et sinistretur articulus ut prius. Hoc facto, addatur secunda secundæ sibi suprapositæ, et fiat ut prius.

### III.—*Subtractio.*

Subtractio est, propositis duobus numeris, majoris ad minorem excessus inventio : vel sic,

subtractio est numeri a numero ablatio, ut videatur summa excrescens. Minor autem de majori subtrahi potest, vel par de pari; major vero de minori nequaquam. Ille quidem numerus major est qui plures habet figuras, dummodo ultima sit significativa: si vero tot sint unitates in uno quot in alio reliquo, videndum est per ultimas vel penultimas, et sic deinceps. In subtractione vero duo sunt numeri necessarii; scilicet, numerus subtrahendus, et numerus a quo debet fieri subtractio. Numerus subtrahendus debet sibi scribi per suas differentias, ita quod prima sub prima, secunda sub secunda, et sic de aliis. Subtrahe ergo primam figuram inferioris ordinis a figura sibi supraposita, et illa aut erit par, aut major, aut minor. Si par, ea deleta loco ejus ponatur cifra, et hoc propter figuras sequentes ne minus significant. Si major supponatur, tunc deleantur tot unitates quot contineat inferior figura et residuum loco ejus ponatur. Si minor quam, major numerus de minori subtrahi non potest, mutuatur unitas a figura proxima sequente quæ valet decem respectu precedentis figuræ; ab illo ergo denario et a figura a qua debuit fieri subtractio simul junctis subtrahatur figura inferior et residuum ponatur in loco figuræ deletæ. Si vero figura a qua mutuanda est unitas sit unitas, ea deleta loco ejus scribatur cifra ne figuræ sequentes minus significant deinde operare ut prius. Si vero figura a qua mutuanda est unitas sit cifra, accedet ad proximam figuram significativam et

ibi mutuatur unitas et in redeundo in loco cujuslibet cifrae pertransitae ponatur figura nonenarii; cum igitur perventum fuerit ad illam figuram de qua intenditur, remanebit tibi denarius ab illo ergo denario, et a figura non potest fieri subtractio simul junctis subtrahatur figura sibi supposita ut prius. Ratio autem quare loco cujuslibet cifrae pertransitae relinquitur nonenarii figura haec est. Si autem tertio loco mutuatur unitas illa respectu illius a qua debuit fieri subtractio, valet centum; sed loco cifrae pertransitae, relinquitur nonenarius qui valet nonaginta, unde remanet tantum denarius, et eadem erit ratio si a quarto loco vel a quinto vel deinceps mutuatur unitas. Hoc facto, subtrahere secundam inferioris ordinis a sua superiori, et negociandum est ut prius. Sciendum est quod tam in additione quam in subtractione possumus incipere operari a sinistra parte tendendo versus dextram; sed, ut dicebatur, fuit commodius. Si autem probare volueris utrum bene feceris, nec ne figuras quas prius subtraxisti adde superioribus, et concurrent eadem figurae si recte feceris, quas prius habuisti. Similiter in additione, quum omnes figuras addideris, subtrahas quas prius addidisti et redibunt eadem figurae quae prius habuisti, si feceris recte: est enim subtractio additionis probatio, et converso.<sup>9</sup>

<sup>9</sup> "Una species probat aliam; si itaque volueris explorare veritatem calculi in additione, subtrahere partes conjungendas ab aggregato: sique nihil remanet, vera est operatio. E contra vero, in subtractione exploraturus calculum, adde relictum ad



IV.—*Mediatio.*

Mediatio est numeri propositi medietatis inventio, ut videatur quæ et quanta sit illa medietas. In mediatione autem tantum est unus ordo figurarum et unus numerus necessarius, scilicet, numerus mediandus. Si ergo velis numerum aliquem mediare, scribatur ille numerus per suas differentias et incipe a dextris, scilicet, a prima figura versus dextram tendendo ad sinistram. Prima igitur figura aut erit significativa aut non: si non sit significativa, cifra præmittatur et fiat alterius: si vero fuerit significativa, ergo representabit unitatem aut alium digitum: si unitatem loco ejus deletæ ponatur cifra propter figuras sequentes ne minus significant, et scribatur illa unitas exterius in tabula, vel resolvatur illa unitas in sexaginta minuta, et medietas illorum sexaginta abjiciatur et reliqua medietas reservetur exterius in tabula, vel scribatur figura dimidii: sciendum tum quod nullum ordinis locum obtineat aliquod, tamen significat quod medietas duplata in suum locum recipiatur in duplicatione. Si autem prima figura significet alium digitum ab unitate, ille numerus aut erit par aut impar. Si par, loco ejus deletæ scribatur medietas illius numeri paris. Si impar, sume

numerum subtrahendum, cumque redit is, a quo subtractio facta est, justa est operatio."—*Winshemii Compendium Logisticæ Astronomicæ*, 12mo. 1563, Sig. B. 3.



numerum proximum parem sub illo contentum, et medietatem ejus pone in loco illius imparis deleti; de unitate autem quæ remanet medianda, fac ut prius. Hoc facto, medianda est secunda figura et negocianda est ut prius, si cifra præmittatur intacta. Si autem figura sit significativa, aut par aut impar erit: si par, loco ejus deletæ scribatur ejus medietas; si impar, aut erit unitas aut alius digitus numerum imparem representans. Si unitas, loco ejus deletæ scribatur cifra. Illa autem unitas cum valet decem respectu figuræ prioris de illis decem sumatur medietas: quinaris et addatur figuræ præcedenti. Si vero fuerit alius digitus numerum imparem representans, sume proximum parem sub illo contentum, et medietas ejus loco illius imparis deletæ ponatur: unitas autem quæ remanet medianda valet decem respectu figuræ præcedentis: dividatur ergo ille denarius in duos quinaris, et unus illorum abjiciatur, et reliquus addatur figuræ præcedenti ut prius. Si autem cifra fuerit cui debet addi quinaris, deleatur cifra, et loco ejus scribatur quinaris, et sic operandum est donec totus numerus mediatur qui scriptus fuerit.

#### V.—*Duplatio.*

Duplatio est numeri propositi ad seipsum aggregatio, ut videatur summa excrescens. In duplicatione tantum unus ordo figurarum est necessarius. In tribus speciebus precedentibus

inchoamus a dextra et a figura minori; in hac autem specie et in omnibus sequentibus inchoamus a sinistra et a figura majori: unde versus—

Subtrahis aut addis a dextris vel mediabis;

A leva dupla, divide, multiplicaque:

Extrahe radicem semper sub parte sinistra.<sup>1</sup>

Si enim velis incipere duplare a prima figura, continget idem bis duplare. Et licet aliquo modo possumus operari incipiendo a dextris, tum difficilior erit operatio et doctrina. Si igitur velis aliquem numerum duplare, scribatur ille numerus per suas differentias, et dupletur ultima figura. Ex illa igitur duplatione aut excrescit digitus, aut articulus, aut numerus compositus. Si digitus, loco illius deletæ scribatur digitus excrescens. Si articulus, loco illius deletæ scribatur cifra, et transferatur articulus, versus sinistram. Si numerus compositus, loco illius deletæ scribatur digitus qui est pars illius compositi et sinistretur articulus. Hoc facto, duplanda est ultima figura, et quicquid excreverit negociandum est, ut prius. Si vero occurrerit cifra, relinquenda est intacta. Sed si aliquis numerus cifræ debeat loco illius

<sup>1</sup> In Dionysii algorismo. MS. Bib. Reg. Mus. Brit. 8. c. iv. Vide *Arithmeticae Brevis Introductio*, per A. Lonicerum, 12mo. *Francof.* 1551:

“Addas, subducas a dextris multiplicesque;  
Dividit ac mediat deinde sinistra manus.”

Vide *Cirveli Algorismus*, 4to. *Par.* 1513. *Buclæi Arith. Memor.* 12mo. *Cantab.* 1613; et *Arithmetica Speculativa Bravardini*, 4to. *Par.* 1500.

deletæ scribatur numerus addendus, eodem modo negociandum est ut prius de omnibus: probatio hujus talis est: si recte mediaveris, dupla et occurrent eædem figuræ quas prius habuisti. Est enim duplatio mediationis probatio et converso.

### VI.—*Multiplicatio.*

Multiplicatio est numeri per se vel per alium, propositis duobus numeris, est tertii inventio qui contineat alterum illorum quot continentur unitates in reliquo. In multiplicatione duo sunt numeri necessarii, scilicet, numerus multiplicandus et numerus multiplicans. Numerus multiplicans adverbialiter nuncupatur. Numerus vero multiplicandus nominalem recipit appellationem: potest et jam tertius numerus assignari qui productus dicitur, perveniens ex ductione unius in alterum. Notandum est quod de multiplicante potest fieri multiplicandus et econverso, manente semper eadem summa, omnis numerus in seipso convertitur multiplicando. Sunt autem sex regulæ multiplicationis, quarum prima talis est: quinam digitus multiplicat digitum, subtrahendus est minor digitus ab articulo suæ denominationis per differentiam majoris digiti ad denarium, denario simul computato. Verbi gratia, si vis scire quot sunt quater in octo, vide quot sunt unitates intra octo et decem, denario simul computato, et patet quot sunt duo: subtrahatur ergo quaternarius a quadraginta bis et remanent

32, et hæc est summa totius multiplicationis. Similiter quando digitus multiplicat seipsum. Quando autem digitus multiplicat numerum compositum, ducendus est digitus in utramque partem numeri compositi, ita quod digitus in digitum per primam regulam, et digitus in articulum per secundam regulam; postea producta conjungantur simul, et erit summa totius multiplicationis. Quando articulus multiplicat articulum, ducendus est digitus a quo denominatur ille articulus in digitum a quo denominatur reliquus. Quando articulus multiplicat numerum compositum, ducendus est digitus articuli in utramque partem numeri compositi; conjungantur producta, et patebit summa totius. Quando numerus compositus multiplicat numerum compositum, ducenda est utraque pars numeri multiplicantis in utramque partem numeri multiplicandi et sic ducetur digitus bis, quia semel in digitum et semel in articulum. Articulus similiter bis, quia semel in digitum et iterum in articulum: hic tamen ubique articulus non ad principales extenditur articulos. Si igitur velis aliquem numerum vel per se vel per alium multiplicare, scribe numerum multiplicandum in superiori ordine per suas differentias, numerum vero multiplicantem in inferiori per suas differentias, ita tamen quod prima figura inferioris ordinis sit sub ultima superioris. Hoc facto, ducenda est ultima multiplicantis in ultimam multiplicandi. Ex illo igitur ductu aut excrescit digitus, aut



articulus, aut numerus compositus. Si articulus, ex directo figuræ multiplicantis scribatur cifra, et transferatur articulus versus sinistram. Si digitus, ex directo super positionem figuræ multiplicantis scribatur digitus excrescens. Si numerus compositus, ex directo figuræ multiplicantis scribatur digitus illius numeri compositi, et sinistretur articulus, ut prius. Hoc autem facto, ducenda est ultima numeri multiplicantis in ultimam multiplicandi, et quicquid inde excreverit, negociandum est, ut prius; et sic fiat de omnibus aliis numeri multiplicantis, donec perveniatur ad primam multiplicantis, quæ ducenda est in ultimam multiplicandi, et ex illo ductu aut excrescit digitus, aut articulus, aut numerus compositus. Si digitus, loco superioris deletæ scribatur digitus excrescens; si articulus, loco superioris deletæ scribatur cifra et sinistretur articulus: si numerus compositus, loco superioris deletæ scribatur digitus qui est pars illius numeri compositi et sinistretur articulus, ut prius. Hoc autem facto, anteriorandæ sunt figuræ numeri multiplicantis per unam differentiam, ita quod prima multiplicantis sit sub penultima multiplicandi, reliquis similiter per unum locum anterioratis. Quo facto, ducenda est figura ultima multiplicantis in illam figuram sub qua est prima figura multiplicantis, et ex illo autem ductu aut excrescit digitus, aut articulus, aut numerus compositus. Si digitus, ex directo figuræ suprapositæ addatur: si articulus, transferatur versus sinis-



tram, et figura directi supraposita relinquatur intacta; si numerus compositus, addatur digitus suprapositæ figuræ et sinistretur articulus. Similiter quælibet figura numeri multiplicantis in penultimam multiplicandi donec perveniatur ad primum multiplicantis, ubi operandum est ut prius, vel quemadmodum determinatur de primis; deinde anteriorandæ sunt figuræ per unicam differentiam, ut prius. Nec cessandus est a tali anterioratione nec a tali ductu. Quovis quælibet figura numeri multiplicantis ducatur in quamlibet figuram numeri multiplicandi. Si autem contingat quod prima figura numeri multiplicantis sit cifra et ei supponatur figura significativa, loco illius superioris deletæ scribenda est cifra. Si autem contingat quod cifra sit inter primam figuram et ultimam multiplicandi, anteriorandus est ordo figurarum per duas differentias, quamvis ex ductione alicujus figuræ in cifram nihil resultat. Ex perdictis ergo patet quod si prima figura numeri multiplicandi sit cifra, sub ea non debet fieri anterioratio. Sciendum autem quod in multiplicatione et divisione et radicum extractione competenter potest relinqui spacium vacuum inter duos ordines figurarum, ut ibi scribatur, quod pervenit addendum aut subtrahendum ne aliquid memoriæ intercidatur.<sup>2</sup>

<sup>2</sup> Vid. Piscatoris *Compendium Arithmeticæ*, 12mo. *Lips.* 1592. Ursini *Systema Arithmeticæ*, 12mo. *Colon.* 1619. Frisii *Arith. Pract. Methodus facilis*, 12mo. *Colon.* 1592. Tonstallus *de Arte Supputandi*, 4to. *Lond.* 1522.

VII.—*Divisio.*

Divisio<sup>3</sup> numeri per numerum est, propositis duobus numeris, majorem in tot partes distribuere quot sunt unitates in minori. Notandum ergo quod in divisione, tres numeri sunt necessarii; scilicet, numerus dividendus; numerus dividens, sive divisor; et numerus denotans quotiens. Numerus autem dividendus semper debet esse major, vel saltem par divisori, si debeat fieri divisio per integra. Si velis igitur aliquem numerum per alium dividere, scribe numerum dividendum in superiori ordine per suas differentias, divisorem vero in inferiori ordine per suas differentias, ita quod ultima divisoris sit sub ultima dividendi, penultima sub penultima, et sic de aliis, si competenter fieri possit. Sunt autem duæ causæ quare ultima sub ultima inferioris ordinis non possit collocari, quia aut ultima inferioris ordinis non possit subtrahi ab ultima superioris quod est minor inferiori, aut quæ licet ultima superioris possit subtrahi a sua superiori: reliquo tamen non possunt subtrahi a figuris sibi suprapositis, si ultima inferioris sit par figuræ suprapositæ. His itaque ordinatis,

<sup>3</sup> “Numeratio conjuncta, est multiplicatio aut divisio: multiplicatio est, qua multiplicandus toties addatur, quoties unitas in multiplicante continetur, et habetur factus: divisio est, qua divisor subducitur a dividendo quoties in eo continetur, et habetur quoties.” — *Rami Arithmetica*, Edit. 1581, pp. 11 et 14.

incipiendum est operari ab ultima figura numeri divisoris, et videndus est quotiens, possit illa subtrahi a figura sibi supraposita, et reliquæ a residuo sibi supraposito, si aliquid fuerit residuum. Viso ergo quotiens, figuræ inferioris ordinis possint subtrahi a suis superioribus, scribendus est numerus denotans quotiens ex directo supraposito illius figuræ sub qua est prima figura numeri divisoris, et per illam dividendæ sunt omnes figuræ inferioris ordinis a suis superioribus. Si autem contingat post anteriorationem quod non quotiens, possit subtrahi ultima figura divisoris a figura sibi supraposita super figuram sub qua est prima divisoris, recte scribenda est cifra in ordine numeri denotantis quotiens, et anteriorandæ sunt figuræ, ut prius; similiter faciendum est ubicunque contingit in numero dividendo quod divisor non possit subtrahi a numero dividendo, ponenda est cifra in ordine numeri denotantis quotiens et anteriorandæ sunt figuræ, ut prius: nec cessandum est a ductu numeri denotantis quotiens in divisorem, nec a ductu divisoris subtrahendæ donec prima divisoris sit subtracta a prima dividendi: quo facto, aut aliquid erit residuum aut nihil: si aliquid sit residuum, reservetur exterius et scribatur in tabula et erit semper unius divisoris. Cum igitur facta fuerit talis divisio, et probare volueris utrum benefeceris, multiplica numerum denotantem quotiens per divisorem et redibunt eædem figuræ quas prius habuisti, si nihil fuerit



residuum; sed si aliquid fuerit residuum, tunc cum additione residui redibunt eadem figuræ quas prius habuisti; et ita probat multiplicatio divisionem, et econtrario. Sed si facta multiplicatione, dividatur productum per multiplicantem, exhibunt in numero denotante quotiens figuræ numeri multiplicandi.

### VIII.—*Progressio.*<sup>4</sup>

Progressio est numerorum secundum æquales excessus ab unitate vel binario sumptorum aggregatio ut universorum summa compendiose habeatur. Progressionum alia naturalis sive continua, alia intercisa sive discontinua. Naturalis est quando incipitur ab unitate et non omittitur in accensu aliquis numerus, ut 1 . 2 . 3 . 4 . 5 . 6 . et cætera; et sic numerus sequens superat numerum precedentem unitate. Intercisa est quando omittitur numerus aliquis, ut 1 . 3 . 5 . 7 . 9 . et cætera. Similiter a binario possunt incipi, ut 2 . 4 . 6 . 8 . et sic numerus sequens superat precedentem numerum in duobus unitatibus. Notandum quod progressionis naturalis duæ sunt regulæ, quarum prima est

<sup>4</sup> “Progressio est numerorum æqualiter distantium in unam summam collectio. Progressio arithmetica continua sive naturalis est ubi post primum characterem nullus intermittitur. Progressio arithmetica discontinua sive intercisa, est figuris æqualiter interceptis numerorum ordo.” Hudaldrichus de Arithmetica, 12mo. *Frid.* 1550, p. 70. Vid. Glareanus de Algorismo, 12mo. *Par.* 1558, p. 20.



talis; quando progressio naturalis terminatur in numerum parem, per medietatem ipsius multiplica numerum proximum totali superiorem; verbi gratia, 1 . 2 . 3 . 4 . multiplica quinarium per binarium, et exhibunt decem, summa totius progressionis. Secunda regula talis est; quando progressio naturalis terminatur in numerum imparem, sume majorem partem illius imparis et per illam multiplica totalem numerum; verbi gratia, 1 . 2 . 3 . 4 . 5 . multiplica quinarium per ipsum trinarium, et resultabunt quidenarius, summa totius progressionis. Similiter de progressionem intercisa duæ dantur regulæ, quarum prima talis est; quando progressio intercisa terminatur in numerum parem, per medietatem illius multiplica numerum proximum medietati superiorem, ut, 2 . 4 . 6 . multiplica quaternariam per ternarium, et resultabunt duodecim, summa totius progressionis. Secunda regula talis est; quando progressio intercisa terminatur in numerum imparem, multiplica majorem portionem per se ipsam; verbi gratia, 1 . 3 . 5 . multiplica ternarium per se et exhibit nonenarius, summa totius progressionis.

