Section 8 Machine Elements

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8-2 MACHINE ELEMENTS

8.1 MECHANISM by Heard K. Baumeister, Amended by Staff

REFERENCES: Beggs, ''Mechanism,'' McGraw-Hill. Hrones and Nelson, ''Analysis of the Four Bag Linkage,'' Wiley. Jones, ''Ingenious Mechanisms for Designers and Inventors,'' 4 vols., Industrial Press. Moliam, ''The Design of Cam Mechanisms and Linkages,'' Elsevier. Chironis, ''Gear Design and Application,'' McGraw-Hill.

NOTE: The reader is referred to the current and near-past professional literature for extensive material on linkage mechanisms. The vast number of combinations thereof has led to the development of computer software programs to aid in the design of specific linkages.

Definition A **mechanism** is that part of a machine which contains two or more pieces so arranged that the motion of one compels the motion of the others, all in a fashion prescribed by the nature of the combination.

LINKAGES

Links may be of any form so long as they do not interfere with the desired motion. The simplest form is four bars *A, B, C,* and *D*, fastened together at their ends by cylindrical pins, and which are all movable in parallel planes. If the links are of different lengths and each is fixed in

turn, there will be four possible combinations; but as two of these are similar there will be produced three mechanisms having distinctly different motions. Thus, in Fig. 8.1.1, if *D* is fixed *A* can rotate and *C* oscillate, giving the **beam-and-crank** mechanism, as used on side-wheel steamers. If *B* is fixed, the same motion will result; if *A* is fixed (Fig. 8.1.2), links *B* and *D* can rotate, giving the **drag-link** mechanism used to

Fig. 8.1.3 Rocker mechanism.

feather the floats on paddle wheels. Fixing link *C* (Fig. 8.1.3), *D* and *B* can only oscillate, and a **rocker** mechanism sometimes used in straight-line motions is produced. It is customary to call a rotating link a **crank;** an oscillating link a **lever,** or beam; and the connecting link a **connecting rod,** or **coupler**. Discrete points on the coupler, crank, or lever can be pressed into service to provide a desired motion. The fixed link is often enlarged and used as the supporting frame.

If in the linkage (Fig. 8.1.1) the pin joint F is replaced by a slotted piece E (Fig. 8.1.4), no change will be produced in the resulting motion, and if the length of links *C* and *D* is made infinite, the slotted piece *E* will become straight and the motion of the slide will be that of pure translation, thus obtaining the engine, or **sliding-block, linkage** (Fig. 8.1.5).

If in the sliding-block linkage (Fig. 8.1.5) the long link *B* is fixed

(Fig. 8.1.6), *A* will rotate and *E* will oscillate and the infinite links *C* and *D* may be indicated as shown. This gives the **swinging-block linkage.** When used as a quick-return motion the slotted piece and slide are usually interchanged (Fig. 8.1.7) which in no way changes the resulting motion. If the short link *A* is fixed (Fig. 8.1.8), *B* and *E* can both rotate,

Figs. 8.1.4 and 8.1.5 Sliding-block linkage.

and the mechanism known as the **turning-block linkage** is obtained. This is better known under the name of the **Whitworth quick-return motion,** and is generally constructed as i[n Fig. 8.1.9](#page-3-0). The **ratio of time of advance to time of return** *H*/*K* of the two quick-return motions (Figs. 8.1.7 and

8.1.9) may be found by locating, in the case of the swinging block (Fig. 8.1.7), the two tangent points (*t*) and measuring the angles *H* and *K* made by the two positions of the crank *A*. If *H* and *K* are known, the axis of *E* may be located by laying off the angles *H* and *K* on the crank circle

Fig. 8.1.8 Turning-block linkage.

and drawing the tangents *E*, their intersection giving the desired point. For the turning-block linkage [\(Fig. 8.1.9](#page-3-0)), determine the angles *H* and *K* made by the crank *B* when *E* is in the horizontal position; or, if the angles are known, the axis of *E* may be determined by drawing a hori-

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zontal line through the two crankpin positions (*S*) for the given angle, and the point where a line through the axis of *B* cuts *E* perpendicularly will be the axis of *E*.

Velocities of any two or more points on a link must fulfill the follow-

Fig. 8.1.9 Whitworth quick-return motion.

ing conditions (see Sec. 3). (1) Components along the link must be equal and in the same direction (Fig. 8.1.10): $V_a = V_b = V_c$. (2) Perpendiculars to V_A , V_B , V_C from the points *A*, *B*, *C* must intersect at a common point *d*, the **instant center** (or instantaneous axis). (3) The velocities of points *A, B,* and *C* are directly proportional to their distances from this center (Fig. 8.1.11): $V_A/a = V_B/b = V_C/c$. For a straight link the tips of

the vectors representing the velocities of any number of points on the link will be on a straight line (Fig. 8.1.12); $abc = a$ straight line. To find the velocity of any point when the velocity and direction of any two other points are known, condition 2 may be used, or a combination of conditions 1 and 3. The **linear velocity ratio** of any two points on a

linkage may be found by determining the distances *e* and *f* to the instant center (Fig. 8.1.13); then $V_c/V_b = e/f$. This may often be simplified by noting that a line drawn parallel to *e* and cutting *B* forms two similar triangles *efB* and *sAy*, which gives $V_c/V_b = e/f = s/A$. The **angular velocity ratio** for any position of two oscillating or rotating links *A* and *C* [\(Fig. 8.1.1\)](#page-2-0), connected by a movable link *B*, may be determined by

scaling the length of the perpendiculars *M* and *N* from the axes of rotation to the centerline of the movable link. The angular velocity ratio is inversely proportional to these perpendiculars, or $O_C/O_A = M/N$. This method may be applied directly to a linkage having a sliding pair if the two infinite links are redrawn perpendicular to the sliding pair, as indicated in Fig. 8.1.14. *M* and *N* are shown also in [Figs. 8.1.1,](#page-2-0) 8.1.2, 8.1.3, 8.1.5, 8.1.6, 8.1.8. I[n Fig. 8.1.5](#page-2-0) one of the axes is at infinity; therefore, *N* is infinite, or the slide has pure translation.

Fig. 8.1.14

Forces A mechanism must deliver as much work as it receives, neglecting friction; therefore, the force at any point *F* multiplied by the velocity V_F in the direction of the force at that point must equal the force at some other point P multiplied by the velocity V_P at that point; or the forces are inversely as their velocities and $F/P = V_P/V_F$. It is at times more convenient to equate the moments of the forces acting around each axis of rotation (sometimes using the instant center) to determine the force acting at some other point. In Fig. 8.1.15, $F \times a \times c/(b \times d) = P$.

CAMS

Cam Diagram A cam is usually a plate or cylinder which communicates motion to a follower as dictated by the geometry of its edge or of a groove cut in its surface. In the practical design of cams, the follower (1) must assume a definite series of positions while the driver occupies a corresponding series of positions or (2) must arrive at a definite location by the time the driver arrives at a particular position. The former design may be severely limited in speed because the interrelationship between the follower and cam positions may yield a follower displacement vs. time function that involves large values for the successive time derivatives, indicating large accelerations and forces, with concomitant large impacts and accompanying noise. The second design centers about finding that particular interrelationship between the follower and cam positions that results in the minimum forces and impacts so that the speed may be made quite large. In either case, the desired interrelationship must be put into hardware as discussed below. In the case of highspeed machines, small irregularities in the cam surface or geometry may be severely detrimental.

A stepwise displacement in time for the follower running on a cam driven at constant speed is, of course, impossible because the follower would require infinite velocities. A step in velocity for the follower would result in infinite accelerations; these in turn would bring into being forces that approach infinite magnitudes which would tend to destroy the machine. A step in acceleration causes a large jerk and large

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Table 8.1.1 Displacement, Velocity, Acceleration, and Jerk for Some Cams

SOURCE: Adapted from Gutman, *Mach. Des.,* Mar. 1951.

shock waves to be transmitted and reflected throughout the parts that generate noise and would tend to limit the life of the machine. A step in jerk, the third derivative of the follower displacement with respect to time, seems altogether acceptable. In those designs requiring or exhibiting clearance between the follower and cam (usually at the bottom of the stroke), as gentle and slow a ramp portion as can be tolerated must be inserted on either side of the clearance region to limit the magnitude of the acceleration and jerk to a minimum. The tolerance on the clearance adjustment must be small enough to assure that the follower will be left behind and picked up gradually by the gentle ramp portions of the cam.