### IX.—*Perambulum ad Radicum Extractionem.*

Sequitur de radicum extractione, et primo in quadratis: unde videndum est qui sit numerus quadratus et quæ sit radix numeri, et quid sit radicem ejus extrahere. Primo notandum tamen

est hæc divisio ; numerorum alius linearis, alius artificialis, alius solidus. Numerus linearis est qui consideratur tamen penes processum, non habito respectu ad ductionem numeri in numerum, et dicitur linearis, quia unicum tantum habet numerum, sicut linea unicam habet dimensionem, longitudinem sine latitudine. Numerus superficialis est qui resultat ex ductu numeri in numerum, et dicitur superficialis quia habet duos numeros denotantes sive mensurantes ipsum, sicut superficies duas habet divisiones; scilicet, longitudinem et latitudinem. Sed sciendum est qui dupliciter potest numerus duci in numerum aut semel aut bis: si numerus semel ducatur in numerum hoc erit in seipsum vel in alium. Sciendum quod si ducatur in se semel, fit numerus quadratus, qui, diversum scriptus per unitates, habet quatuor latera æqualia admodum quadranguli. Si ducatur in alium, fit numerus superficialis et non quadratus, ut binarius ductus in ternarium constituit senarium, numerum superficialem, et non quadratum; unde patet quod omnis numerus quadratus est superficialis et non convertitur. Radix autem numeri quadrati est ille numerus qui ita ducitur in se, ut bis duo sunt quatuor. Quaternarius igitur est primus numerus quadratus, et binarius est ejus radix. Si autem numerus bis ducatur in numerum, facit numerum solidum, ut dicitur, sicut solidus corpus tres habet dimensiones; scilicet, longitudinem et latitudinem et spissitudinem. Ita numerus iste

tres habet numeros ducentes in se. Sed numerus potest bis duci in numerum dupliciter, qui quot in seipsum aut in alium. Si igitur numerus bis ducatur in se vel semel in se et postea in suum quadratum sit numerus cubicus, et dicitur numerus cubicus ab nomine cubi quod est solidus. Est autem cubus quidam corpus habens sex superficies, solidos octo angulos, et duodecim latera. Si autem aliquis numerus bis ducatur in alium fit numerus solidus et non cubicus; ut bis tria bis constituerunt duodecim. Unde patet quod omnis numerus cubicus est solidus, sed non convertitur. Ex predictis igitur patet quod idem numerus est radix numeri quadrati et cubici, non tamen illius radices idem est quadratus et cubicus. Cum igitur ex ductu unitatis in se semel vel bis nihil perveniat nisi unitas, sicut dicit Boetius in arithmetica sua, quod omnis unitas potentialiter est numerus omnis, nullus autem auctus. Notandum autem quod inter quoslibet quadratos proximos continget reperire unicum medium proportionale, quod pervenit ex ductu radices numeri quadrati in radicem alterius. Item inter quoslibet duos cubicos proximos est reperire dicitur medium proportionale, scilicet, minus medium et majus. Minus medium pervenit ex ductu radices majoris cubici in quadratum minoris. Majus medium est, si ducatur radix minoris cubici in quadratum majoris. Cum igitur ultra summam numerorum solidorum in arte præsentis, non fiat processus, autem quatuor limites nume-



rorum distinguuntur : est enim limes numerorum ejusdem naturæ extremis contentorum terminis, continua ordinatio ; unde primus limes est novem digitorum continua progressio. Secundus novem articularum principalium est tertius centenariorum. Quartus novem millenariorum tres limites et resultant in composites per digitorum appositionem super quam cubum articularum trium predictorum, ut si alter alteri proponatur. Sed per finalis termini rationem ex millenariorum receptione super se semel per modum quadratorum, aut bis per modum solidorum, resultat penultima et ultimus limes.

#### X.—*Extractio radicum in quadratis.*

Radicem numeri quadrati extrahere est, proposito aliquo numero, radicem quadrati invenire, si numerus propositus quadratus fuerit. Si numerus vero non fuerit quadratus, tunc radicem extrahere est maximi quadrati sub numero proposito contenti invenire. Si velis igitur radicem alicujus numeri quadrati extrahere, scribe numerum illum per suas differentias, et computa numerum figurarum, utrum sit par vel impar. Si par, incipiendum est operari sub penultima. Si impar, ab ultima ; et, ut breviter dicatur, incipiendum est a figura posita in ultimo loco impari ; sub ultima igitur figura in impari loco posita, inveniendus est quidam digitus, qui ductus in se deleat totum sibi suprapositum respectu sui vel inquan-



tum vicinius potest; tali igitur invento, ducto digito et a superiori subtracto, duplandus est ille digitus, et duplatum ponendum est sub proxima superioris versus dextram et ejus duplum sub illo. Quo facto, inveniendus est quidam digitus sub proxima figura ante duplatum, qui ductus in duplatum deleat totum suprapositum respectu duplati; deinde ductus in se deleat totum suprapositum respectu sui vel in quantum vicinius potest: vel potest ita subtrahi digitus ultimo inventus ut ducatur in duplatum vel duplata et postea in se; deinde illa duo producta simul addantur, ita quod prima figura ultimi producti ponatur ante primam primi producti et superiora addatur primæ, et sic de aliis, et subtrahatur simul a totali numero respectu digiti inventi. Si autem contingit quod non possit aliquis digitus inveniri post anteriorationem, ponenda est cifra sub tertia figura versus dextram, et anteriorandum est primum duplatum cum suo subduplo: non cessandum est a talis digiti inventione, nec a digiti inventi duplicatione, nec a duplatorum anterioratione, nec a subdupli subduplo positione, donec sub prima figura inventus sit quidam digitus, qui ductus in omnes duplatos deleat totum suprapositum respectu sui vel in quantum vicinius potest. Quo facto, aut aliquid erit residuum aut nihil; si nihil constat, quamvis propositus fuerit quadratus et ejus radix est digitus ultimo inventus cum subduplo vel cum subduplis, ita quod proponatur: si vero aliquid fuerit residuum,

constat quod numerus propositus non fuerit quadratus. Sed digitus ultimo inventus cum subduplo vel subduplis est radix maximi quadrati sub numero proposito contenti. Si velis ergo probare utrum beneficeris necne, multiplica digitum ultimo inventum cum subduplo vel cum subduplis per eundem digitum, et redibunt eadem figuræ quas prius habuisti, si non fuerit residuum; sed si aliquid fuerit residuum, tunc cum additione illius redibunt eadem figuræ quas prius habuisti.

#### XI.—*Extractio radicum in cubicis.*

Sequitur de radicum extractione in cubicis: videndum est quid sit numerus cubicus et quæ sit radix ejus, et quid sit radicem cubicam extrahere. Est igitur numerus cubicus, sicut patet ex predictis, qui pervenit ex ductu alicujus numeri bis in se vel semel in suum quadratum: radix numeri cubici est ille numerus qui ita ducitur bis in se vel semel in suum quadratum. Unde patet quod numerus cubicus et quadratus eandem habuit radicem sicut supra dictum est. Radicem autem cubicam extrahere est numeri propositi radicem invenire cubicam, si numerus propositus sit cubicus: si vero non sit cubicus, tunc radicem cubicam extrahere est maximi cubici sub numero proposito contenti radicem cubicam invenire. Proposito igitur aliquo numero, cujus radicem velis extrahere cubicam;

primo computandæ sunt figuræ per quartas vel sub loco ultimo millenarii inveniendus est quidam digitus qui ductus in se deleat totum suprapositum respectu sui vel in quantum vicinior potest. Quo facto, triplandus est ille digitus et triplatum ponendum est sub proxima figura tertia versus dextram et ejus subtripulum sub subtriplo. Deinde inveniendus est quidam digitus sub proxima figura ante triplatum, qui cum subtriplo ductus in triplatum, deinde cum subtriplo ductus in productum deleat totum suprapositum respectu triplati. Deinde ductus in se deleat totum suprapositum respectu sui vel in quantum vicinior potest: hoc facto, triplandus est ille digitus iterum et ponendum est triplatum sub tertia figura ut prius, et ejus triplatum sub eo; postea anteriorandum est primum triplatum cum subtriplo per duas differentias. Deinde inveniendus est quidam digitus ante triplatus sub proxima figura, qui cum subtripulis ductus in triplata et postea sine subtripulis ductus in productum deleat totum suprapositum respectu sui vel in quantum vicinior potest. Nec cessandum est a talis digiti inventione, nec a digiti inventi triplatione, nec a triplatorum anterioratione per suas differentias, nec a subtriplo subtriplo positione, nec a tali multiplicatione, nec a subtractione, donec perventum fuerit ad primam figuram sub qua inveniendus est quidam digitus qui cum subtripulis ductus in triplata, deinde sine subtripulis ductus in productum deleat



totum suprapositum respectu sui vel in quantum vicinius potest. Notandum est quod productum perveniens ex ductu digiti inventi in se possunt addi et similiter simul contrahi a tali numero supraposito in respectu digiti inventi: hoc facto, aut aliquid erit residuum aut nihil: si nihil, constat quod numerus propositus fuit cubicus, et ejus radix est digitus ultimo inventus propositus cum subtriplicis vel subtriplo, quæ radix si ducatur in se et postea in productum erunt eadem figuræ quas prius habuisti. Si vero fuerit residuum, reservetur idem exterius in tabula, et constat quod ille numerus non fuit cubicus. Sed digitus ultimo inventus cum subtriplo vel subtriplicis est radix maximi cubici sibi numero proposito contenti, quæ radix si ducatur in se et postea in productum est maximus cubicus sub numero proposito contentus, et si illo cubico addatur residuum in tabula, erunt eadem figuræ quæ prius fuerunt. Si autem aliquis digitus post anteriorationem, non inveniri possit, tunc ponenda est cifra sub quarta figura versus dextram et anteriorandæ sunt figuræ ut prius. Notandum est, et quod si in numero proposito non est aliquis locus millenarii, incipiendum est operari sub prima figura. De extractione radicum dicta sufficient.



A METHOD USED IN ENGLAND IN THE  
FIFTEENTH CENTURY FOR TAKING  
THE ALTITUDE OF A STEEPLE OR  
INACCESSIBLE OBJECT.<sup>5</sup>

MS. LANSD. MUS. BRIT. 762. Fol. 23. B.

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HERE foloweth a rule howe a mann stondyng in a playne by a steple or such another thyng of height by lokyng vponn it shall knowe the certentie of the height thereof. First, let a mann consider by his estimacioun howe farre he stondeth from it be it xx, xxx, or xl fadam, And thereaboute as he demeth the certentie let hym stonde and there pitche a staffe the vpper poynte thereof to be iuste with his yie, he stondyng upp righte therby. And thann let hym leye hym

<sup>5</sup> It is scarcely necessary to observe that this method of proceeding could only have been practised by the more ignorant classes: the English mathematicians of that period were skilful in the application of the quadrant, and all other then known scientific instruments, as may be seen from their numerous works which still remain in manuscript in the various public and private collections of Great Britain. Fuller quaintly remarks, "I never did spring such a covey of mathematicians all at once, as I met with at this time."—*History of the Worthies of England*. Edit. 1811. Vol. II. p. 413.

downe alonge upp righte beyonde the staffe from the steple warde his feet juste to the staffe, and whann the staffe so stondesth he lying as is aforesaid, as his yie on the hyghest poynte of the staffe is juste with the height of the heighest poynte of the steple. Than the juste space from his yie as he lyith to the foote of the steple, that is to saye to that parte of the foote which is as litill as the top therof is the juste mesure of the height of the said steple. And if the staff stonde not juste let hymm remeve it till his yie he lying as is aforesaid with the highest poynte of the staf accorde with the highest poynte of the steple.

A TREATISE  
ON THE  
NUMERATION OF ALGORISM,

FROM A MS. OF THE 14<sup>TH</sup> CENTURY.

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To alle suche even nombrys the most have cifrys as to ten. twenty. thirfty. an hundred. an thousand and suche other. but ye schal vnderstonde that a cifre tokeneth nothinge but he maketh other the more significatyf that comith after hym. Also ye schal vnderstonde that in nombrys composyt and in alle other nombrys that ben of diverse figurys ye schal begynne in the rihth syde and so rekene backwarde and so he schal be wryte as thus—1000. the cifre in the rihth side was first wryte and yit he tokeneth nothinge no the secunde no the thridde but thei maken that figure of 1 the more signifycatyf that comith after hem by as moche as he born oute of his first place where he schuld yf he stode ther

tokene but one. And there he stonidith nowe in the ferye place he tokeneth a thousand as by this rewle. In the first place he tokeneth but hymself. In the secunde place he tokeneth ten times hymself. In the thridde place he tokeneth an hundred tymes himself. In the ferye he tokeneth a thousand tymes himself. In the fyfthe place he tokeneth ten thousand tymes himself. In the sexte place he tokeneth an hundred thousand tymes hymself. In the seveth place he tokeneth ten hundred thousand tymes hymself, &c. And ye schal vnderstond that this worde nombre is partyd into thre partyes. Somme is callyd nombre of digitys for alle ben digitys that ben withine ten as ix, viii, vii, vi, v, iv, iii, ii, i. Articles ben alle thei that mow be devyded into nombrys of ten as xx, xxx, xl, and suche other. Composititys be alle nombrys that ben componyd of a digyt and of an articule as fourtene fyftene thrittene and suche other. Fourtene is componyd of four that is a digyt and of ten that is an articule. Fyftene is componyd of fyve that is a digyt and of ten that is an articule and so of others . . . . . But as to this rewle. In the firste place he tokeneth but himself that is to say he tokeneth but that and no more. If that he stonde in the secunde place he tokeneth ten tymes himself as this figure 2 here 21. this is oon and twenty. This figure 2 stonidith in the secunde place and therfor he tokeneth ten tymes himself and ten tymes 2 is



twenty and so forye of every figure and he stonde after another toward the lest syde he schal tokene ten tymes as moche more as he schuld token and he stode in that place ther that the figure afore him stondesth: lo an example as thus 9634. This figure of foure that hath this schape 4 tokeneth but himself for he stondesth in the first place. The figure of thre that hath this schape 3 tokeneth ten tyme himself for he stondesth in the secunde place and that is thritti. The figure of sexe that hath this schape 6 tokeneth ten tyme more than he schuld and he stode in the place yer the figure of thre stondesth for ther he schuld tokene but sixty. And now he tokeneth ten tymes that is sexe hundrid. The figure of nyne that hath this schape 9 tokeneth ten tymes more than he schulde and he stode in the place ther the figure of 6 stondesth inne for thanne he schuld tokene but nyne hundryd. And in the place that he stondesth inne nowe he tokeneth nine thousand. Alle the hole nombre of these foure figurys. Nine thousand sexe hundrid and foure and thritti.

A TREATISE  
ON THE PROPERTIES AND QUALITIES OF GLASSES  
FOR OPTICAL PURPOSES,

ACCORDING TO THE MAKING, POLISHING, AND GRINDING OF THEM.

BY WILLIAM BOURNE.

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FROM MS. LANSD. MUS. BRIT. 121.

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EPISTLE DEDICATORY.

To the Right Honorable, and hys singuler good  
Lorde, Sir Wilyam Cicil, Baron of Burghley,  
Knight of the moste noble order of the garter,  
Lorde Highe Treasurer of Englande : Mr. of the  
Courte of Wardes and Liverys, Chancelour of the  
Vniversity of Cambridge, and one of the  
Queens Majestie's Honorable Privy Counsell.

Right Honorable, fynding myself moste deeply  
bounde, vnto youre Honour, in dyvers respects :  
And also youre Honours moste excellent and  
worthy skilles, and knowledge in all notable,  
laudable and noble experiences of learning in all  
maner of causes : And also, for that of late  
youre honour hathe had some conference and

speache with mee, as concerning the effects and qualityes of glasses, I have thought yt my duty to furnish your desyer, according vnto suche simple skill, as God hathe given me, in these causes, Whiche ys mucche inferiour vnto the knowledg of those, that ys learned and hathe red suche authors, as have written in those causes, and also have better ability and tyme, to seke the effects, and quality thereof, then I have, eyther elles can, or may, by the meanes of my small ability, and greate charge of children: Whiche (otherwyse) yt ys possible that I shoulde have bene better able to have done a number of thinges, that now I must of force leave, that perhapps shoulde have bene. And allso aboute seaven yeares passed, vppon occasyon of a certayne written Booke of myne, which I delivered your honour, Wherein was set downe the nature and qualite of water: As tuchinge ye sinckinge or swymminge of thinges. In sort youre Honoure had some speeche with mee, as touching measuring the moule of a shipp. Whiche gave mee occasyon, to wryte a litle Boke of Statick.<sup>6</sup> Whiche Booke since that tyme, hath bene profitable, and helpped the capacityes, bothe of some sea men, and allso shipp carpenters. Therefore, I have now written this simple, and breefe note, of the effects, and qualityes of glasses, according vnto the several formes, facyons, and makyngs

<sup>6</sup> The work here alluded to is probably his "Treasure for Travellers," which was published at London in 1578.

of them, and also the foylinges of them. That ys to saye, the foyle or using of them, that yow may not looke thorowe the Glass: Whiche causeth the Glass to cast a beame vnto your eye, acord- ing vnto the shape, or forme of any thinge, yt standeth against yt. And also the polishing and grynding of glasse, whiche causeth sondry effects: As in ye readinge hereafter dothe ap- peare the merveyulous nature and operation of glasses &c. I humbly desyring your Honour, to take this simple rude matter in good parte: And to accept yt as my good Will, allthoughe that the matter ys of none importance.