Table 8.1.1 shows the comparable and relative magnitudes of velocity, acceleration, and jerk for several high-speed cam, where the displacements are all taken as 1 at time 1 without any overshoot in any of the derivatives.

The three most common forms of motion used are uniform motion (Fig. 8.1.16), harmonic motion (Fig. 8.1.17), and uniformly accelerated and retarded motion (Fig. 8.1.18). In plotting the diagrams (Fig. 8.1.18) for this last motion, divide *ac* into an even number of equal parts and *bc*

into the same number of parts with lengths increasing by a constant increment to a maximum and then decreasing by the same decrement, as, for example, 1, 3, 5, 5, 3, 1, or 1, 3, 5, 7, 9, 9, 7, 5, 3, 1. In order to prevent shock when the direction of motion changes, as at *a* and *b* in the uniform motion, the harmonic motion may be used; if the cam is to be operated at high speed, the uniformly accelerated and retarded motion should preferably be employed; in either case there is a very gradual change of velocity.

Pitch Line The actual pitch line of a cam varies with the type of motion and with the position of the follower relative to the cam's axis. Most cams as ordinarily constructed are covered by the following four cases.

FOLLOWER ON LINE OF AXIS. (Fig. 8.1.19). To draw the pitch line, subdivide the motion *bc* of the follower in the manner indicated in Figs. 8.1.16, 8.1.17, and 8.1.18. Draw a circle with a radius equal to the smallest radius of the cam $a0$ and subdivide it into angles $0a1'$, $0a2'$,

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 $0a3'$, etc., corresponding with angular displacements of the cam for positions 1, 2, 3, etc., of the follower. With *a* as a center and radii *a*1, *a*2, *a*3, etc., strike arcs cutting radial lines at *d, e, f,* etc. Draw a smooth curve through points *d, e, f,* etc.

OFFSET FOLLOWER (Fig. 8.1.20). Divide *bc* as indicated in [Figs.](#page-4-0) [8.1.16,](#page-4-0) 8.1.17, and 8.1.18. Draw a circle of radius *ac* (highest point of rise of follower) and one tangent to *cb* produced. Divide the outer circle into parts $1', 2', 3'$, etc., corresponding with the angular displacement of

the cam for positions 1, 2, 3, etc., of the follower, and draw tangents from points $1', 2', 3'$, etc., to the small circle. With a as a center and radii *a*1, *a*2, *a*3, etc., strike arcs cutting tangents at *d, e, f,* etc. Draw a smooth curve through *d, e, f,* etc.

ROCKER FOLLOWER (Fig. 8.1.21). Divide the stroke of the slide *S* in the manner indicated in [Figs. 8.1.16,](#page-4-0) 8.1.17, and 8.1.18, and transfer these points to the arc *bc* as points 1, 2, 3, etc. Draw a circle of radius *ak* and divide it into parts $1', 2', 3'$, etc., corresponding with angular dis-

placements of the cam for positions 1, 2, 3, etc., of the follower. With *k*, $1', 2', 3'$, etc., as centers and radius *bk*, strike arcs *kb*, $1'd$, $2'e$, $3'f$, etc., cutting at *bdef* arcs struck with *a* as a center and radii *ab, a*1, *a*2, *a*3, etc. Draw a smooth curve through *b, d, e, f,* etc.

CYLINDRICAL CAM (Fig. 8.1.22). In this type of cam, more than one complete turn may be obtained, provided in all cases the follower returns to its starting point. Draw rectangle *wxyz* (Fig. 8.1.22) representing the development of cylindrical surface of the cam. Subdivide the desired motion of the follower *bc* horizontally in the manner indicated in [Figs. 8.1.16,](#page-4-0) 8.1.17, and 8.1.18, and plot the corresponding angular displacement $1', 2', 3'$, etc., of the cam vertically; then through the intersection of lines from these points draw a smooth curve. This may best be shown by an example, assuming the following data for the diagram in Fig. 8.1.22: Total motion of follower $= bc$; circumference of cam = $2\pi r$. Follower moves harmonically 4 units to right in 0.6 turn, then rests (or ''dwells'') 0.4 turn, and finishes with uniform motion 6 units to right and 10 units to left in 2 turns.

Cam Design In the practical design of cams the following points must be noted. If only a small force is to be transmitted, sliding contact may be used, otherwise **rolling contact**. For the latter the pitch line must

be corrected in order to get the true slope of the cam. An approximate construction (Fig. 8.1.23) may be employed by using the pitch line as the center of a series of arcs the radii of which are equal to that of the follower roll to be used; then a smooth curve drawn tangent to the arcs will give the slope desired for a roll working on the periphery of the cam

(Fig. 8.1.23*a*) or in a groove (Fig. 8.1.23*b*). For plate cams the roll should be a small cylinder, as in Fig. 8.1.24*a*. In cylindrical cams it is usually sufficiently accurate to make the roll conical, as in Fig. 8.1.24*b*, in which case the taper of the roll produced should intersect the axis of the cam. If the pitch line *abc* is made too sharp [\(Fig. 8.1.25\)](#page-6-0) the follower

Fig. 8.1.24 Plate cam.

will not rise the full amount. In order to prevent this **loss of rise,** the pitch line should have a radius of curvature at all parts of not less than the roll's diameter plus $\frac{1}{8}$ in. For the same rise of follower, *a*, the angular motion of the cam, *O*, the slope of the cam changes considerably, as indicated by the heavy lines *A*, *B*, and *C* [\(Fig. 8.1.26\).](#page-6-0) Care should be

taken to keep a moderate slope and thereby keep down the side thrust on the follower, but this should not be carried too far, as the cam would become too large and the friction increase.

ROLLING SURFACES

In order to connect two shafts so that they shall have a definite angular velocity ratio, rolling surfaces are often used; and in order to have no slipping between the surfaces they must fulfill the following two conditions: the line of centers must pass through the point of contact,

and the arcs of contact must be of equal length. The angular velocities, expressed usually in r/min, will be inversely proportional to the radii: $N/n =$ *r*/*R.* The two surfaces most commonly used in practice, and the only ones having a constant angular velocity ratio, are cylinders where the shafts are parallel, and cones where the shafts (projected) intersect at an angle. In either case there are

two possible directions of rotation, depending upon whether the surfaces roll in opposite directions (external contact) or in the same direction (internal contact). In Fig. 8.1.27, $R = nc/(N + n)$ and $r = Nc/(N + n)$; in Fig. 8.1.28, $R = nc/(N - n)$ and $r = Nc/(N - n)$. In Fig. 8.1.29, $\tan B = \sin A/(n/N + \cos A)$ and $\tan C = \sin A/$

 $(N/n + \cos A)$; in Fig. 8.1.30, $\tan B = \sin A/(N/n - \cos A)$, and $\tan C = \sin A/(n/N - \cos A)$. With the above values for the angles *B* and *C*, and the length *d* or *e* of one of the cones, *R* and *r* may be calculated.

The natural limitations of **rolling without slip,** with the use of pure rolling surfaces limited to the transmission of very small amounts of torque, led historically to the alteration of the geometric surfaces to include teeth and tooth spaces, i.e., **toothed wheels,** or simply **gears**. Modern gear tooth systems are described in greater detail in Sec. 8.3. This brief discussion is limited to the kinematic considerations of some common gear combinations.