By your Honoures, dutyfully to Commande,

W. BOURNE.

### CHAPTER I.—*Introduction.*

Whereas the eye ys the principall member of the body neyther the Body in respect, coulde not moove any distance, but vnto perrill, yf yt were not for the sighte of the Eye, whose quality ys moste wonderfull, and hathe the largest prehem- inence of all the members of the body. For that the Eye ys able to discern and see any thinge, how farr down that the distance ys from yow: Yf the thinge bee of magnitude or bignes, corres- pondent vnto the distance. Now, this quality of the sighte of the Eye ys of no quantity or bignes:



But onely the quality of the eye ys to see, and begynneth at a poynte, withoute any quantity or bignes. As for example you may knowe yt by this : Pricke a hoale in any thinge, with the poynte of a fine needle, and then holde that vnto your Eye, and beholde any thinge thorowe the hole, and you may see a greater thinge, if that yt bee any distance from yow : yow may beholde a whole towne, beeynge a greate distance from you, &c. And for that perspective ys the discerning of any thinge either substancyall or accidentall, accordinge to the bignes, and distance, and hath his boundes, betweene too righte lynes, from a poynte : And so extending infinitely from the sight of the Eye, yt showeth yt self according to the quantity or bignes, correspondent vnto the distance. And for that perspective ys muche amplified and furered by the vertue and meanes of Glasses, I do thinke yt good to shewe the property of glasses : And suche, as touchinge the nature and quality of glasses, commonly called Lookinge Glasses. Whiche are those sortes of Glasses, that have a ffoyle, layde on the backe syde thereof, that causeth the same glasse to cast from yt a beame or shadowe, accordinge vnto the forme of that thinge that standeth ageanst yt shewynge yt vnto the sighte of the eye. Whereof there ys three severall sortes, accordinge vnto the sundry makeinge and polisshinge of these glasses : I do not meane sondry sortes of stuffe, ffor that there ys some sortes of lookinge glasses

that are made of metalles, which are commonly called steele glasses. But I do meane three sondry sorts of forms of making them. As in the one sorte, the beame will shewe ytself accordinge to the bignes, as yt ys: And in the other sorte yt will shewe ytself less, as in the order of the making of yt, the face of a man shall not shewe ytself as broade as the nayle of youre hande. And so accordingly you may make the glasse to shewe the face, at what bignes you lyst, vntill that yt shall shewe the face at inst the bignes thereof. And the thirde sorte of the making of glasses as you may make the glasse, in sorte, that you will make the face as bigg as the whole glasse, howe broade soever that the glasse ys, yow standing at some one assigned distance.

## CHAPTER II.

*In what forme to make Glasses, for to have yt shewe yt self, according to the bignes of the thinge.*

For to have a Glasse (to shewe the beame vnto the eye of that bignes that the thinge ys) That glasse must bee made flatt and playne; and being well polysshed, and smoothe, and well foyled on the back syde. Then you standinge righte with the middle thereof, you shall receave a beame vnto your eye of the trewe forme and shape of

your face, or any thinge, that standeth directly right against yt. But yf that you do stande any thinge oblique, or awrye, so shall you receave the beame, or see any thinge that maketh the lyke triangle, eyther acute, or sharpp, and obtuse or broad; Accordinge vnto the angle: that commeth from youre eye, vnto the glasse. So shall you receave, or see that beame, accordinge vnto the angle on the other syde, whatsoever that yt bee, howe farr soever that thinge ys in distance from the place, or neare hande.

### CHAPTER III.

*In what forme to make glasses for to have them shewe the forme or facyon of any thinge less in bignes then yt ys.*

To have a glasse to make any thinge shewe smaller then yt ys, That must be in the makeinge thereof made hillye or bossy outwards, and to have the foylle layde on the hollowe or concave syde, and so yt may bee made, that youre face showe in the beame that commeth to the eye, as small as you lyst, or any syse that ys less than your face at your pleasure. And for to have yt shewe very smalle, then let yt be made half a globe, or boawle, as smalle as a Tennys balle, and so the foylle layde on the concave or hollowe syde. So

shall the beame that ys cast vnto your eye, shewe your whole face, not to be so bigg as the nayle of your fingeres, and so you may make yt to bee hilly, or bossy outewardes, to have any thinge to shewe of what syse, that you lyst. For if that yt bee made as half a boawle or globe, Then of what syde soever you doo stande, you shall see youre owne face, or any thinge that standeth right as you do stande : And to bee in swellenes accordinge to the forme of the hylling or bossing outewardes. And allso as many tymes, that you doo see looking glasses, which make the face longer or broder then the forme or proportyon of your face, the reason thereof ys, that yt hilleth or bosseth more one way, then yt dothe another way. And that way that yt bendeth moste outewardes, that way yt maketh moste narrowest, and that way, that the glasse ys moste myghtest, that way yt sheweth the face moste longest. For yf that a glasse were made righte one way, and rounde outewardes the other way, and the foyle layde on the hollow syde, Then that Glasse woulde make the face, the streighte way, the inst lengthe of the face, and the other way narrowe accordinge vnto the roundinge of the glasse. So that all sortes of Lookinge glasses, that dothe bosse or hyll owtewardes, dothe shewe the thinge less then yt ys, accordinge vnto the bendinge hilling or bossinge outwarde.



## CHAPTER IV.

*In what maner of forme to make Lookinge Glasses, to make any thinge shewe bigger then yt ys.*

To make lookinge Glasses for to shewe any thinge bigger then yt ys, That Glasse muste bee made very large: for elles yt will not conteyne any quantitye in sighte; and this glasse must bee Concave inwardes, and well pollyshed of the hollowe or concave syde: and then the foylle must bee layde on that syde that doth swell, as a hyll, and bosse outwarde. And then this glasse, the property of yt ys, to make all thinges which are seene in yt to seeme muche bigger then yt ys to the syghte of the Eye, and at some appoynted distance, from the glasse, accordinge to the forme of the hollownes, the thinge will seeme at the biggest, and so yow standinge nearer the thinge will seeme less, vnto the sighte of the eye: so that, accordinge vnto the forme of the concavity or hollownes, and at some appointed distance from hym that looketh into the glasse, And yf that the glasse were a yearde broade, the beame that shoulde come vnto his eye, shall showe his face as broade, as the whole glasse, And to see his face in this glasse, hee must stande righte with the middle of the glasse, &c. And these sortes of glasses ys very necessary for

perspective: for that yt maketh a large beame, whereby that a small thinge may be seene, at a greate distance from you: and especially to bee amplified by the ayde of other glasses, &c.

## CHAPTER V.

*In what order to make a glass, that yow may looke thorow, that shall forther your sighte, and to have a small thyng to seem bigg, which ys very necessary for perspective: And yt may bee so made, that you may discerne a small thinge, a greate distance, and specyally by the ayde of other glasses.*

And nowe furdere more, as I have shewed before, the forme, and facyon of glasses, that dothe reflect a beame from the glasse, commonly called Lookinge Glasses: So in lyke manner I will shewe you the makinge of Glasses called perspective glasses, that do helpe sighte, by the meanes of the beame, that pearceth commonly thorowe the glasse. And first for makinge of the smallest sorte of them, commonly called spectacle glasses. These sortes of glasses ys grounde vppon a toole of Iron, made of purpose, somewhat hollowe, or concave inwardes. And may be made of any kynde of glasse, but the clearer the better. And so the Glasse, after that yt ys full rounde, ys made fast with syman vppon a smalle block,

and so grounde by hande, vntill that yt ys bothe smoothe and allso thynne, by the edges, or sydes, but thickest in the middle. And then yt ys the quality or property of the Glasse that ys cleare, to shewe all thinge, that ys seene through yt, to seeme bigger and perfecter, then that yow may see yt withoute the Glasse, and the thynner vnto the sydes and edges. And the thicker that yt ys in the middle, the bigger or larger any thinge sheweth vnto the eye, and yf that the glasse bee very cleare, the more perfecter, &c. And now allso in lyke manner for to make a glasse for perspective, for to beholde, and see any thinge, that ys of greate distance from yow, which ys very necessary: for to viewe an army of men, or any castle, or forte, or such other lyke causes. Then they must prepare very cleare, and white Glasse that may bee rounde, and beare a foote in diameter; as fyne and white Vennys Glasse. And the larger, the better: and allso yt must bee of a good thicknes, and then yt must bee grounde vppon a toole fitt for the purpose. Beynge sett fyrst vppon a syman block, and firste, grynde on the one syde, and then on ye other syde, vntill that the sydes bee very thynn, and the middle thicke. And for that yf the glasse bee very thicke, then yt will hynder the sighte. Therefore yt must bee grounde vntill that the myddle thereof bee not above a quarter of an ynche in thickness: and the sydes or edges very thynne, and so polysshed or cleared. And so



sette in a frame meete for the purpose for use : so that yt may not be broken. And so this glasse being made in this forme, Then yt wille have three marvellous operacyons, or qualities, as hereafter you shall see.

## CHAPTER VI.

*The first, and the Principall quality of this Glasse, and ys, as touchinge perspectyve.*

The quality of the Glasse, (that ys made as before ys rehearsed) ys, that in the beholding any thinge thorowe the glasse, yow standinge neare vnto the Glasse, yt will seeme thorow the glasse to bee but little bigger, then the proportion ys of yt : But as yow do stande further, and further from yt, so shall the perspective beame, that commeth through ye glasse, make the thinge to seeme bigger and bigger, vntill suche tyme, that the thinge shall seeme shall seeme <sup>7</sup> of a marvellous bignes : Whereby that these sortes of glasses shall muche proffet them, that desyer to beholde those things that ys of great distance from them : And especially yt will be much amplified and fundered, by the receavinge of the beame that commeth thorow the glasse, somewhat

<sup>7</sup> This repetition of the words "shall seeme" is evidently a mistake, but being in the original MS. I have retained it in the text.



concave or hollowe inwardes and well polysshed as I will hereafter furder declare.

## CHAPTER VII.

*The seconde quality of this glass made in the forme before declared.*

The quality of this Glass ys, if that the sunne beames do pearce throughe yt, at a certayne quantity of distance, and that yt will burne any thinge, that ys apte for to take fyer : And this burnynge beame, ys somewhat furder from the glasse, then the perspective beame.

## CHAPTER VIII.

*The thyrde quality of this kynde of Glass, that ys grounde, and made in that forme before declared, ys to reverse, and turne that thyng that yow do beholde, thorowe ye glass, to stande the contrary way.*

And yf that yow doo beholde any thinge thorowe this Glasse, and sett the glasse furder from yowe then the burnynge beame, and so extendynge after that what distance that yow list, all suche thinges, that yow doo see or beholde, thoroughe the glasse, the toppes ys turned downwardes. Whether that yt bee trees, hilles, shippes on the water, or any other thinge what-

soever that yt be : As yf that yt were people, yow shall see them thorough the Glasse, theyre heades downwardes, and theyre feete vpwardes, their righte hande turned to theyre lefte hande, &c. So that this kynde of Glasse beyng thus grounde hath three marvellous qualites. For at some assigned, or appoynted distance, accordinge vnto the gryndinge of the Glasse, bothe in his diameter, and thicknes in the middle, and thinnes towardes the sydes. That (beholdinge any thinge thorowe the glasse) yt shall make the best perspective beame : So that the thinge that yow doo see thorowe shall seeme very large and greate : and more perfitter withall. And also standing further from the glasse yow shall discerne nothinge thorowe the glasse : But like a myst, or water : And at that distance ys the burninge beame, when that yow do holde yt so that the sunne beames dothe pearce thorowe yt. And also yf that yow do stande further from the glasse, and beholde any thinge thorowe the glasse, Then you shall see yt reversed and turned the contrary way, as before ys declared. So that accordinge vnto youre severall standinge, nearer, or furder from the Glasse, beholding any thinge thorowe yt. Suche, yt hath his perspective beame : and then standinge furder from the glasse, and then all things seen thorowe, shall shewe vnto the sighte of your eye, cleene turned, and reversed another way, whatsoever that yt bee.

## CHAPTER IX.

*The effects what may bee done with these two last sortes of glasses: The one concave with a foyle, vppon the hylly syde, and the other grounde and pollished smoothe, the thickest in the myddle, and thinnest towordes the edges or sydes.*

For that the habillity of my purse ys not able for to reache, or beare the charges, for to seeke thorowly what may bee done with these two sortes of Glasses, that ys to say, the hollowe or concave glasse: and allso that glasse, that ys grounde and polysshed rounde, and thickest on the myddle, and thynnest towards the sydes or edges, Therefore I can say the lesse vnto the matter. For that there ys dyvers in this Lande, that can say and dothe knowe mucche more, in these causes, then I: and specially Mr. Dee, and allso Mr. Thomas Digges, for that by theyre Learninge, they have reade and seene many moo auctors in those causes: And allso, theyre ability ys suche, that they may the better mayntayne the charges: And also they have more leysure and better tyme to practyze those matters, which ys not possible for mee, for to knowe in a nombre of causes, that thinge that they doo knowe. But notwithstanding upon the smalle prooffe and experyence those that bee but vnto small purpose,

of the skylles and knowlledge of these causes, yet I am assured that the glasse that ys grounde, beyng of very cleare stufte, and of a good largenes, and placed so, that the beame dothe come thorowe, and so reseaved into a very large concave lookinge glasse, That yt will shewe the thinge of a marvellous largeness, in manner vncredable to bee beleaved of the common people. Wherefore yt ys to bee supposed, and allso, I am of that opinyon, that havinge dyvers, and sondry sortes of these concave lookinge glasses, made of a great largeness, That suche the beame, or forme and facyon of any thinge beeyng of greate distance, from the place, and so reseaved fyrste into one glasse: and so the beame reseaved into another of these concave glasses: and so reseaved from one glasse into another, beeyng so placed at suche a distance, that every glasse dothe make his largest beame. And so yt ys possible, that yt may bee helped and furdered the one glasse with the other, as the concave lookinge glasse with the other grounde and polysshed glasse. That yt ys lykely yt ys true to see a smalle thinge, of very greate distance. For that the one glasse dothe rayse and enlarge, the beame of the other so wonderfully. So that those things that Mr. Thomas Digges hathe written<sup>8</sup> that his

<sup>8</sup> "My father by his continual paynfull practises, assisted with demonstrations Mathematicall, was able, and sundrie times hath by proportionall Glasses duely situate in convenient angles, not onely discovered things farre off, read letters, numbred



father hathe done, may bee accomplisshed very well, withowte any dowbte of the matter : But that the greatest impediment ys, that yow can not beholde, and see, but the smaller quantity at a tyme.

peeces of money with the very coyne and superscription thereof, cast by some of his freends of purpose vppon Downes in open fieldes, but also seven myles of declared what hath been doon at that instante in private places.”—*Pref. to Pantometria*. Edit. 1571. Sig. A. iii. b.

# JOHANNIS ROBYNS

DE COMETIS

COMMENTARIA.

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DEDICATIO.

AD invictissimum principem Henricum ejusdem nominis octavum, Serenissimum Anglorum Regem, de cometis commentaria Johannis Robyns sui Alumni, et socii Collegii Omnium Animarum, Oxoniæ.

Quanquam omnes philosophiæ partes (Princeps Illustrissime) tum utiles, tum jucundæ sint; ea tamen philosophiæ portio, quæ de cælis, cælorumque motibus ordine ac influentiis agit, cæteris longe præstantior, multo jucundior, et pene divinum quid nobis esse videtur. Id quod luculentius apparebit, si de his, quæ in aliis philosophiæ partibus tractantur, pauca dixerimus. Et primam a crassissimo, et infimo elemento, scilicet terra, orationem inchoabimus, quæ in media mundi sede collocatur, cernitur solida

globosa, et undique nutibus suis conglobata; floribus, herbis, arboribus, frugibus ornata, quorum omnium incredibilis multitudo insatiabili varietate distinguitur. Adde etiam fontium gelidas perhennitates; liquores perlucidos amnium; riparum vestitus viridissimos; speluncarum concavas altitudines; saxorum asperitates; impendentium montium sublimitates; immensitatesque camporum. Adde etiam reconditas auri, argenti, metallorumque venas, infinitamque vim marmoris. Quæ vero, et quam varia genera bestiarum, vel cicurum, vel ferarum! qui volucrum lapsus! atque cantus! qui pecudum pastus! quæ vita silvestrium! Quid jam de hominum genere loquar! qui quasi cultores terræ constituti, nec patiuntur eam immanitate belluarum efferari, nec stirpium asperitate vastari. Quorumque operibus agri, insulæ, littoraque collucent, distincta tectis et urbibus. Jam de liquidibus et fusilibus elementi (maris inquam) pulchritudine pauca dicamus oportet. Cujus quidem maris speciem, et animantium quæ in eodem continentur, satis admirari nequeo. Nam ipsum mare undique terram circumfluens, continentes, insulas, peninsulas, et isthmos efficit, et quatenus diversas alluit regiones, et diversa sortitur nomina; ut mare Britannicum, Gallicum, Libicum, Punicum, et cætera. Ac ita quidem terram appetens circumquaque littoribus claudit, et quasi una ex duabus naturis conflata videatur. Quid de piscibus, bellisque marinis dicam?

Quot genera, quamque disparia, partim submersarum, partim fluitantium, partim innatantium belluarum, partim ad saxa nativis testis inhærentium? De quarum generatione, proprietatibus, et natura, Aristoteles omnium philosophorum facile princeps in historia naturali acutissime disputat. Exinde mari finitimus est aer; cujus suprema portio purior quidem, et sincerior, cœli orbiculationem (sicuti et ipse ignis) subsequitur. Media vero aeris plaga quæ (ut doctiores sentiunt) non parum frigescit, aptior deputatur locus, ubi vapores elevati in nubes concrecant. Inibi etiam fulmina, fulgetra, et tonitruum sedes sibi peculiare vendicant. At infima aeris regio, quæ partim terræ, partim aquatico elemento conterminata junctaque cernitur, avium volatus sustinet, et salutarem, vitalemque spiritum animantibus quidem terrestribus ministrat. Jam ab aere ad ignem postea nostra demigrabit oratio, qui, ex elementis in supremo ac maxime sublimi loco constitutus, aerem in sua concavitate fovens, orbiculariter complectitur. Sicut aer aquam, et aqua terram undique circuit, nisi que una pars terræ propter vitam quorundam animantium tuendam aquis discooperta relinquitur. Neque sentiendum est, qua deus et natura inaniter, ac superflue hoc quartum corpus simplex scilicet ignem superaddiderunt. Aeris enim caliditas ab aquæ terræque frigiditate ilico consumeretur, nisi superior ignea vis calefactiva aerem refocillaret. Præterea terræ siccitas ab aere et aqua



facillime obrueretur, nisi ignis vim suam arescen-tem emittens, aeris humiditatem deliniret. Hac-tenus succincte de elementis, cæterisque corpo-ribus, quæ infra sphæram activorum et passivorum continentur. Quarum rerum scientia, si (ut revera est) jucunda et delectabilis fuerit, quid de illorum corporum cognitione, quæ cœlestia æter-naque esse feruntur sentiendum est? A quorum influentiis et virtutibus tum elementata (ut ita dicamus) suum regimen sortiuntur. Ab istis enim orbis terrarum plagæ ac regiones habitatae quibusdam certis temporum vicibus suas magnas hyemes et æstates (ut Aristotelico utar verbo) recipiunt. Magna autem æstas dicitur cum aliqua provincia ex nimia siccitate et fervore ita sterilescit, ut diutius inhabitatores fovere ne-queat. Versa ince, magnam hiemem alicujus regionis appellamus, cum humectantes cœlorum influentiæ sic in eadem regione sæviunt, ut terra fluctibus et aquis penitus obruatur; id quod ab aliquibus vocatur diluvium particulare: et non solum istæ prodigosæ mutationes cœlorum constellationibus tanquam causis attribuuntur, verum etiam quæ diversæ regiones diversa progignunt, corporum cœlestium benignitati aut asperitati primi-tus ascribitur. Quælibet enim terræ habitabilis portio, suos fructus et fruges, arbores, herbas, ac frutices, lapides etiam pretiosos et mineralia, pro cœli qualitate et influentiis producit. Quid de fertilitate et abundantia, pace atque tranquillitate, fame, bello, pestilentia, et brutorum animan-