EPICYCLIC TRAINS

Epicyclic trains are combinations of gears in which some of or all the gears have a motion compounded of rotation about an axis and a translation or revolution of that axis. The gears are usually connected by a link called an arm, which often rotates about the axis of the first gear. Such trains may be calculated by first considering all gears locked and the arm turned; then the arm locked and the gears rotated. The algebraic sum of the separate motions will give the desired result. The following examples and method of tabulation will illustrate this. The figures on each gear refer to the number of teeth for that gear.

In Figs. 8.1.31 and 8.1.32 lock the gears and turn the arm *A* righthanded through 1 revolution $(+1)$; then lock the arm and turn the gear *B* back to where it started (-1) ; gears *C* and *D* will have rotated the amount indicated in the tabulation. Then the algebraic sum will give the relative turns of each gear. That is, in Fig. 8.1.31, for one turn of the

Figs. 8.1.31 and 8.1.32 Epicyclic trains.

arm, *B* does not move and *C* turns in the same direction $3\frac{1}{2}$ r, and *D* in the opposite direction $\frac{1}{4}$ r; whereas in Fig. 8.1.32, for one turn of the arm, *B* does not turn, but *C* and *D* turn in the same direction as the arm, respectively, $2\frac{1}{2}$ and $1\frac{3}{7}$ r. (Note: The arm in the above case was turned 1 1 for convenience, but any other value might be used.)

Figs. 8.1.33 and 8.1.34 Bevel epicyclic trains.

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Bevel epicyclic trains are epicyclic trains containing bevel gears and may be calculated by the preceding method, but it is usually simpler to use the general formula which applies to all cases of epicyclic trains:

Turns of C relative to arm
Turns of B relative to arm
absolute turns of
$$
C
$$
 – turns of arm
as of B relative to arm
absolute turns of B – turns of arm

The left-hand term gives the value of the train and can always be expressed in terms of the number of teeth (*T*) on the gears. Care must be used, however, to express it as either plus $(+)$ or minus $(-)$, depending upon whether the gears turn in the same or opposite directions.

Relative turns of
$$
\vec{B} = \frac{C - A}{B - A} = -1
$$
 (in Fig. 8.1.33)

$$
= + \frac{T_E}{T_C} \times \frac{T_B}{T_D}
$$
 (Fig. 8.1.34)

HOISTING MECHANISMS

Pulley Block (Fig. 8.1.35) Given the weight *W* to be raised, the force *F* necessary is $F = V_{W}W/V_{F} = W/n =$ load/number of ropes, V_{W} and V_{F} being the respective velocities of *W* and *F*.

Differential Chain Block (Fig. 8.1.36)

Fig. 8.1.37 Worm and worm wheel.

Fig. 8.1.38 Triplex chain block.

Fig. 8.1.39 Toggle joint.

Worm and Wheel (Fig. 8.1.37) $F = \pi d(n/T)W/(2\pi R) = WP(d/D)/$ $(2\pi R)$, where $n =$ number of threads, single, double, triple, etc.

Triplex Chain Block (Fig. 8.1.38) This geared hoist makes use of the epicyclic train. $W = FL/[M[1 + (T_D/T_C) \times (T_B/T_A)]$, where $T =$ number of teeth on gears.

Toggle Joint (Fig. 8.1.39) $P = Fs (\cos A)/t$.

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by Antonio F. Baldo

REFERENCES: American National Standards Institute (ANSI) Standards. International Organization for Standardization (ISO) Standards. Morden, ''Industrial Fasteners Handbook,'' Trade and Technical Press. Parmley, ''Standard Handbook of Fastening and Joining,'' McGraw-Hill. Bickford, ''An Introduction to the Design and Behavior of Bolted Joints,'' Marcel Dekker. Maleev, ''Machine Design,'' International Textbook. Shigley, ''Mechanical Engineering Design,'' McGraw-Hill. *Machine Design* magazine, Penton/IPC. ANSI/Rubber Manufacturers Assn. (ANSI/RMA) Standards. ''Handbook of Power Transmission Flat Belting,'' Goodyear Rubber Products Co. ''Industrial V-Belting,'' Goodyear Rubber Products Co. Carlson, ''Spring Designer's Handbook,'' Marcel Dekker. American Chain Assn., ''Chains for Power Transmission and Material Handling —Design and Applications Handbook,'' Marcel Dekker. ''Power Transmission Handbook,'' DAYCO. ''Wire Rope User's Manual,'' American Iron and Steel Institute. Blake, ''Threaded Fasteners—Materials and Design,'' Marcel Dekker.