tium strage dicam? quid de sectis, legibus, civitatibus, imo et regnis integris loquar? Quorum omnium fœlicitas et infœlicitas, mala, damna, et infortunia, successiones, prosperitates, et bona, dispositive saltem a cœlorum constellationibus dependent. Nec minorem certe potestatem in liquido elemento (inquam) in mari influentiæ cœlestes exercent. Maris enim fluxus, et refluxus æstuosi, in istis fretorum angustiis, a virtutibus lunæ demanant. Præterea piscium et marinarum belluarum ortus, et interitus, augmentationes, diminutiones, et alterationes; necnon eorundem copia, ac penuria, astrorum virtutibus (omnium doctissimorum consensu) ascribuntur. At in aere quam manifestum imperium habent sidera, quorum præsentia vel absentia efficitur, ut idem aer nunc fulgentissima luce splendescat, nunc obscurus et tenebrosus relinquatur. Sol etenim exoricens, suis clarissimis radiis aerem illustrans, diem conficit, et cum primum a nobis recesserit subter cardinem occidentalem . . . . ., subrepta nox, quippe quæ nil aliud est, quam ut aer (propter solis sub horizonte dilapsus) tenebris offundatur. Rursus et a solis cursu sub zodiaco quatuor anni tempora, ver, æstas, autumnus, et hyems proficiscuntur. In quibus equidem temporibus sol aerem et cætera elementa tum tristitia quadam contrahit, tum vicissim ita lætificat, ut cum ipso cœlo exhilarata esse videantur. Nolim hic in cæterarum stellarum (quæ erraticæ dicuntur) ratione, ordine et influentiis multus videri, qua-

rum tantus est concentus ut cum summa Saturni infrigidet, media Martis accendat, his interjecta Jovis stella temperet et illuminet, infraque Martem tres soli obediunt; Luna, Venus, et Mercurius. Et hæ omnes stellæ quas errores appellamus, iisdem vagantur spatiis, quibus et sol, et eodem modo circa terram agitatae oriuntur, et occidunt, quarum motus nunc incitantur, nunc retardantur, suisque aspectibus et influentiis, (secundum quod sub variis discurrant signis) quatuor anni tempora nunc calidiora, nunc frigidiora, nunc humidiora, nunc sicciora redeunt: qua contemplatione nihil pulchrius, nihil admirabilius esse potest. Quid de gelu, nive, grandine, ventis, pluvia tonitruo, fulmine, fulgetro, stellis item caducis et per aerem discurrentibus dicam? quæ omnia ab astrorum constellationibus progrediuntur. Postremo et illa crinita sidera famosa quidem et portentosa cœlestium stellarum vires, causam suæ generationis, et, si rarius spectantur, æque naturaliter sibi, vendicant, atque ea quæ ab oculis quotidie videntur. Sed plebei quamvis numerosa rerum naturalium multitudo recitari possit, quarum causæ secretiores et magis abditæ sunt, tamen ob insolitam ipsius rei faciem maximopere cometas admirantur. De quibus siquidem cometis tua sacrosancta majestas voluit, ut a nobis quædam commentaria in lucem æderentur. Id quod non hac quidem de causa factum erat (certissime scio) ut in his nostris perlegendis, tua sacrosancta majestas quidpiam eruditionis exhauriret, sed



aliorum consulens utilitati. Ut qui harum rerum (de quibus tractamus) minus essent periti ex nostris commentariis aliquid saltem adipisci possent. Non enim incognitum est (eruditissime Princeps) quam singularis in scientiis mathematicis tua fuerit doctrina. Id quod ex illis disputationibus manifestissime mihi perspectum erat, quas de cometarum naturis et effectibus tum Woydstokiæ, tum Bokynghamiæ nobiscum habuisti, quis enim invenire poterat argutius, quis colligere veruosius, quis explicare venustius? In aliis vero scientiis et potissime theologia (serenissime Rex) quam præstantissima tua fuerit cognitio, nihil dicturus sum. Opera enim ea quæ a tua sacrosancta majestate edita sunt, sufficienter ostendunt. In quibus equidem operibus (ut illud quod sentio ingenue dicam) nec Augustino, nec Hieronimo cædere videris. Nam quam caste quam nitide, quam polite omnia mihi disputantur, solidi, succi, et nervorum plena, sed temperabo me a laudibus. Scio etenim, scio (laudatissime Princeps) quam nolunt laudari hi, qui laudes maximæ merentur omnium.

[*From what is here given the nature of the work may be seen, and I do not think it as a whole necessary to be printed in this place.—ED.*]



# TWO TABLES:

ONE SHEWING THE TIME OF HIGH WATER AT LONDON  
BRIDGE, AND THE OTHER THE DURATION OF  
MOON LIGHT.

FROM A MS. OF THE 13<sup>TH</sup> CENTURY.

*Bib. Cott. Mus. Brit. Jul. D. vii. Fol. 45, b.*

FLOD AT LONDON BRIGGE.

Ætas Luna.	Hore.	Minuta.	Ætas Luna.	Hore.	Minuta.
1	3	48	16	3	48
2	4	36	17	4	36
3	5	24	18	5	24
4	6	12	19	6	12
5	7	0	20	7	0
6	7	48	21	7	48
7	8	36	22	8	36
8	9	24	23	9	24
9	10	12	24	10	12
10	11	0	25	11	0
11	11	48	26	11	48
12	12	36	27	12	36
13	1	24	28	1	24
14	2	12	29	2	12
15	3	0	30	3	0

QUANTUM LUNA LUCET IN NOCTE.

Ætas Luna.	Hore.	Minuta.	Ætas Luna.	Hore.	Minuta.
1	10	48	16	11	12
2	1	36	17	10	24
3	2	24	18	9	36
4	3	12	19	8	48
5	4	0	20	8	0
6	4	48	21	7	12
7	5	36	22	6	24
8	6	24	23	5	36
9	7	12	24	4	48
10	8	0	25	4	0
11	8	48	26	3	12
12	9	36	27	2	29
13	10	24	28	1	36
14	11	12	29	0	48
15	12	0	30	0	0

# A TREATISE

ON THE

## MENSURATION OF HEIGHTS AND DISTANCES.

FROM A MS. OF THE 14TH. CENTURY.

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*Bib. Sloan. Mus. Brit. 213. xiv. Fol. 120.*

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*Nowe sues here a Tretis of Geometri wherby  
you may knowe the heghte, depnes, and the  
brede of mostwhat erthely thynges.*

Geometri<sup>9</sup> es saide of þis greke worde *geos*.  
þat es erthe on englisch. and of þis greke worde

<sup>9</sup> Vid. MS. Bib. Reg. Mus. Brit. 17 A. 1. f. 2<sup>b</sup>-3.

“The clerk Euclýde on þis wyse hit fonde  
Thys craft of gemetry yn Egypte londe  
Yn Egypte he tawghte hyt ful wyde,  
Yn dyvers londe on every syde.  
Mony crys afterwarde y vnderstonde  
Gher þat þe craft com ynto þys londe.  
Thys craft com ynto England, as y ghow say,  
Yn tyme of good kyng Adelstones day.”

This notice of the introduction of Euclid's Elements into England, if correct, invalidates the claim of Adelard of Bath, who has always been considered the first that brought them from abroad into this country, and who flourished full two centuries

*metros.* þat es mesure on englisch. þan es geometri als erthly mesure. for it es one of þe sevene science techyng to mesure þe erth in heght. depnes and brede. and length. THIS TRETIS ES DEPARTED IN THRE. þat es to say. hegh mesure.

after the "good kyng Adlestone." Adelard translated the Elements from the Arabic into Latin, and early MSS. of the translation occur in so many libraries, that we may fairly conclude that it was in general circulation among mathematicians for a considerable time after it was written. Tiraboschi was the first who remarked, that the translation attributed to Campanus, was in reality Adelard's, with a commentary by the former, (*Libri Hist. des Mat. tom. ii. p. 48*); there are also several MSS. in the titles to which this is expressly stated, (MS. Bib. Bodl. Seld. Arch. B. 29. MS. Bodl. 3623. MSS. Paris, Lat. 7213, 7214, 7215. MS. Harl. Mus. Brit. 5266: "per Adelardum Bathoniensum de Arabico in Latinum translatus, cum Commento Campani Novariensis."). In the Library of Queens' College, Cambridge, there was formerly a MS. entitled "Geometria Euclidis cum Commentario Adelardi" (*Lelandi Collect. tom. iii. p. 19*), and Chasles (*Aperçu Historique, p. 509,*) mentions one in the library of the Dominicans of St. Marc at Florence, under the same title; this would appear to intimate that the commentary is also by Adelard, and many MSS. in which the name of Campanus does not appear, contain the commentary, (MS. Oxon. in Coll. S. Trin. 30, iv. MS. Harl. Mus. Brit. 5404. MS. Bib. Pub. Cant. Dd. 12, 61). Doctor John Dee, in the Catalogue of his Collection of MSS. (MS. Harl. 1879. MS. Bib. Trin. Coll. Cant. Collect. Gal. O. 4, 20. MS. Ashm. 1142.) gives the title of one, in which the books of Euclid on Optics and Catoptrics, as well as the Elements, appear under Adelard's name.

There have been two independent notices of the plagiarism of Campanus; one by Charles Butler, (the author of the "Introduction to the Mathematics," 8vo. 1814,) in some MS. papers in the Editor's possession: the other by the Author of the article *Geometry*, in the "Penny Cyclopædia."

playne mesure. and depe mesure. First foryi shewe we hegh mesure. þat es to say howe any thyng þat has heght may be met howe hegh it es. and þis may be done in many maneres. first perfor schewe howe it may be done by þe quadrant. When you wille wite þe heghte of any thyng þat you may negh. biholde þan þe heght of þat thyng by bothe holes of þe quadrant and come toward and go froward til þe perpendicle þat es to say þe threde whereon þe plumbe henges falle vpon þe mydel lyne of þe quadrant. þat es to say þe 45 degre. þan take als mykel lande behynde ye as fro þethen to þe erthe and marke wele þat place. þan mete howe many fete are bytwene þi mark and þe fondement of þat thyng whos heght you sekest. and sekirly so many fote heght it es. Also when you wilt wite þe heght of any thyng by þe quadrant. biholde þe heght of þat thyng by bothe þe holes. and byholde vpon what place of þe quadrant þe perpendicle falles. for ouþer it wille falle on þe vmbre toward or on þe vmbre froward. and if it falle vpon þe vmbre toward biholde vpon whilk poynte of þat vmbre þe perpendicle falles. þan mesure þe distaunce þat es to say þe space betwene ye and þat thyng whos heght you sekas, and when you has so done þan multiply you by 12 þat same mesure. þan al þat comes of þat multiplyeng departe you by þe nonmbre of þe poyntes of þe vmbre. and to alle þat comes þereof set þe quantite of þin heghte. and set al þis togydere. and þan you has þe



heght of þe thyng whos heght you sekcs. If  
 peradventure þe perpendicle falle vpon þe vmbre  
 froward biholde þan þe poyntes þereof and torne  
 þem into þe poyntes of þe vmbre toward and do  
 furth þan as we taght byfore and þus sekirly you  
 sale have þe heght of þe thyng whos heght you  
 sekcs. namely so þe space be playne bitweene þe  
 and it. Note you þat þe quadrat. þat es to say  
 4 square whilk es descryvede þat es to say  
 schewed in þe quadrant has tuo sides. þat es to  
 say þe side of þe vmbre toward. and þe side of þe  
 vmbre froward. and aþer of þese 2 sides es depar-  
 ted in 12 even parties. When you holdes þe cone  
 of þe quadrant. þat es to say þe cornel of þe  
 quadrant even vpryght in whilk cornel es þe nayle  
 whereby þe perpendicle henges. þan þe circum-  
 ferens. þat es to say þe cumpasse es toward þe  
 erth. þan þat side of þe quadrat whilk es nere  
 ye es called þe vmbre toward and þat oþer side es  
 called þe vmbre froward. and þe 12 departynges  
 of aþer of þo sides are called poyntes. þan es  
 a poynte þe twelft parte of any thyng. namely of  
 ouþer side of þe quadrat in þe quadrant. Also  
 when þe heght of þe sonne es more þan 45 degrees.  
 þan þe perpendicle falles vpon þe vmbre toward.  
 And ageynward when þe heght of þe sonne es less  
 þan 45 degrees. þan þe perpendicle falles vpon þe  
 vmbre froward. When sothly þe heght of þe  
 sonne es even 45 degrees. þan þe perpendicle  
 falles even vpon þe 45 whilk es þe medil lyne.  
 If you may nocht negh þe thyng þat you wolde

mesure for letting of water or summe oþer thyng bitwene. þan biholde þe heght þereof by bothe þe holes. and biholde þe nonmbre of þe poyntes of þe vmbre toward. namely vpon whome þe perpendicle falles. þan set D for a mark in þat place where you stondes þan. go ferre or nerre þat thyng whos heght you sekis. and þat by an evene lyne and beholde este þe forsaide heght by bothe holes. þan þere stondyng seke þe nonmbre of þe poyntes of þe vmbre toward. and set þere C for anoþer mark. þan mesure howe many fete are bitwene þise tuo markes D and C and kepe þat wele in þi mynde. þan abate þe lesse nonmbre of þese tuo in þe vmbre toward fro þe more and kepe wele þe difference bytwene þo tuo nonmbres. þan multiplie by twelve þe distaunce bitwene þe forsaide D and C and alle þat comes of þat multeplyeng departe you by þe distaunce of þe poyntes. and to þat þat leves over. set als mykel as fro þethen to þe erthe and þan sekirli you has þe heght of þat thyng. bot loke þe holes of þi quadrant be right straite and elles you may lightly be deceyvede. Peraventure you standes in an aley. and þe thyng þat you wolde mete es vp on an hegh hille. first þan biholde þe heghte of þe hille by both þe holes of þe quadrant. and þat by tuo stondynges of D and C as we taght nowe next bifore. and marke þat wele in þi mynde. þan biholde in þe same wise þe heght of the hille and of þat same thyng togedire. þan abate þe heght of þe hille

fro al þat remenant and þan sekirly hast ou þe heght of þat thyng. If peraventure þe contry es hilly. þan do þat þe perpendicle falle even vpon þe begynnyng of þe side of þe vmbre froward. þan se by bothe holes in þe thyng to be mesured þe poynte þat es called A and do as we taght bifore. and þat leues after þi wirkyng es þe heght fro A poynte to þe heght of þe thyng: bot þan salt you noght set þereto þe heght of þi stature. Parcas you woldest mesure þe heght of a thyng by the schadowe þereof. þan abyde til þe sonne be in þe heght of fyve and fourti degrees. þan mesure þe vmbre of þat thyng and þat es þe heght þereof. If you wilt mesure þe heght of any thyng by þe schadowe þat es to say þe vmbre þereof in ilk houre þan do þus. mesure þe vmbre þat es to say þe schadowe of þat thyng. and multiply þat by 12 and al þat departe þan by þe poyntes of þe vmbre toward. and þe nonmbre howe ofte euer it be es þe heght of þat thyng if þe perpendicle falle vpon þe vmbre toward. If þe perpendicle falle vp þe poyntes of þe vmbre froward. þan multeply þe vmbre. þat es to say þe schaddowe by þe poyntes of þat vmbre. and al þat departe by 12 and þe nonmbre howe oft it be. es þe heght of þat thyng. Or if you wilt. lede þe poyntes of þe vmbre froward into þe poyntes of þe vmbre toward. and þan multeply þe vmbre. þat es to say þe schaddowe of þat thyng by 12 and þan al þat departe by þe



poyntes of þe vmbre ladde. Whilk after þe ledying are poyntes of þe vmbre toward. Take þe poyntes of the vmbre þus. late þe sonne benies passe by bothe holes. and mark where þe perpendicle falles. þan counte þe poyntes fro þe begynnyng of þe side of þe vmbre to þe touche of þe perpendicle. and þo are þe poyntes of þe vmbre. þat es to say þe schadowe. What poyntes ever yei be. wheþer of þe vmbre toward or froward. When any thyng es whose hight you wilt mesure by þe schadowe þereof and a ŷerde. þan rere even vp a ŷerde vpon þe playne grounde were þe ende of þe schadowe of þat thyng whilk you wille mesure, so rere it þat þe one parte of þame ŷerde falle vpon þat schadowe. and þe oþer part of þat ŷerde falle withouten. and mark þe place in þe ŷerde where þe schadowe begynnes to touche it. and by þe quantite of the ŷerde whilk es bitwene þe touche of þe schadowe in þe ŷerde and þe playne. multeply þe quantite of al þe schadowe whilk es bitwene þe lower party of þe thyng to be mesured and þe toppe of þe schadowe in þe playne. and depart þan al þat by þe quantite of þe schadowe whilk es bitwene þe toppe of þe schadowe and þe ŷerde. and þe nonmbre þat þan comes es þe heght of þat thyng. Also if you wilt mesure þe heght of a thyng by þe schadowe in ilk houre of þe day. take a ŷerde of two fote longe or thre. and on a playne rayse it even vp. and



þan mesure þe schadowe of it. þan mesure þe schadowe of þat thyng to be mesuride. and multiply þat by þe length of þe zerde. and þan departe al þat by þe schadowe of þe zerde and þat nonmbre howe ofte it be es þe heght of þat thyng. If you wilt have þe heght of any thyng wantyng grounde. as if you be in an house and wolde wite howe ferre were any thyng beyng in þe rofe. Take a table and rayse it vp a litel fro þe erthe. so þat you may se þat ilk thyng bitwene þe erthe and þat table. þan take a reulure and continu it to þe table. þat es to say side to side. and þan se by al þe reulure þe thyng to be mesurede. and þan drawe a lyne in þe table by þe reulure. este do þe same in anoþer site. þat es to say place of þe table. and make anoþer lyne. þan mesure þe heght whilk es bitwene þe hyhere parte of þe table and þe erthe. and þat mesure sale be callede þe heght kept. þan set þe table on þe erthe and take tuo thredes and put þat one in þat one lyne. and þat oþer threde in þat oþer lyne. þan make a mark þere as þise tuo thredes metes. þan mesure þe length bitwene þe mark and þe table. and set þereto þe heght kept. and þan hast ou þe heght of þat thyng. If you wilt mesure þe heght of any thyng withouten quadrant and withouten schadowe. rayse evene vp a rodde on a playne ageyne þat thyng and go toward it and froward it til þi sight beme passe by þe heght of þe zerde

and of þat thyng. þan loke<sup>1</sup> howe mikil es bitwene þi fote and þe grounde of þat þyng in þe tyme of beholdyng. and to þat length set þe space fro þethen to þe erthe. þan multiply al þat by þe length of þe Ʒerde. and þan departe al þat by þe space bitwene ye and þe Ʒerde and þere-with þe quantite fro þethen to þe erthe. and þat es þe heght. Also when you wilt mesure þe heght of any thing by two Ʒerds, even corneldly joyned, take a Ʒerde even to þe length of þi stature. and anoþer Ʒerde, tuo so longe als þat in þe myddel of þe lengere Ʒerde, set þe schortere even corneldely þan þis instrument þus made layde by þe playne ground til by þe toppes of bothe þe Ʒerdes you se þe toppe of the þyng to be mesured, þan make þere a mark and set þereto þi stature. and þan set þe marke þere. and so heigh es þat thyng howe mekil length es bitwene þe grounde of þat thyng and þe latter mark. bot forgete nocht þat perpendicle or equipendy, þat es to say, even hangere lolle by þe toppe of þe longer rodde to schewe when þin instrument es even vpright, and when it bagges. Ensample, þe stature of þe matere be called AB, þe Ʒerde doubling it CD þe Ʒerde evene corneldly joyned to it AE, and the foundement of þe þyng F, þan I say þe height of the þyng es BF, with þe quantite of BC. When you standes by a walle of a castelle or toure, and you wolde mesure þe heght of it with outen defaute, make

<sup>1</sup> MS. loloke.

a quadrat or quarterd. þat es to say a table even foure square of wode or brasse of what quantite you wilt, and ay þe more it be. þe better it es. and loke it be over alle square. in þe manner of ABCD and put a chippe of what length you wilt in þe cornelle B and anoþer in þe cornelle C and þe þird in þe cornel D and loke þei be fast on þat quadrat þat evenly þei stande raysed vp. and þe side of þe quadrat bitwene A and B mote be persede reulefully. in whilk persyng put a chippe like þe oþer thre. bot it sale be moveable fro A to B and þis chippe sale hight E and wite you that A es þe right cornel vpward. B þe left cornel vpward. C þe left cornel donward. D þe right cornel donward. When þe face of þe quadrat es torned toward ye. and þese chippes I calle eighen as in þe quadrant, þan loke even vp by C and B chippis or eighne to þe heyest of þe toure. So þat þe quadrat joyne to þe walle. and þat highest of þe toure sale hight F loke þe side AB be departed on 30 or 40 or howe fele you wilt. and in þe same manere departe þe side AD. þan move þe chippe E hedire and þedire til you se þe hiest F ageyne thurgh chippes D, E nocht chaunging þe raþer place BC þan biholde where þe chippe E stondes bitwene A and B and loke howe mekil þat part es EA to AD and so mekil part es DC to CBF and howe ofte EA es in AB so ofte es CD in CBF forþi multiply DA in AB and þat comes þereof departe by AE and þat nonmbre howe ofte it be es þe heght of CBF and



þat you have al the heght fro F to þe erthe. measure þe length AC to þe erth. whilk length set to þe heght CBF and þat comes is þe verey heght. If you wilt measure þe heght of any thyng by a myrure. lay þe myrure in þe playne grounde, and go toward and froward til you se þe toppe of þat thing in þe mydel of þat myrure. þan multiply þe playne bitwene þe fundament of þat thyng to be measured and þe myrure by þe space fro þethen to þe erthe. and þat comes þereof departe by þe space bytwene þi fote and þe myroure and þe nonmbre howe ofte it be es þe heght of þat thyng. Also als fro þethen to þe erthe has it to þe space bytwene þi fote and þe myrure so þe heght of þat thyng has it to þe playne. Whilk es bitwene þe rote of þat thyng to be measured and þe myrure and so ageyne.

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*Nowe we have taght to measure the heght of a thyng whilk es the first parte of oure tretis. We wil teche to measure the playne. for that es the seconde parte.*

When you wilt measure þe length of any playne with þe quadrant stonde in one ende of þe playne and byholde þat oþer by bothe holes. and holde þe cone. þat es to say þe cornelle of þe quadrant nere þin eigh. and þe compas toward þe playne to be measured. þan when you sees þe oþer ende of þat playne take þe nonmbre of þe poyntes of þe vmbre froward whilk þe perpendicle kyttes. þan multeply



þe distaunce. þat es to say þe space fro þethen to þe erthe by 12 and departe þat comes þereof by þe nonmbre of þe vmbre of þe poyntes froward raþer had. and þe nonmbre howe ofte it be es þe quantite of þe length of þat playne. Parcas þe playne whose length you wolde mesure es noght evene nor even distondyng to þin orisont. þat es to say to þe ende of þin sight. bot þat playne es lift vp and croked. þan biholde þe crokidnes þereof by þe holynge. þat es to say þe eyghne of þe quadrant. whilk þus you schalt do. set vpright tuo gerdes of one length in þe endes of þe playne to be mesurede. þan biholde þe toppes of þise thynges by bothe þe eyghne of þe quadrant. þan loke howe fele poyntes þe perpendicle kyttis. and þat of þe vmbre froward. if parcas þe perpendicle falle vpon þe poyntes of þe vmbre toward. þan torne þem into þe poyntes of þe vmbre froward. þan kepe þise poyntes. Est se þe ende of þat playne by bothe þe eyghen of þe quadrant. and loke howe fele poyntes of þe vmbre froward þe perpendicle kyttis. þan set þese poyntes to þe poyntes raþer kept. if you stonde in a lowere place aftere þan you did bifore. and if you stonde in an heighere. þan take away þe poyntes raþer kept. þan do with þise poyntes as you did with þe poyntes in þe next Chaptere bifore in mesuryng of an evene playne. þat es to say multeply þe distaunce fro þethen to þe erthe by 12 and depart þat comes þereof by þe poyntes of þe vmbre froward. and þe nonmbre howe ofte it be es þe

quantite of þe length of þat playne. When you wilt mesure þe playne of lande or water withouten þe quadrant. take þan tuo zerges and rayse þat one even vp right on þe playne. and calle þe playne BE and þe zerge vp raysed AB in whilk zerge set evene corneldly anoþer zerge even distonding to þe playne and þis zerge sale hight CD þan beside þe zerge vp raised AB set þin eigh and biholde þe ende of þe playne to be mesurede. and mark by whilk place of þat oþer zerge CD þi sight bem passes. and calle þat poynte E þan by þe quantite of þe seconde zerge CD multeply þe first zerge AB and departe þat comes þereof by þe quantite of AC and þan comes þe length of þe playne. When you wilt wite whilk es þe brede of a ryvere. kast a table vpon þe grounde nere þe ryvere. þan biholde þe ende of þat oþer side þe ryver by a reulure vpon þe table. And drawe a lyne by þe reulure on þe table. Est se þe forsaide ende by þe same reulure in an oþer place of þe table. and þere make anoþer line. þan go in a playne place and lay a threde on þat one lyne. and anoþer threde on þat oþer lyne and continu þem even til þei come to gidere. and howe mykel distaunce þat es to say space es fro þe metyng of þe thredes to þe table so brode es þe ryvere. When you wilt mesure þe brede of a ryvere by a quadrat, make þi quadrat ABCD as it es saide bifore of mesuryng of heght by þe quadrant. þan set þe quadrat beside þe ryvere and loke by CB þe ende on þat oþer side þe ryvere. and calle þat

ende F and B es þe ende on þis side þe ryvere. þan go fro B poynte by an evene lyne with þis quadrat. and þat þe reulure of þat lyne be octogonyely. þat es to say even corneldly bytwene B and F til yu se est þe ende F by þe poyntes or chippes D, B in þe quadrat. and calle G þe mark in þe place of þe seconde site. þat es to say stondynge þan howe mekil length es bitwene B and G so mekil as þe brede bytwene B and F. Also when you stondes by a ryvere and wille mesure þe brede of it. put þis quadrat vpon þe erche nere þe ryvere. and biholde by þe lyne CB þe ende on þat oþer side þe ryvere whilk es called F. þan move E hedire and þidere til you se þe same ende F by DE noght changyng þe first place of BC. þan biholde where E stondes bitwene A and B þan multiply DA into AB and departe þat comes þereof by AE and þe nonmbre þat comes howe oft it be es þe brede of þe ryvere whilk es BF. When you wilt mesure a playne by a mesure. þan rayse vp right on þe playne a rod of þe length fro þin eigh to þe erche. and calle þat rod AB. on þat rod hange a litel myrure. and ay þe lesse þe better. and þe place on þe rod where þe myroure hanges calle C and þe playne to be mesurede sale hight AD. þan stonde you vpon þo playne bitwene þe myrure and þe ende of þe length of þe playne. and loke in þe myrure movyng toward and froward þe myrure til you se þe ende of þe playne in þe mydille of the myrure. þat place of þe playne where you stondes



you sale calle it E. þan multiply þe length<sup>3</sup> of þi stondynge fro þe gerde by þe quantite bytwene þe myrure and þe playne. and departe þat comes þereof by þe distaunce of þe myrure fro þe hyere parte of þe rod. and þat nonmbre howe ofte it be es þe length of þat playne. as þus. multiply AE in AC and depart þat comes þereof by þe lyne CB. and þe nonmbre þat comes þereof es þe length of þe playne.

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*Nowe we have taght to mesure the playnes of ilk erthly thyng whilk es the secunde parte of this tretyse. So we teche to mesure the depnes. for that es the thrid parte and laste of this boke.*

When you wille mesure þe depnes of a welle. loke fro þat one side of þe welle to þe ende of þat oþer syde in þe bothome of þe same welle with þe quadrant. and holde þe cornel of þe quadrant nere þine eigh. and þe circumferens toward þe welle and take hede what es þe nonmbre of þe poyntes of þe vmbre toward vpon whilk þe perpendicle falles. þan mesure þe diameter of þe pit or welle. þat es to say þe mouthes brede. and multiply þat by 12 and depart þat comes þereof by þe nonmbre of þe forsaide poyntes and howe ofte þat nonmbre be. it es þe depnes of þat pitte. Also for þe same. rayse vp a table on þe mouthe of þe welle. þan put vpon þe table a reulure whereby biholde you þe ende on þe bothome þereof. þan make þer a lyne by þat reulure. est put þe reulure in anoþer place



of þe table. and þan se by þat reulure þe forsaide ende. and þere make anoþer lyne by þe reulure in þat table. þan lay þe table vpon þe playne grounde. and lay on þise tuo lynes tuo thredes even til þei mete. þan mesure þe distaunce bitwene þe metyng of þo thredes and þe table. and so depe es þe welle. Also for þe same. rayse even vp on þe mouthe of þe well swilk a quadrat as we spak of bifore. þan by CB loke þe ende in þe bothome of þe welle. and þat sale hight F. þan move E toward and froward til by DE you se est F noght chaungynge þe first place BC. þan biholde where E stondes bytwene AB. þan multiply DA in AB and departe þat comes þereof by AE. and þat nonmbre howe oft it be es þe depnes of þe welle. whilk es BF.

*Nowe oure tretis of geometri es thus endid.*



## CARMEN DE ALGORISMO.

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HÆC algorismus ars præsens dicitur;<sup>2</sup> in qua  
Talibus Indorum<sup>3</sup> fruimur bis quinque figuris.

0. 9. 8. 7. 6. 5. 4. 3. 2. 1.

Primaque significat unum: duo vero secunda:  
Tertia significat tria: sic procede sinistra  
Donec ad extremam venias, quæ cifra vocatur;  
Quæ nil significat; dat significare sequenti.  
Quælibet illarum si primo limite ponas,  
Simpliciter se significat: si vero secundo,

<sup>2</sup> "Hæc præsens ars dicitur algorismus ab Algore rege ejus inventore, vel dicitur ab *algos* quod est ars, et *rodos* quod est numerus; quæ est ars numerorum vel numerandi, ad quam artem bene sciendum inveniebantur apud Indos bis quinque (id est decem) figuræ." *Comment. Thomæ de Novo-Mercatu.* MS. Bib. Reg. Mus. Brit. 12 E. 1.

<sup>3</sup> "Hæc necessariae figuræ sunt Indorum characteros." *MS. de numeratione.* Bib. Sloan. Mus. Brit. 513, fol. 58. "Cum vidissem Yndos constituisse *ix* literas in universo numero suo propter dispositionem suam quam posuerunt, volui patefacere de opere quod sit per eas aliquidque esset levius discentibus, si Deus voluerit. Si autem Indi hoc voluerunt et intentio illorum nihil novem literis fuit, causa quæ mihi potuit. Deus direxit me ad hoc. Si vero alia dicam præter eam quam ego exposui, hoc fecerunt per hoc quod ego exposui, eadem tam certissime et absque ulla dubitatione poterit inveniri. Levitasque patebit aspicientibus et discentibus." MS. Bibl. Publ. Cant. 1869, li. vi. 5.

Se decies : sursum procedas multiplicando.  
 Post prædicta scias breviter quod tres numerorum  
 Distinctæ species sunt; nam quidam digiti sunt;  
 Articuli quidam; quidam quoque compositi sunt.  
 Sunt digiti numeri qui semper infra decem sunt;  
 Articuli decupli digitorum; compositi sunt  
 Illi qui constant ex articulis digitisque.  
 Ergo, proposito numero tibi scribere, primo  
 Respicias quis sit numerus; quia si digitus sit,  
 Una figura satis sibi; sed si compositus sit,  
 Primo scribe loco digitum post articulum; atque  
 Si sit articulus, in primo limite cifram,  
 Articulum vero tu in limite scribe sequenti.  
 Quolibet in numero, si par sit prima figura,  
 Par erit et totum, quicquid sibi continuatur;  
 Impar si fuerit, totum sibi fiet et impar.  
 Septem<sup>4</sup> sunt partes, non plures, istius artis;  
 Addere, subtrahere, duplareque dimidiare;  
 Sextaque dividere est, sed quinta est multiplicare;  
 Radicem extrahere pars septima dicitur esse.  
 Subtrahis aut addis a dextris vel mediabis;  
 A leva dupla, divide, multiplicaque;

<sup>4</sup> En argorisme devon prendre  
 Vii especes . . . .  
 Adision subtracion  
 Doubloison mediacion  
 Monteploie et division  
 Et de radix enstracion  
 A chez vii especes savoir  
 Doit chascun en memoire avoir  
 Letres qui figures sont dites  
 Et qui excellens sont ecrites.



Extrahe radicem semper sub parte sinistra.<sup>5</sup>  
Addere si numero numerum vis, ordine tali  
Incipe; scribe duas primo series numerorum  
Primam sub prima recte ponendo figuram,  
Et sic de reliquis facias, si sint ibi plures.  
Inde duas adde primas hac conditione:  
Si digitus crescat ex additione primorum,  
Primo scribe loco digitum, quicumque sit ille;  
Sed si compositus, in limite scribe sequenti  
Articulum, primo digitum; quia sic jubet ordo.  
Articulus si sit, in primo limite cifram,  
Articulum vero reliquis inscribe figuris;  
Et per se scribas si nulla figura sequatur.  
Si tibi cifra superveniens occurrerit, illam  
Dele suppositam; post illic scribe figuram:  
Postea procedas reliquas addendo figuras.  
A numero numerum si sit tibi demere cura,  
Scribe figurarum series, ut in additione;  
Majori numero numerum suppone minorem,  
Sive pari numero supponatus numerus par.  
Postea si possis a prima demere primam,  
Scribas quod remanet, cifram si nil remanebit.  
Sed si non possis a prima demere primam;  
Procedens, unum de limite deme sequenti;  
Quod demptum pro denario reputabis ab illo,  
Subtrahe totalem numerum quem proposuisti.  
Quo facto, scribe super quicquid remanebit,  
Facque nonenarios de cifris, cum remeabis,  
Occurrant si forte cifrae, dum demeris unum;  
Postea procedas reliquas demendo figuras.

<sup>5</sup> Vide p. 11.

An subtractio sit bene facta probare valebis,  
 Quas subtraxisti primas addendo figuras.  
 Nam, subtractio si bene sit, primas retinebis,  
 Et subtractio facta tibi probat additionem.  
 Si vis duplare numerum, sic incipe ; solam  
 Scribe figurarum seriem, quamcumque voles tu ;  
 Postea procedas primam duplando figuram ;  
 Inde quod existit, scribas, ubi jusserit ordo,  
 Juxta præcepta quæ dantur in additione.  
 Nam si sit digitus, in primo limite scribe ;  
 Articulus si sit, in primo limite cifram,  
 Articulum vero reliquis inscribe figuris ;  
 Vel per se scribas, si nulla figura sequatur :  
 Compositus si sit, in limite scribe sequenti  
 Articulum, primo digitum ; quia sic jubet ordo :  
 Et sic de reliquis facias, si sint ibi plures.  
 Incipe sic, si vis aliquem numerum mediare :  
 Scribe figurarum seriem solam, velut ante ;  
 Postea procedas medians, et prima figura  
 Si par aut impar videas ; quia si fuerit par,  
 Dimidiabis eam, scribens quicquid remanebit ;  
 Impar si fuerit, unum demas mediare,  
 Quod non præsumas, sed quod superest mediabis ;  
 Inde supertactum, fac demptum quod notat unum ;  
 Si monos, dele ; sit ibi cifra post nota supra.  
 Postea procedas hac conditione secunda :  
 Impar<sup>6</sup> si fuerit, hinc unum deme priori,  
 Inscribens quinque, nam denos significabit  
 Monos prædictam : si vero secunda sit una,  
 Illa deleta, scribatur cifra ; priori

<sup>6</sup> *i. e.* figura secundo loco posita.