NOTE. At this writing, conversion to metric hardware and machine elements continues. SI units are introduced as appropriate, but the bulk of the material is still presented in the form in which the designer or reader will find it available.

SCREW FASTENINGS

At present there exist two major standards for screw threads, namely Unified inch screw threads and metric screw threads. Both systems enjoy a wide application globally, but movement toward a greater use of the metric system continues.

Unified Inch Screw Threads (or Unified Screw Threads)

The Unified Thread Standard originated by an accord of screw thread standardization committees of Canada, the United Kingdom, and the United States in 1984. The Unified Screw-Thread Standard was published by ANSI as American Unified and American Screw Thread Publication B1.1-1974, revised in 1982 and then again in 1989. Revisions did not tamper with the basic 1974 thread forms. In conjunction with Technical Committee No. 1 of the ISO, the Unified Standard was adopted as an ISO Inch Screw Standard (ISO 5864-1978).

Of the numerous and different screw thread forms, those of greatest consequence are

UN—unified (no mandatory radiused root)

UNR—unified (mandatory radiused root; minimum $0.108 = p$)

UNJ—unified (mandatory larger radiused root; recommended $0.150 = p$

M—metric (inherently designed and manufactured with radiused root; has $0.125 = p$)

MJ—metric (mandatory larger radiused root; recommended $0.150 = p$

The basic American screw thread profile was standardized in 1974, and it now carries the UN designations ($UN =$ unified). ANSI publishes these standards and all subsequent revisions. At intervals these standards are published with a ''reaffirmation date'' (that is, R1988). In 1969 an *international* basic thread profile standard was established, and it is designated as M. The ISO publishes these standards with yearly updates. The UN and M profiles are the same, but **UN screws** are manufactured to **inch** dimensions while **M screws** are manufactured to **metric** dimensions.

The **metric system** has only the two thread forms: **M**, standard for commercial uses, and **MJ**, standard for aerospace use and for aerospace-quality commercial use.

Certain groups of diameter and pitch combinations have evolved over time to become those most used commercially. Such groups are called **thread series.** Currently there are 11 UN series for inch products and 13 M series for metric products.

The Unified standard comprises the following two parts:

1. **Diameter-pitch combinations.** (Se[e Tables 8.2.1](#page-9-0) to 8.2.5.)

NOTE: Radiused roots apply only to external threads. The preponderance of important commercial use leans to UNC, UNF, 8UN (eight-threaded), and metric coarse M. Aerospace and aerospacequality applications use UNJ and MJ.

2. **Tolerance classes.** The amounts of tolerance and allowance distinguish one thread class from another. Classes are designated by one of three numbers (1, 2, 3), and either letter A for external threads or letter B for internal threads. Tolerance decreases as class number increases. Allowance is specified only for classes 1A and 2A. Tolerances are based on engagement length equal to nominal diameter. 1A/1B—liberal tolerance and allowance required to permit easy assembly even with dirty or nicked threads. 2A/2B most commonly used for general applications, including production of bolts, screws, nuts, and similar threaded fasteners. Permits external threads to be plated. 3A/3B—for closeness of fit and/or accuracy of thread applications where zero allowance is needed. 2AG—allowance for rapid assembly where high-temperature expansion prevails or where lubrication problems are important.

Unified screw threads are designated by a set of numbers and letter symbols signifying, in sequence, the nominal size, threads per inch, thread series, tolerance class, hand (only for left hand), and in some instances in parentheses a Thread Acceptability System Requirement of ANSI B1.3.