Tradendo quinque pro denario mediato ;  
Nec cifra scribatur, nisi deinde figura sequatur :  
Postea procedas reliquas mediando figuras,  
Ut supra docui, si sint tibi mille figuræ.  
Si mediatio sit bene facta probare valebis,  
Duplando numerum quem primo dimidiasti.  
Si tu per numerum numerum vis multiplicare,  
Scribe duas, quascunque velis, series numerorum ;  
Ordo tum servetur, ut ultima multiplicandi  
Ponatur super anteriorem multiplicantis ;  
A leva reliquæ sunt scriptæ multiplicantis.  
In digitum cures digitum si ducere, major  
Per quantum distat a denis respice, debes  
Namque suo decuplo tocies delere minorem ;  
Sicque tibi numerus veniens exinde patebit.  
Postea procedas postremam multiplicando,  
Recte multiplicans per cunctas inferiores,  
Conditione tamen tali ; quod multiplicantem  
Scribas in capite, quicquid processerit inde ;  
Sed postquam fuerit hæc multiplicata, figuræ  
Anteriores seriei multiplicantis ;  
Et sic multiplica, velut istam multiplicasti,  
Quæ sequitur numerum scriptum quibusque figuris.  
Sed cum multiplicas, primo sic est operandum,  
Si dabit articulum tibi multiplicatio solum ;  
Proposita cifra, summam transferre memento.  
Sin autem digitus excreverit articulusve,  
Articulus supraposito digito salit ultra ;  
Si digitus autem, ponas ipsum super ipsam,  
Subdita multiplicans hanc quæ super incidit illi  
Delebit penitus, et scribens quod venit inde ;



Sed cum multiplicat aliam positam super ipsam,  
Adjunges numerum quem probet ductus earum ;  
Si supraposita cifra debet multiplicare,  
Prorsus eam delet, scribi quod loco cifra debet,  
Sed cifra multiplicans aliam posita super ipsam,  
Sitque locus supra vacuis super hanc cifra fiet ;  
Si supra fuerit cifra semper pretereunda est ;  
Si dubites, an sit bene multiplicatio facta,  
Divide totalem numerum per multiplicantem,  
Et reddet numerum emergens inde priorem.  
Si vis dividere numerum, sic incipe primo ;  
Scribe duas, quascunque velis, series numerorum ;  
Majori numero numerum suppose minorem,  
Nam docet ut major teneat bis terve minorem ;  
Et sub supprima supprimam pone figuram,  
Sic reliquis reliquas a dextra parte locabis ;  
Postea de prima primam sub parte sinistra  
Subtrahe, si possis, quociens potes adminus illud,  
Scribens quod remanet sub tali conditione ;  
Ut toties demas demendas a remanente,  
Quæ serie recte ponuntur in inferiori,  
Unica si, tum sit ibi decet hac operari ;  
Sed si non possis a prima demere primam,  
Procedas, et eam numero suppose sequenti ;  
Hanc uno retrahendo gradu comites retrahantur,  
Et, quoties poteris, ab eadem deme priorem,  
Ut toties demas demendas a remanente,  
Nec plusquam novies aliquem tibi demere debes,  
Nascitur huic numerus quociens supraque sequentem  
Hunc primo scribas, retrahens exinde figuras,  
Dum fuerit major suppositus inferiori,



Et rursus fiat divisio more priori ;  
Et numerum quotiens supra scribas pereunti,  
Si fiat saltus retrahendo cifra locetur,  
Et pereat numero quotiens, proponas eidem  
Cifram in numerum pereat vis, dum locus illic  
Restat, et expletus divisio non valet ultra :  
Dum fuerit numerus minor inferiore seorsum  
Illum servabis ; hunc multiplicando probabis,  
Si bene fuisti, divisor multiplicetur  
Per numerum quotiens ; cum multiplicaveris, adde  
Totali summæ, quod servatum fuit ante,  
Redditurque tibi numerus quem proposuisti ;  
Et si nil remanet, hunc multiplicatio reddet.  
Cum ducis numerum per se, qui pervenit inde  
Sit tibi quadratus, ductus radix erit ejus,  
Nec numeros omnes quadratos dicere debes,  
Est autem omnis numerus radix alicujus.  
Cum voles numeri radicem quærere, scribi  
Debet ; deinde notes si sit locus ultimus impar,  
Estque figura loco talis scribenda sub illo,  
Quæ, per se ducta, numerum tibi destruit illum,  
Vel quantum poteris ex huic delebis eadem ;  
Et retrahendo duplex retrahens duplando sub illa  
Quæ primo sequitur, duplicatur per duplcatam,  
Post per se minuens sub ea saliendo.  
Post his propones digitum, qui, more priori  
Per precedentes post per se multiplicatus,  
Destruit in quantum poterit numerum remanentem,  
Et sic procedas retrahens duplando figuram,  
Reponendo novam donec totum peragatur,  
Subdupla propriis servare docetque duplatis ;

Si det compositum numerum duplacio, debet  
Inscribi digitus a dextra parte propinqua,  
Articulusque loco quo non cedebat duplicando ;  
Si dabit articulum, sit cifra loco pereunte  
Articulusque locum tenet unum, duplanda recessit ;  
Si donet digitum, sub prima pone sequente,  
Si supraposita fuerit duplicata figura  
Major proponi debet tantum modo cifra,  
Has retrahens solito propones more figurarum,  
Usque sub extrema ita fac retrahendo figuras,  
Si totum debes numerum quem proposuisti,  
Quadratus fuerit de dupla quem duplicasti,  
Sicque tibi radix illius certa patebit,  
Si de duplatis sit juncta supprima figura ;  
Si radicem per se multiplices habeasque  
Propositum primo, bene te fuisse probasti ;  
Non est quadratus, si quis restat, sed habentur  
Radix quadrati qui stat major sub eodem ;  
Vel quicquid remanet tabula servare memento ;  
Hoc casu radix per se quoque multiplicetur,  
Et sic quadratus sub primo major habetur,  
Huic addas remanens, et prius debes habere ;  
Si locus extremus fuerit par, scribe figuram  
Sub pereunte loco per quam debes operari,  
Quæ quantum poterit supprimas destruat ambas,  
Vel penitus legem teneas operando priorem,  
Si suppositum digitus in fine repertus,  
Omnino delet illic scribi cifra debet,  
A leva si qua sit ei sociata figura ;  
Si cifrae remanent in fine pares decet harum  
Radices, numero mediam propone partem,

Tali quesita radix patebit arte reperta.  
 Per numerum recte si nosti multiplicare  
 Ejus quadratum, numerus qui pervenit inde  
 Dicetur cubicus; primus erit radix ejus;  
 Nec numeros omnes cubicatos dicere debes,  
 Est autem omnis numerus radix alicujus;  
 Si cures cubici radicem quærere, primo  
 Inscriptum numerum distinguere per loca debes;  
 Quæ tibi mille notant a mille notante supprima  
 Junctum, summes operandi parte sinistra,  
 Illic et scribas digitum, qui multiplicatus  
 In semet cubicæ suprapositum sibi perdat,  
 Et si quid fuerit adjunctum parte sinistra  
 Si non omnino quantum poteris inveniando,  
 Hunc triplans retrahe saltem, faciendo sub illo  
 Quod manet a digito deleto; terna figura  
 Sibi propones quæ sub triplo asocietur,  
 Et cum subtriplo per eam tripla multiplicatur;  
 Hinc per eam solam productum multiplicabis,  
 Postea totalem numerum, qui pervenit inde  
 A suprapositis respectu tolle triplata  
 Addita supprimo cubicæ tunc multiplicetur,  
 Respectu cujus, numerus qui progredietur  
 Ex cubito ductu suprapositis adimetur;  
 Tunc ipsam dele triples saltum faciendo,  
 Semper sub terna, retrahens alias triplicatas  
 Ex hinc triplatis aliam propone figuram,  
 Quæ per triplatas ducatur more priori;  
 Primo sub triplis sibi junctis, postea per se,  
 In numerum ducta, productum de triplicatis:  
 Utque prius dixi numerus qui prevenit inde



A suprapositis has respiciendo trahatur,  
 Huic cubicæ junctum supprimo multiplicabis,  
 Respectuque sui, removebis de remanente,  
 Et sic procedas retrahendo triplando figuras.  
 Et proponendo nonam, donec totum peragatur,  
 Subtripla sub propriis servare decet triplicatis ;  
 Si nil in fine remanet, numerus datus ante  
 Est cubicus; cubicam radicem sub tripla probent,  
 Cum digito juncto quem sub primo posuisti,  
 Huic cubicæ ducta, numerum reddant tibi primum.  
 Si quid erit remanens non est cubicus, sed habetur  
 Major sub primo qui stat radix cubicati,  
 Servari debet quicquid radice remansit,  
 Extracto numero, decet hoc addi cubicato.  
 Quo facto, numerus reddi debet tibi primus.  
 Nam debes per se radicem multiplicare  
 Ex hinc in numerum duces, quod pervenit inde  
 Sub primo cubicus major sic invenietur ;  
 Illi jungatur remanens, et primus habetur,  
 Si per triplatum numerum nequeas operari ;  
 Cifram propones, nil vero per hanc operari  
 Sed retrahens illam cum saltu deinde triplatum,  
 Propones illi digitum sub lege priori,  
 Cumque cifram retrahes saliendo, non triplicabis,  
 Namque nihil cifræ triplacio dicitur esse ;  
 Aut tu cum cifram pertraxeris autem triplicatam,  
 Huic cum subtriplo semper servare memento :  
 Si det compositum, digiti triplacio debet  
 Illius inscribi, digitus saliendo super ipsam ;  
 Quæ manet a digito deleta, terna figura ;  
 Articulus jungitur cum triplata pereunte,



Sed facit hunc scribi per se triplacio prima,  
Quæ si det digitum per se facit scribi illum ;  
Consumpto numero, si solæ fuit tibi cifræ  
Triplatae, propone cifram saltum faciendo,  
Cumque cifram retrahe triplata, scribendo figuram,  
Propones cifræ, sic procedens operare,  
Si tres vel duo series sint, pone sub una,  
A dextris digitum servando prius documentum.

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PREFATIO  
DANIELIS DE MERLAI

AD LIBRUM

DE NATURIS SUPERIORUM ET INFERIORUM.

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*Bib. Arundel. Mus. Brit. 377.*

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*Philosophia magistri Danielis de Merlai ad  
Johannem Norwicensem episcopum.*

Cum dudum ab Anglia me causa studii ex-  
cepissem et Parisius aliquandiu moram fecissem,  
videbam quosdam bestiales in scholiis gravi auc-  
toritate sedes occupare, habentes coram se scamna  
duo vel tria et descriptos codices importabiles  
aureis literis Ulpiani traditiones representantes:  
necnon et tenentes stilos plumbeos in manibus,  
cum quibus asteriscos et obelos in libris suis  
quadam reverentia depingebant: qui dum propter  
inscientiam suam locum statue tenerent, tamen  
volebant sola taciturnitate videri sapientes: sed  
tales cum aliquid dicere conabantur infantissimos  
ripperiebam. Cum hoc, inquam, in hunc modum  
se habere Deprehenderem, ne et ego simile dam-  
num incurrerem, artes que scripturas illuminant

non in transitu salutandas vel sub compendio pretereundas mecum sollicita deliberatione tractabam. Sed quoniam doctrina Arabum, que in quadrivio fere tota existit, maxime his diebus apud Toletum celebratur, illuc ut sapientiores mundi philosophos audirem, festinantur properavi. Vocatus vero tandem ab amicis et invitatus ut ab Hyspania redirem, cum pretiosa multitudine librorum in Angliam veni. Cumque nunciatum esset mihi quod in partibus illis discipline liberales silentium haberent, et pro Ticio et Seio penitus Aristotiles et Plato oblivioni darentur, vehementer indolui, et tamen ne ego solus inter Romanos Græcus remanerem, ubi hujusmodi studium florere didiceram, iter arripui. Sed in ipso itinere obviam honorem Dominum meum et principem spirituales Johannem Norwicensem episcopum qui me honorifice ut eum decebat recipiens; valde meo congratulabatur adventui.

# PROPOSALS

FOR SOME

## INVENTIONS IN THE MECHANICAL ARTS.

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*MS. Lansd. 101.*

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### *A Note of sundry sorts of Engynes. 1583.*

1. First a cariedge with his properties to carry or drawe fyve hundreth weight with one mans strength.
2. An ingen of wonderfull strength to pull downe parcullices or irone gatts.
3. A chaine of yron non licke it in strength of his bidgnes.
4. A paire of gripes to the same chaing belonging of strange fashone.
5. A gine to hoyste or pull vp earth to make rampiors.
6. A scaffold to be removed.
7. A device to remove any burden of 10 tonne weight without horse or beast.
8. An ingen to lanch shippes.
9. A float to pase men over waters.



10. A bridg to be carried for passing an army of men ordenaunce and such licke carriges over any ryvers, &c.

11. A myll to grine by water winde or men for forte castell or towne of warr.

12. A crane to hoyst vp 10 or 20 tonne weight.

13. A gynne to hoyst vp any cannon and laie him in his carriage by one man onley.

14. An ingen for clensing or taking away of any shelves or shallow places in the river of Tems or any such river the same device maie serve for clensing of diches about citties or towns pondes or any such licke standing waters.

15. A water myll to rune longer then before tyme.

16. A winde myll and not to turne the howse about.

17. To make water workes for fountains cunditts and suche licke.

18. To make pipes of lead 6 or 7 foot long without sauder.

19. To make a boat to goe fast one the water without ower or saile.<sup>7</sup>

<sup>7</sup> This was a favourite project about this time. In a few "speciall breife remembrances" of some "pleasante serviceable and rare inventions as I have by longe studie and chargeable practice founde out," addressed to Queen Elizabeth by Ralphe Rabbard, I find one headed "The rarest engyne that ever was invented for sea service;" and this is described as follows:—"A vessell in manner of a Tally or Talliote to passe upon the seas and ryvers without oars or sayle against wynde and tyde, swifter than any that ever hath bynne seene, of wonderfull

20. To preserve a boat from drowning and the people that be therein.

effect bothe for intelligence and many other admirable employtes almost beyonde the expectation of man :” MS. Lansd. 121. Now see Bourne’s *Inventions or Devises*, a book deserving the particular attention of all those who are interested in the history of mechanical inventions. Edmund Jentill, in 1594, proposed a “device wonderfull strange,” similar to the above : it was one of the inventions which he offered to discover to Lord Burghley, on his release from prison, for counterfeiting foreign coin :—MS. Lansd. 77 and 113.

# THE PREFACE

TO

## A CALENDAR OR ALMANAC

FOR THE YEAR 1430.

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*MS. Harl. 937.*

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My soverayne maistres. certen evydens have done me to vnderstonde your abylyte to lerne scyens partyculere, and als wele consyder I your desyre in specyal to lerne a certen conclusyons of þe new kalender. I say a certen conclusyons for þys cawse for sum of þaim profoundly to be expressyd or lerned for defawte of termes convenyent in ower moder langage beyn to stronge to a tendyr wytte to comprehende þat is not elevate be processe and cowrse of scoles. þerefor als myche as þe grete phylosophyr sayth he wrappyth hym in hys frende þat condescendyth to þe ryghtfull prayer of hys frende . . . . me and mor mevyth me syth I . . . . bondene to make satisfactyon to your desire prayng ever dyscrete persone þat þis redyth or heryth to have my rude endytyng excusyd and

my superfluyte of wordes for two causes. þe furste cause for so curyos and harde sentens in obscure termes is full tedyos to syth a tender wytte to cousayne. þe secunde cause is for sothely me semythe better to wryte and twyse teche one gode sentens þen ones forgotten. levyng þerfore all vayne preambles of superfluyte þat papyr fullyllygte with owtyn fruyte þis lesone I gyfe zow fyrste þat in zour zerus beyn xii moneth. January February March Aprile May June July Auguste Septembre Octobre Novembre Decembre. And ccc and sixty days and 5 and sex odde howres qwyche odde howres gedyrde togeder 4 zerus makeyth 24 howres þat is a day naturale so þat in þis zere þat is clepyt lyp zere beyng ccc and sixty and sex days. In everych zere we vse a new letter þat Sunday gothe by. In þe lyp zere we occupy twene þe furste servyth fro new zerus day to seynt mathye day. þe secunde tellyth us owre soneday þe remnande of þe zere.

zour pryme schal be to zow a special doctour of dyverse conclusyons querfore in latyn he is clepyt þe golden nownbur and begynnygt at one and rennyth to xix and turnyth azayn to one, and so in case þat one were pryme þis zere next zere schulde 2 be pryme and þe 3 zere 3. so rennyng zere be zere to xix and azayn to one and so abowte with owten ende. In þe fyrst table of zowre kalendere by þe reede letters in þe firste lyne joynded to þe blake letters in þe secunde lyne schal ze knowe þe lyp zere qwen it fallyth. In



þe 3 lyne beyn wryten primes frome one to xix and turnyth aȝayn. Seche þen ȝour prime of þe ȝere þat ȝe be in jonyd to þe domynycale letter of þe same ȝere and þen may ȝe se by þe rede letters in þe fyrst lyne qwenus it be lyp ȝere, or how nere ȝe be, þis ensample. I ȝyffe ȝow þe ȝere of owre lorde a.mccccxxx in qwyche ȝere þis kalendere to ȝow was wryten. Went prime by 6 and ȝowre letter domynycale was A qwyche beyn jonyd and wryten to geder in þe hede and þe begynnyng of þis sayd table. þen behalde how þe next ȝere folowyng schal 7 be prime and G domynycale. And þe next ȝere after schal 8 be prime and be lyp ȝere as ȝe may se by þe reede letter F jonyd to þe blak letter E so þat in þis lyp ȝere schal F be domynycale letter fro þe Circumscycyon þat is clepyd newȝerus day vnto seynt Mathye day. and þen schal E be ȝour sonday letter to þe ȝerus ynde as I sayd before. þis doctryne kepe þurghe alle þe forsayd table. Amonge þe blak letters in þe same lyne beyn wryten reede letters qwyche teches þe indyccyon þat is a terme ful necessary to þaim þat lyste know þe verray and certene date of þe Pope bulles and of þe olde Imperyale wrytynge of Rome. ȝyf it lyke ȝow to wytte in qwat Indyccyon ȝe be in Take ȝour prime and ȝour domynycale letter of þe same ȝere þat ȝe beyn in qwyche letter in case þat it be rede calle þat þe first Indyccyon and þe next letter þe secunde jndiccion and so rennyng vnto xv and ȝen aȝayn to one at þe

next reede letter. gif it be a blake letter þat gour prime fallyth one cownte fro þe next goyng beforus and so mony is þe jndiccyon þat ge seche forgete not þis lesone.

A table þat next folowygt is callyd þe table of þe 5 festes moveyabyll þat is to say qwen septuagesime commeygt in þat is þe sonday before lentyn qwen Allia is closyd vp. Also þis table tellygt qwen lentyn fallyth qwen Eysterday. qwen þe Rogacyons and qwen qwytesoneday. It techygt also how mony weykes be fro Crystemesday to lentyn how mony wekes and days fro qwytesonday to mydsommerday And how mony fro Whytesonday to þe advente on þis maner. Tak þe prime of þe gere þat ge be in. in þe fyrste lyne wryten with reede. and þe domynycal letter next folowyng in þe secunde lyne. and folowe stryght forthe in to þe lyne of þat thyng wryten in þe heyde þat ge desyre. and by þe nounbur þat ge fynde schalle ge know þat ge desyre. Vnderstonde wele þis ensample. Aftyr crystynmesse þe gere of owre lorde a.m.cccc.xxx. I was aferde of lentyn and lokyd in my kalender for septuagesime and lentyn how nere þai were and soghte my prime in þe fyrste lyne þat hap pynd to be 7 þe same tyme. and toke my domynycal letter þat was G next following. þo turnyd I forth fro þis G streight in to nexte lyne þat haythe Septuagesime writyn in þe hede and I fonde 28 þere wryten þereby demyd I þat septuagesime sonday schal falle ge 28 day

of þe moneyth of Januare wrytyn in þe hede. þo loked I forthermore in þe next lyne that hayth lentyn wryten in þe hede and þere I fonde 18 wryten and þereby I demyd þat first sonneday of lentyn schulde be on þe 18 day of þe moneyth of February nexte wrytyn above zyt I loked forthermore in þe next lyne for Esterday and fonde þere 1 wryten and þen wyste I þat Esterday schulde be on þe firste day of þe moneythe of Aprile wrytyn next above. and zow take ensample as I have do and loke ze kepe þe same thurghe alle þe table.

JOHANNIS NORFOLK  
IN ARTEM PROGRESSIONIS SUMMULA.

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MS. Harl. 3742.

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*In artem progressionis continue et discontinue  
secundum magistrum Johannem Norefolk incipit  
summula.*

Non inuenientes sed doctrinam tradita inde  
numerorum progressionem ab Algore rege quondam  
Castellie suo in Algorismo de integris perficere  
curantes. occultas aliorum tradiciones si que fu-  
erint penitus omittentes dummoda tales nostra  
assidua percunctacione non obstante re maxima  
nobis miranda ante nostram edicionem in nostras  
manus visuras nos nusquam recepisse fatemur  
testimonium tamen fide dignorum nostrorum ami-  
corum nobis possibilitatem operis concludebat eo  
quod tales regulas utilem artem progressionis  
concernentes ante nostra tempora fuisse editas  
testabantur. Oportunum igitur apud nos indi-  
cavimus cum ars tam preciosa arithmeticeque  
sciencie prefulgida margarita conspectibus ho-  
minum se non presentabat sed quorundam forte  
inpericia incarcerata atque porcis oblata sciolos



latebat circa possibilitatem operis novarumque regularum edicionem divino auxilio primitus invocato petitisque auctoritatibus et favoribus eorum quibus incumbit hujusmodi summulas corrigere operas exiles soleritur impendere et eas sic collectas nostro calamo rudique stilo descriptas. Primo ad honorem Dei beatissime virginis Marie et omnium suorum sanctorum ac ad profectum animarum omnium fidelium defunctorum quarum collegio Oxonie primus vicecustos exciteramus et ad ceteras hujusmodi scienciam diligentes plenius promulgare curavimus. Reverendam ergo tuam benevolenciam quiscunque es o carissime has nostras regulas exiles exiliterque collectas placito vultu bonoque animo ut acceptare digneris benigne rogamus. Est namque opus harum regularum omnium numerorum proportionalitate aliqua comperatorum sive plures paucioresve fuerunt ut in his exemplis. 1. 2. 4. 8. 16. 32. vel sic. 5. 6. 7. 8. vel sic. 4. 8. 12. 16. vel sic. 1. 2. 3. 4. 5. 6. et sic ad quantitatem unitatum sive percussionum horologii quas sonat horologium ad 12 horas vel ad quartem partem diei naturalis et similibus quid resultans fuerit levi arificio explicare. Fiat obsecramus legitimum kalendare ergo in anima tua o lector honorande hoc scriptum exiguum magna tamen solertia et industria compilatum nec desit tibi spes enarrandi quid ex predictis numeris resultat et omnibus consimilibus proportionalitate aliqua comperatis cum regule satis sufficienter

sunt tradite et nomen auctoris publice prefato est monstratum preambulo. Sic ergo karissime incipe et mente tua recollige tria documenta generalia que tractatus presentis processimi plenissime facilitabunt. Primum documentum est quod scias quid progressio sit et quod sectionem patitur in continuam et discontinuam prout posterius apercius clarescet. Secundum documentum est ut bene consideres quod omnium numerorum ordinate se in progressionem habentium aliqua proportionalitas reperta nec quid ex talibus artificiose poterit certificari propter infinite variabilitatis talem. Tercium est quod non deficiat tibi spes perveniendi in finem premissum per hanc artem facillimam cum de omnibus numeris proportionalitate geometrica ordinatis ac de quibusdam arithmetica proportionalitate magis famose reperibilibus dantur regule sequentes solum omittentes numeros inusitados arithmetica tamen proportionalitate constitutos ac omnes numeros musica proportionalitate collectos tum facilius sit enarrare qui ex talibus numeris resultat quam hujusmodi numeros artificiose reperire et componere et hec tria documenta nota diligentissime. Specificantes modo predicta tria documenta generalia dicamus primo quod progressio est numerorum diversorum ordinata collectio et dicitur ordinata pro tanto quod si aliqua collectione numerus minor sequatur majorem ut hic. 12 65. 413. ibi non est ratio progressio judicanda quamvis enim metaphorica progressio nuncupanda

est omnis numerorum collectio a minore incipiendo terminando in majorem numerum ipsa tamen proprie dicitur progressio cum numeri quadam proportionalitate colliguntur istud namque evidentissimum est cum apud omnes maxime indicatur progressionem naturalem esse incipiendo computare ab unitate ascendendo ad alios numeros naturali ordine succedentes et ibi aliqua proportionalitas inter terminos reperta est et que postea apparebit. Progressio sic proprie sumpta dividitur in continuam et discontinuam progressio continua est numerorum diversorum ordinata collectio nullo numero alium superexcrecente nisi sola unitate et ista potest indrunter contingere vel incipiendo ab unitate vel ultra unitatem ut sic. 1. 2. 3. 4. 5. vel sic. 3. 4. 5. 6. et cætera. Progressio vero discontinua est numerorum diversorum ordinata collectio uno alio supraexcrecente plusquam unitate servata tamen ut prius in progressionem continuam proportionalitate geometrica et hoc indrunter incipiendo ab unitate vel altro numero quocunque ut hic. 1. 4. 7. 10. 13. et cætera. vel sic. 5. 7. 9. 11. 13. 15. et cætera. Et quia progressio proprie dicta ut dictum est constat ex numeris geometrica proportionalitate covintis ne tractatus iste necessarii videatur deficere superfluisve habundare quorum utrumque collectoris impericie ascribendum esset videndum est de proportionalitate quid sit et ejus speciebus quæ etiam species ejus. ad hanc artem magis pertinet que vero abji-



cienda. Est namque proportionalitas duarum proportionum aut plurimum in simul comperatorum habitudo hujus autem tres sunt species scilicet geometrica arithmetica arismonica sive musica proportionalitas geometrica est quando sunt tres termini aut plures et equales est excessus secundi ad primum sicut tertii ad secundum et quarti ad tertium et cætera si tanti fuerint ut hic. 1. 2. 3. 4. 5. 6. vel sic. 2. 4. 6. 8. vel sic. 2. 7. 12. 17. 22. et cætera. Proportionalitas vero arithmetica est quando sunt tres termini vel plures et equalis est proportio inter primum et secundum et secundum ad tertium et tertium ad quartum ut hic. 1. 2. 4. 8. 16. vel sic. 1. 3. 9. 27. et cætera. Sed proporcionalitas musica sive arsmonica est quando sunt tres termini insimul proporcionalitati et equalis est proportio tertium ad primum sicut est proportio excessus tertii ad secundum ad excessum secundi ad primum ut hic. 3. 4. 6. vel sic. 6. 8. 12. vel sic. 12. 16. 24. hiis sic brevissime recitatis per nos dicamus quod in omnibus numeris proporcionalitate geometrica proporcionalitatis hec ars habet locum sive plures fuerint sic pauciores etiam in numeris famosioribus arithmetica proporcionalitate comperatis ut in numeris proporcionalitate duplica collectis omittentes alias species ejusdem proporcionalitatis sicut omittimus omnes species arsmonica proporcionalitate integritas ob id quod superius docetur documento tertio. Hiis sic specificatis inducamus primam



regulam primo de numero geometrica proportionalitate adunatis et ubi progressio continua est que hec est. Numero locorum secundum progressionem continuam exeunte sub numero pari per minus medium multiplicetur numerus locorum et habetur quod queritur hæc namque regula generalis est ut ostendent exempla posita in prima tabula in fine tractatus hujus et quamvis hæc regula viris maturis aliquantulum arithmetice sciencie noticia inbutis satis lucida est ut tamen juvenes et minus provecti per eam sapiant sic eam delucidamus ut ejus aliarumque regularum recitandarum noticie perfectus habeantur primo notanda sunt quid nominis horum quinque terminorum scilicet numerus locorum vel loca numerorum numerus par numerus impar majus medium minus medium eiis quinque terris nostro more declaratis facillime perquiritur sensus regule precedentis ac cujusque quatuor regularum sequentium. Sic vero incipientes dicamus quod non probabile aliquem pro eadem morula sive eodem . . . . plures numeros recitare et sic numerum primo recitatum dicimus esse in primo loco et secundo recitatum numerum dicimus esse in secundo loco et sic de aliis quibuscumque recitandis conformiter sicut si numeri diversi scribi debeant oportet quod variis locis scribantur et de eiis idem indicare quoad loca quare citissime cognoscitur numerus locorum secundum numerationem numerorum enumeratorum. De secundo et tercio terminis in simul licet annotare quia

cognito quid sit numerus par tanquam suum privatam cognoscitur numerus impar qui aliam cognitionem non habet quam per suum positivum ut docet aristolus. Est autem numerus par ut notat Boycius in sua arithmetica et est sua prima definitio illius quilibet numerus qui potest in duo equalia nullo medio intercedente dividi ab hac namque condicione deficit numerus impar ut constat quia quamvis quinaris dividi potest in duos binarios etiam in duo equalia tamen aliqua unitas integrans quinarium intercidit cum duo et tria faciunt quinque. Ceterum restat declarare quid minus medium quidve majus medium sit promissum ut impleatur pro quorum noticia est primo animadvertendum quid sit medium. Est namque medium quod equaliter distat ab extremis et sicut facillime ymaginatur medium ubi loca numerorum numerantur numero impari ut hic 1. 2. 3. 4. 5. 3. est medium vel sic ubi loca numerorum numerantur a numero pari saltem ultra binarium inveniendi sunt duo tales numeri quorum minor numerus minus medium dicitur et major numerus majus medium nuncupatur ut hic. 2. 3. 4. 5. numerus locorum est quatuor minus medium. 3. majus medium. 4. aut sic. 5. 8. 11. 14. 4. est numerus locorum ut prius minus medium est. 8. majus medium est. 11. hiis sic cognitis evidens est prima regula prius recitata de progressionem continua et sequitur secunda regula de progressionem continua eadem facilitate que hec est. Numero locorum secundum pro-

gressionem continuam existente sub numero impari per medium multiplicetur numerus locorum et habetur quod queritur sine aliqua subtractione vel additione et hec regula certissima est perfectus a nobis jam duabus regulis ad progressionem continuam pertinentibus succedunt. 3. regule spectantes ad progressionem discontinuam et quia in tali progressionem minor erat difficultas nobis certitudinem regularum uti-  
 pium invenire ut tamen posteri nostri eas regulas citissime cognoscant quas nostris magnis laboribus a diu percuntavimus licet ipse aliquibus obscuris terminis a nobis primo dentur declarationibus tamen nostris levissime conceptis quilibet mediocri ingenii capacitate fultus ipsas poterit facillime experiri et est prima regula talis. In progressionem discontinua numero locorum exeunte sub numero pari et si eorum numerorum excessus nominatus fuerit a numero impari per majus medium intelligibile inter numeros mediales multiplicetur numerus locorum et subtrahatur medietas numeri locorum et habetur quod queritur hanc autem regulam assumpto hoc exemplo. 5. 10. 15. 20. sic delucidamus nam in exemplo dato numerorum loca esse sub numero pari nullius ambigit et unumquemque numerum excedere suum numerum in medietate precedentem per 5. 3. qui est numerus imper nulli dubium est tunc constat quod inter duos numeros mediales qui sunt 10. et 15. quatuor numeros ordine naturali intelligi posse videlicet 11. 12. 13. 14.



eorumque numerorum subintellectorum majus medium esse 13 hic vero numerus 13. multiplicandus est per numerum locorum scilicet 4. et subtrahatur 2. qui est medietas numeri locorum et patet summa ideo vero dicitur 13. medium intelligibile quia non expresse inter numeros exemplo positos invenitur sed quadam solertia per intellectus indagacionem experitur ac etiam quod majus medium sit consimiliter indicatur. Hiis sic declaratis sequitur secunda regula que hec est. Si progressionem discontinua numerus locorum fuerit par eorumque numerorum excessu exeunte sub numero pari per medium intelligibilem inter numeros mediales multiplicetur numerus locorum et habetur summa quesita hanc autem regulam duobus exemplis declaramus sic primum exemplum. 2. 4. 6. 8. in quo exemplo medium intelligibile est 5. qui ductus in numerum locorum exurgunt 20 ut evidet qui est summa totalis. Exemplum secundum prefate regule in quo exemplo numerus excessus est 4. medium vero intelligibilem 11. cum inter duos numeros mediales scilicet 9. et 13. ordine naturali intercipiuntur hii tres numeri scilicet 10. 11. 12. aut intelligi possunt quorum medium est 11. ut dictum est per quod multiplicetur numerus locorum et habetur numerus ex omnibus resultans. Ultima regula secundum genus proportionalitatis geometricae et habita in ordine est hec progressionem discontinua numero locorum ex-



eunte sub numero impari per medium multiplicetur numerus locorum et habetur quod queritur exemplum 6. 8. 10. per 8. multiplicetur numerus locorum qui est tertia et exurgunt. 24. Et quia prius promissum est regulas fieri de quibusdam numeris arithmetica proportionalitate comparatis hanc solam regulam disposuimus pro numeris magis famosis et sunt illi numeri qui proportione dupla inter se comperantur ut hic 1. 2. 4. 8. 16. 32. et cetera et est regula talis. Si plures numeri proportionalitate arithmetica comperati ubi posterior suum immediate priorem proportione dupla excedit insimul comperentur dupletur ultimus et a resultante subtrahatur primus et habetur quod queritur evidet hec regula in exemplo posito nam dupatur 32. resultant 64. a quibus subtrahatur unitas que est primus numerus et resultant 63. et hec regula generalis est in omnibus talibus sive ab unitate incipiatur sive non sive vero loca numerorum paria fuerint sive non de aliis autem numeris secundum hoc genus proportionalitatis dicimus nunc ut dictum est prius documento tertio. *et sic perfectus est iste tractatus brevissimus in collegio animarum Oxonie anno domini millesimo quadringentesimo quadragesimo quinto quod Norfolk scriptor ac compiler hujus tractatus.*

*Explicit.*

Nil amplius restat ad perfeccionem hujus summe colligere et scribere quam quod antedictum

est sed solum regulas prescriptas ad facilitatem prospicere volencium recolligere cum tabulis exemplarium ac consulere quod lectores ejusdem perfecte sint in arte multiplicationis per intellectum ideo sequitur tabula subscripta et deo gratias.

*Prima regula.*

Numero locorum secundum progressionem continuam exeunte sub numero pari per minus medium multiplicetur numerus locorum et addatur medietas numeri locorum et habetur quod queritur.

*Exemplum prime regule.*

1 . 2 . 3 . 4 . 5 . 6 . 7 . 8 . 9 . 10 . 11 . 12.

Vel sic { 2 . 3 . 4 . 5 . 6 . 7 . vel sic 6 . 7 . 8 . 9 . 10 . 11 .  
3 . 4 . 5 . 6 . 7 . 8 . vel sic 19 . 20 . 21 . 22 .

*Secunda regula.*

Numero locorum secundum progressionem continuam exeunte sub numero impari per medium multiplicetur numerus locorum et habetur quod queritur sine aliqua subtractione vel additione.

*Exemplum secunde regule.*

1 . 2 . 3 . 4 . 5 . vel sic 5 . 6 . 7 . 8 . 9 . 10 . 11 .

vel sic 12 . 13 . 14 . 15 . 16 .

vel sic 21 . 22 . 23 . 24 . 25 . 26 . 27 .

*Tercia regula.*

In progressionē discontinua numero locorum exeunte sub numero pari et si eorum numerorum excessus nominatus fuerit a numero impari per majus medium intelligibilem inter numeros mediales multiplicetur numerus locorum et subtrahatur medietas numeri locorum et habetur quod queritur.

*Exemplum tercie regule.*

. 5 . 10 . 15 . 20 . 25 . 30 . vel sic 2 . 5 . 8 . 11.  
 vel sic 3 . 10 . 17 . 24 . 31 . 38.  
 vel sic 3 . 6 . 9 . 12.

*Quarta regula.*

Numerus locorum si progressionē discontinua fuerit par eorumque numerorum excessu exeunte sub numero pari per medium intelligibilem inter numeros mediales multiplicetur numerus locorum et habetur quod queritur.

*Exemplum quarte regule.*

5 . 9 . 13 . 17. vel sic 3 . 5 . 7 . 9.  
 vel sic 2 . 4 . 6 . 8 . 10 . 12. vel sic 3 . 7 . 11 . 15.

*Quinta regula.*

Numero locorum secundum progressionem discontinuam exeunte sub numero impari per medium multiplicetur numerus locorum et habetur quod queritur.

*Exemplum quinte regule.*

4 . 6 . 8. vel sic 3 . 5 . 7 . 9 . 11 . 13 . 15.  
 vel sic 12 . 14 . 16. vel sic 3 . 7 . 11 . 15 . 19 . 23 . 27.

*Sexta regula sed est de numeris arithmetica proportionalitate collectis.*

Si plures numeri ubi posterior suum immediate precedentem proportionem dupla excedat insimul comparentur dupletur ultimus et a resultante subtrahitur primus et habetur quod queritur.

*Exemplum sexte regule.*

12 . 4 . 8 . 16 . 32. vel sic 2 . 4 . 8 . 16.

*Explicit tabula exemplarium summule super progressionem continua et discontinua secundum Norefolk.*



## APPENDIX.

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### I.

*A few Observations on the Numerical Contractions found in some manuscripts of the Treatise on Geometry by Boetius.*

THE remarks which follow have not, as far as I am aware, found a place in any prior publication: I intend them to form an appendix to the interesting chapter on the same subject presented to the literary world by M. Chasles.

I could not have connected the following pages in the form of a continuous history, without introducing much that is already known; I have, therefore, considered it advisable to place my notes under distinct articles, without any attempt at arrangement.

1. It is very probable that the well-known passage on the *Abacus*, in the first book of the Geometry of Boetius, is an interpolation. For in a MS. once belonging to Mr. Ames, no such passage appears; and in another, now in the library of Trinity College, it is also wanting: again, no such contractions occur in any copy of the Treatise on

Arithmetic\* by the same author; although, in the library† just mentioned, there is a list of them, on a fly-leaf to a MS. of that work, in a hand-writing of the fourteenth century, which is thus headed:

Primus igin; andras; ormis; quarto subit arbas;

Quinque quinas; termas; zenis; temenias; celentis.

and over these names the contractions are written, as well as Roman numerals explaining them.

2. There are two MSS. in the Bodleian Library which merit particular attention. One, MS. Hatton. 112, possesses two distinct treatises on arithmetic on this system: the first is very extensive, but anonymous; the rubrication to the preface of the other is as follows: *Incipit prefatio libri Abaci quæ junior Berhelinus edidit Parisiis, Domino suo Amulio.* In both these treatises, as well as in the other MS., local position is clearly pointed out.

3. Vossius‡ attributes them to a Grecian origin; Huet§ derives them from the Hebrew; and the Bodleian MSS. refer them to Syria and Chaldea. It is scarcely necessary to observe, that there is no connection between these numerals and those among the contractions of Tyro and Seneca.

4. M. Chasles has confused the sipos and celentis, the latter of which was seldom used as a cipher. In the second Bodleian MS. we read, *inscribitur et in ultimo figura 0, sipos nomine. Que licet numerum nullum significet: tum ad alia quædam utilis est.* In the

\* Most of the MSS. of this work that I have examined are very old,—generally prior to the thirteenth century. Only one MS. that I am acquainted with (Bib. Burn. 275.) contains Arabic numerals. It may also be remarked here, that a treatise on arithmetic in verse, by one Leopald (Bib. Arund. 339.) possesses numerals whose forms are, as far as I know, unique. But this tract will receive its due attention in a proper place.

† R. xv. 16. There are also a few pages on arithmetic, which contain the following account of its rise among the ancients: *Hanc igitur artem numerandi apud Grecos Samius Pitagoras et Aristoteles scripserunt, diffusiusque Nicomachus et Euclides; licet et alii in eadem floreunt, ut Erastosthenes et Crisippus. Apud Latinos primus Apuleius, deinde Boecius.*

‡ Observations ad Pomponiam Melam. 4to. Hag. Com. 1658, p. 64.

§ Demonstratio Evangelica. Prop. iv. p. 173. E.

Lansdown collection (842) in the British Museum, is a very beautiful MS. of the whole works of Boetius: what renders it more interesting in the present inquiry, is the contraction for the sipos without the drawing of an abacus, which curiously illustrates the difficulty of the transition from numerical operations, by means of that instrument, to local position without distinguishing boundaries.

5. The Metz MS. in the Arundel collection, referred to by Mr. Hallam, is probably an abridgment of one or more extensive treatises on the subject: the author says, *quicquid ab abacistis excerpere potui compendiose collegi, componens inde mihi certas regulas, que volentibus ad hanc disciplinam attingere non inutiles.* He quotes Boetius.

6. The following verses occur in a MS.\* of the fourteenth century on arithmetic:

Unus adest igin; andras duo; tres reor armin;  
 Quatuor est arbas; et per quinque fore quinas;  
 Sex calcis; septem zenis; octo zenienias;  
 Novem celentis; per deno sume priorem.

And a list of the contractions is given on the preceding page of the same volume.

7. The fractional notation appears to be as curious as the integral, but the contractions are not quite so arbitrary, and a regular system is evidently followed up throughout. It is for the most part merely an adapta-

\* Bib. Trin. Coll. Cant. inter MSS. Gal. O. 2. 45. f. 33b. Chasles has given verses to the same import, but he does not mention the source whence he has obtained them. There is every reason to think that the sipos was a later improvement, and the Metz MS. contains no allusion to it. Mr. Barnwell, of the British Museum, informs me, that a short tract on celentis was once pointed out to him in a MS. volume belonging to that establishment, but no reference to it being in any of the catalogues, I have not been fortunate enough to find it.

tion of the Roman weights to numerical computation ; for instance, taking as for unity, we have—

$\frac{1}{1\frac{1}{2}}$ deunx	$\frac{1}{1\frac{0}{2}}$ dextans
$\frac{9}{1\frac{1}{2}}$ dodrans	$\frac{8}{1\frac{1}{2}}$ bisse
$\frac{7}{1\frac{1}{2}}$ septunx	$\frac{6}{1\frac{1}{2}}$ semis
$\frac{5}{1\frac{1}{2}}$ quicunx	$\frac{4}{1\frac{1}{2}}$ triens
$\frac{3}{1\frac{1}{2}}$ quadrans	$\frac{2}{1\frac{1}{2}}$ sextans
$\frac{1}{1\frac{1}{2}}$ uncia	

The *uncia* was also divided into twelve portions, but differently—

$\frac{1}{2}$ semiuncia	$\frac{1}{3}$ duella
$\frac{1}{4}$ sicilius	$\frac{1}{6}$ sexcula
$\frac{1}{8}$ dragma	$\frac{1}{12}$ hemissecla
$\frac{1}{18}$ tremissis	$\frac{1}{24}$ scrupulus
$\frac{1}{48}$ obulus	$\frac{1}{72}$ bissiliqua
$\frac{1}{96}$ ceraces	$\frac{1}{144}$ siliqua

To these was added the  $\frac{1}{192}$ <sup>th</sup> part of the *uncia*: *ut usque ad minimum extremum diatessaron et diapente symphoniarum tonorum semitonorumque intervallis distinclarum, harum fractionum denominatio conscenderet vel contenderet.* Zambertus gives the contractions, *quæ sepiissime in antiquis libris.\** In the Metz MS. the contraction for the *as* is omitted. Several examples of reckoning *time* by this method occur in the classical writings, especially in Pliny,† as also in some MSS. of the eleventh and twelfth centuries in the British Museum. Bede wrote a tract on this fractional notation, and he adds, *hæc ponderum vocabula, vel characteres non modo ad pecuniam mensurandam, verum ad quævis corpora, sive tempora dimetienda, conveniunt.* A MS. in the Public Library (Kk. v. 32) contains an explanation in

\* Euclidis Elementa ex Campano a Zamberto, fol. Par. 1516, p. 248.

† Archæologia, vol. xxvi. p. 159. Vid. Bedæ Opera. Edit. Bas. 1563, t. i., col. 101, 141, et 182. MS. Arund. Mus. Brit. 25, f. 124, et 356, f. 45.



Saxon, which very much coincides with that given by Bede, and would appear to be taken from it.

It would be impossible, with the few materials yet brought to light, to conjecture with any great probability how far these Boetian contractions may have influenced the introduction, or co-operated with the Arabic system to the formation, of our present numerical notation. It appears to me highly probable that the two systems became united, because the middle age forms of the figure five coincide with the Boetian mark for the same numeral, and those of two others are very similar. The idea of local position, again, may have had an independent European origin; the inconveniences of the abacus on paper would have suggested it by destroying the distinguishing boundaries, and inventing an arbitrary hieroglyphic for the representation of an empty square.

## II.

## NOTES ON EARLY ALMANACS.\*

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THE following short paper has been compiled from notes collected at various times, and without any intention of placing a dissertation on the subject before the public. I mention this merely to suggest to the reader that no connected history of almanacs has been attempted, and that it will be unfair to view what is here placed before him as any other than an attempt to abridge the labour of a successor who might wish, at some future period, to dive more deeply into the subject.

The early history of almanacs is involved in much obscurity. The Egyptians, indeed, possessed instruments answering most of the same purposes: but the log calendars are the most ancient almanacs, properly so called. Verstegan† derives their name from a Saxon origin, viz. *al-mon-aght*, or the observation of all the moons, that being the purpose for which they were originally made: an eastern origin would appear to me to be more probable. They are doubtless of high antiquity, and, if we can be guided by the errors of the more modern ones in their\*

\* This has been printed in the "Companion to the British Almanac" for 1839; to the kindness of Mr. Knight, the publisher of that useful periodical, I am indebted for power to reprint it here.

† Restitution of decayed intelligence, p. 64.

ecclesiastical computation, we might refer them to the second or third century.\* Gruter has delineated one at Rome, and which is said to have been used by the Goths and Vandals: this was cut in elm, though most are in box, and some few in fir, brass, horn, &c. Each of these calendars contains four sides, for the four quarters of the year, and gives the golden numbers, epacts, dominical letter, &c. The numerical notation is imperfect but curious; dots are put for the first four digits, a mark similar to the Roman numeral V, for five; this mark, and additional dots for the next four, and the algebraical sign + for ten. Specimens of these logs may be seen in the British Museum†; and, as they are not uncommon, it is unnecessary to enter into further detail.

Before I commence with written almanacs, it will be necessary to remark the distinction between astronomical and ecclesiastical calendars, the first of which contain astronomical computations, and the other lists of saints' days, and other matters relative to the church; sometimes, indeed, both are found united, although the latter claim a higher antiquity, being prefixed to most ancient Latin manuscripts of the Scriptures.

The folding calendars were, perhaps, the most ancient forms of them, and merit particular attention. Several of these are in the British Museum,‡ and at Oxford; one of them was written in the year 1430, and is in English; but the writer confesses his inability to find suitable expressions

\* MS. Harl., Mus. Brit., 5958.

† MSS. Harl., 197, 198. The last of these is a modern one used in Derbyshire or Staffordshire, and cut, probably, in the latter part of the 17th century: the other one is much earlier, though perhaps not of very high antiquity. Others may be seen in the Ashmolean Museum, and in St. John's College, Cambridge. I refer to Dr. Plott's History of Staffordshire for a very good description of them. (See also Brady's *Clavis Calendaria*.)

‡ Cotton Rolls, viii. 26; MSS. Harl. 937, 3812, 5311; MSS. Sloan. 996, 2250; which last is the calendar of John Somers, afterwards mentioned. There is also one in the Ashmolean collection at Oxford in singularly fine preservation.

for the technical terms which were derived for the most part from Arabic, *for defawte of terms convenyent in our moder langage*. In the Pepysian library at Cambridge there is one printed by Wynkin de Worde, in octo-decimo, which, in its original form, folds up from a small folio sheet of vellum; it bears the date of 1523.\*

The standard almanacs emanated from Oxford, the seat of British science throughout the middle ages: in fact, before Newton's time, Cambridge was a blank, and the only scientific names that cheer the pages of the history of its early literature are Holbroke of St. Peter's College, Buckley of King's, and Dee of St. John's: the first known by his astronomical tables, the second by a plagiarism of a method of extracting the roots of fractions from Robert Record, and the third a memorable instance of one of the greatest men of his time uniting the pure truths of science with the grossest absurdities. All three were astrologers, † owing, perhaps, more to the place of their education than to the individuals themselves.

There has been some dispute relative to the authenticity of Roger Bacon's calendar, of which there is a MS. in the British Museum: the following is an exact transcript of the commencement:—

“ Kalendarium sequens extractum est a tabulis tholetanis . anno domini . 1292 . factus ad meridiem civitatis tholeti que in Hispania scita est cujus meridianus non multum distat a meridiano medii puncti Hibernie in quo . 3 . continentur.” f. 2.

If we retain *factus*, it cannot be translated, but, fortunately, the other MS. at Oxford has *factum*, and this must evidently be the true reading. Professor Peacock

\* Hartshorne's 'Book Rarities of Cambridge.'

† Holbroke is admitted by all to have been an astrologer. Buckley wrote a treatise which involves the principles (MS. Bib. Reg. 12 A. xxv.); and with respect to Dr. Dee, no doubt can arise.



writes *factis*, but there is not, as far as I know, any MS. authority for it. With respect to the author of it, the Bodleian MS., in a coeval rubric, states the calendar to have been written *à fratre Rogero Bacon*; while the Cotton MS., not having any original title, is ascribed to Roger Bacon, in a hand of the 17th century: both of the MSS. belong to the 14th century. In the Harleian collection (No. 941) is a MS. on the length of the days throughout the year, stated to have been *made at Oxynforde be the new kalendere and proved in all the univarsity*: this *new kalendere* may possibly refer to Roger Bacon's; but there are not sufficient data to enable us to attain an approach to certainty.

The calendar of John Somers, of Oxford, written in 1380, was one of the most popular of the time: there is generally appended to it, *Tabula docens algorismum legere, cujus utilitas est in brevi satis spatio numerum magnum comprehendere. Et quia numeri in kalendario positi vix excedunt sexaginta, ultra illam summam non est protensa*.\* Several English translations of this tract are among the Ashmolean MSS.

We have likewise in MS. *Almanach Profacii Judei*, which is very ancient. Walter de Elvendene wrote a calendar in 1327,† and Nicholas de Lynna published another in 1386.‡ Sometimes these calendars are found in rolls.

In the library at Lambeth Palace is a very curious calendar in the English language, written in 1460; at the end is a table of eclipses from 1460 to 1481; but a very perfect volvelle is most worthy of notice, because those instruments are generally found imperfect. In the Cottonian collection is another English calendar, written about

\* MS. Bib. Cott. Mus. Brit. Vespas. E. vii. f. 4.

† MS. Sloan. Mus. Brit. 286.

‡ MS. Ashm. Oxon. 5.

1450, but so much damaged by the fire that the nature of it cannot be seen. In Trinity College, Cambridge, there is a MS., said to have been composed in 1347, and entitled, *An Almanak, translated in perpetuite, out of Arabike into Latin*; and in the same library I find *The Effermerides of John of Mounte Riol*, a German Prince of *Astronomyers*. Professor Leslie mentions a very beautiful calendar in the library of the university of Edinburgh, with the date of 1482: he does not appear to be aware that they were common in MS. libraries, and he greatly overrates its value.

There was printed at Hackney, in 1812, a small octavo volume, containing an account of an English almanac for the year 1386: it contains a very large portion of astronomical and medical matter, but appears to be of little interest, save that it is the earliest one in English I have ever heard of. The contents of this calendar are as follow:—

1. The houses of the planets and their properties.
2. The exposition of the signs.
3. Chronicle of events from the birth of Cain.

In 1325 there was a *grete hungur* in England; in 1333 a great tempest; in 1349 the first, in 1361 the second, and in 1369 the third pestilence. It is curious to remark the clumsy method of expressing numbers consisting of more than two figures: for instance, we have 52mcc20 put for 52,220. This shows that the Arabic notation was even then but imperfectly understood among the common people.

4. To find the prime numbers.
5. Short notes on medicine.
6. On blood-letting.
7. A description of the table of the signs, and moveable feasts.
8. *Quantitates diei artificialis*.

The extracts from this calendar are wretchedly transcribed, and evidently by one who was totally unacquainted with MSS.

The clock or albion of Richard de Walingford, of St. Alban's, answered the purpose of a calendar.\* This clock made, says Bale, who appears to have seen it, *magno labore, majore sumptu, arte vero maxima*, was considered the greatest curiosity of its time. In his account of it, which still remains in manuscript, we have the following definitions:—*Albion est geometricum instrumentum: almanac autem arimetricum*. Peter Lightfoot's celebrated astronomical clock at Glastonbury may have been something of the same sort.

Peter de Dacia, about 1300, published a calendar, of which there is a very early MS. in the Savilian library at Oxford: the *condiciones planetarum* are thus stated—

Jupiter atque Venus boni, Saturnusque malignus;  
Sol et Mercurius cum Luna sunt mediocres.

The *homo signorum*, so common in later calendars, probably originated with him.

The earliest almanac printed in England was the *Sheapeheard's Kalender*, translated from the French, and printed by Richard Pynson, in 1497. It contains a vast portion of extraneous matter. The following verses on the planets will, at the same time, give a good idea of the nature

\* In one almanac of the commencement of the 17th century (MS. Harl. 5937. Bagford Collect., s. 139) is a very singular method for finding the hour of the day, if in the country and without any watch. I refer to it merely out of charity to those right-hearted enthusiastic antiquaries who do not *stick at trifles* in pursuing researches that can in any way illustrate the customs of our ancestors in the *good old times*. To those who only value the researches of antiquaries in proportion as they are likely to furnish some evident tangible utility, I would willingly spare their time in recurring to a method which, though it might excite their ridicule, could never, from its nature, be brought into practice in the present age.

of the astrological information in this and other calendars of the period :—

“ Some hot, some colde, some moyst, some dry,  
 If three be good, foure be worse at the most.  
 Saturne is hiest and coldest, being full old,  
 And Mars, with his bluddy swerde, ever ready to kyll ;  
 Jupiter very good, and Venus maketh lovers glad,  
 Sol and Luna is half good and half ill,  
 Mercury is good and will verily  
 And hereafter shalt thou know ;  
 Whiche of the seven most worthy be,  
 And who reigneth hie, and who a lowe ;  
 Of every planets propertie,  
 Which is the best among them all,  
 That causeth welth, sorrowe, or sinne,  
 Tarry and heare sone thou shalt,  
 Speake softe, for now I beginne.”

Afterwards follow some prognostications of the weather. The following method *to knowe what wether shall be all the yere after the chaunge of every moone by the prime dayes*, is taken from a MS. in Lambeth Palace :—

“ Sondaye pryme, drye wether.  
 Mondaye pryme, moyst wether.  
 Teusdaye pryme, cold and wynde.  
 Wenesdaye pryme, mervelous.  
 Thursdaye pryme, sonne and clere.  
 Frydaye pryme, fayre and fowle.  
 Saturdaye pryme, rayne.”

Prognostications of the weather were early matters of reproach—

“ Astronomyers also aren at ere whittes ende,  
 Of that was calculed of the clymat the contrye thei fyndeth.

And in Heber's library was a little tract of three leaves, entitled 'A Mery Prognostication'—

“ For the yere of Chryste's incarnacyon,  
 A thousande fyve hundreth fortye and foure.  
 This to prognosticate I may be bolde,  
 That whan the new yere is come, gone is the olde.”



Henry VIII. issued a proclamation against such false prognostications as this tract was intended to ridicule, but still no printer ventured to put his name to it. Not long after to believe them was a crime; "as for astrologically and other like vaine predictions or abodes," says Thomas Lydiat, "I thanke God I was never addicted to them."\*

Johannes de Monte-Regio, in 1472, composed the earliest European almanac that issued from the press; and, before the end of that century, they became common on the Continent. In England they were not in general use until the middle of the sixteenth century. Most of the best mathematicians of the time were employed in constructing them; but, before the end of the following century, almanac-makers began to form a distinct body, and, though they often styled themselves "studentes in the artes mathematicall," very few of them were at all celebrated in the pure sciences.

It may not be wholly irrelevant here to make some few observations on the memory-rhymes found in some almanacs of the present day, and which date their origin to a much earlier period. The well-known lines, used by many for recalling to their recollection the number of days in each month, I find in Winter's Cambridge Almanac for 1635, under the following slightly-varied form—

" Aprill, June, and September,  
 Thirty daies have as November;  
 Ech month else doth never vary  
 From thirty-one, save February;  
 Wich twenty-eight doth still confine,  
 Save on Leap-year, then twenty-nine."

And the nursery-rhymes, commencing " Multiplication is my vexation," were certainly made before 1570.†

\* MS. Bodl. 662.

† Professor Davies's Key to Hutton's Mathematics, p. 17.

The early history of ecclesiastical computation is intimately connected with that of calendars. Dionysius Exiguus was one of the first who wrote on the subject: after him, Bede, Gerlandus, Alexander de Villa Dei, and Johannes de Sacro-Bosco, were the most celebrated. The *Massa Compoti* of Alexander de Villa Dei, so common in MS., is perhaps the most singular tract on the subject that has come down to us: his reason for the title of the book is exceedingly curious:—*Sicut de multis laminis æris in conflatorio massa una efficitur, ideo librum istum vocari volui massam compoti.*

I cannot conclude without mentioning the ‘*Almanac and Prognostication*’ of Leonard Digges, which was so often reprinted in the latter half of the sixteenth century: it is filled with the most extravagant astrological absurdities, and a table of weather predictions. With respect to the latter, however, I have had the curiosity to test its accuracy for some months in comparison with our two celebrated weather almanacs, and, on the average, have found it to be quite as “*neare the marke*” as either of them.

THE END.

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