EXAMPLE. 1⁄4-20 UNC-2A-LH (21), or optionally 0.250-20 UNC-2A-LH (21), where $\frac{1}{4}$ = nominal size (fractional diameter, in, or screw number, with decimal equivalent of either being optional); $20 =$ number of threads per inch, n ; UNC = thread form and series; $2A =$ tolerance class; LH = left hand (no symbol required for right hand); (21) = thread gaging system per ANSI B1.3.

3. **Load considerations**

a. *Static loading.* Only a slight increase in tensile strength in a

screw fastener is realized with an increase in *root* rounding radius, because minor diameter (hence cross-sectional area at the root) growth is small. Thus the basic tensile stress area formula is used in stress calculations for all thread forms. Se[e Tables 8.2.2,](#page-11-0) 8.2.3, and 8.2.4. The designer should take into account such factors as stress concentration as applicable.

b. *Dynamic loading.* Few mechanical joints can remain absolutely free of some form of fluctuating stress, vibration, stress reversal, or impact. Metal-to-metal joints of very high-modulus materials or non-elastic-gasketed high-modulus joints plus preloading at assembly (preload to be greater than highest peak of the external fluctuating load) can realize absolute static conditions inside the screw fastener. For ordinary-modulus joints and elasticgasketed joints, a fraction of the external fluctuating load will be transmitted to the interior of the screw fastener. Thus the fastener must be designed for fatigue according to a **static plus fluctuating load** model. See discussion under ''Strength'' later.

Since **fatigue failures** generally occur at locations of high **stress concentration,** screw fasteners are especially vulnerable because of the abrupt change between head and body, notchlike conditions at the thread roots, surface scratches due to manufacturing, etc. The highest stress concentrations occur at the thread roots. The stress concentration factor can be very large for nonrounded roots, amounting to about 6 for sharp or flat roots, to less than 3 for UNJ and MJ threads which are generously rounded. This can effectively double the fatigue life. UNJ and MJ threads are especially well suited for dynamic loading conditions.

Screw Thread Profile

Basic Profile The basic profiles of UN and UNR are the same, and these in turn are identical to those of ISO metric threads. Basic thread shape (60° thread angle) and basic dimensions (major, pitch, and minor diameters; thread height; crest, and root flats) are defined. See [Fig.](#page-11-0) [8.2.1.](#page-11-0)

Design Profile Design profiles define the maximum material (no allowance) for external and internal threads, and they are derived from the basic profile. UN threads (external) may have either flat or rounded crests and roots. UNR threads (external) must have rounded roots, but may have flat or rounded crests. UN threads (internal) *must* have rounded roots. Any rounding must clear the basic flat roots or crests.

Metric Screw Threads

Metric screw thread standardization has been under the aegis of the International Organization for Standardization (ISO). The ISO basic profile is essentially the same as the Unified screw thread basic form,

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Table 8.2.1 Standard Series Threads (UN/UNR)*

* Series designation shown indicates the UN thread form; however, the UNR thread form may be specified by substituting UNR in place of UN in all designations for external use only.
SOURCE: ANSI B1.1-1982; reaffirmed in 198

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* British: effective diameter.

† See formula under definition of tensile stress area in Appendix B of ANSI B1.1-1987. ‡ Design form. See Fig. 2B in ANSI B1.1-1982 or Fig. 1 in 1989 revision.

§ Secondary sizes. SOURCE: ANSI B1.1-1982, revised 1989; reproduced by permission.

Fig. 8.2.1 Basic thread profile.

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Table 8.2.3 Basic Dimensions for Fine Thread Series (UNF/UNRF)

* British: effective diameter.
† See formula under definition of tensile stress area in Appendix B of ANSI B1.1-1982.
‡ Design form. See Fig. 2B of ANSI B1.1-1982 or Fig. 1 in 1989 revision.

§ Secondary sizes. SOURCE: ANSI B1.1-1982, revised 1989; reproduced by permission.

Table 8.2.4 Basic Dimensions for Extra-Fine Thread Series (UNEF/UNREF)

* British: effective diameter.
† Design form. See Fig. 2B in ANSI B1.1-1982 or Fig. 1 in 1989 revision.
‡ See formula under definition of tensile stress area in Appendix B in ANSI B1.1-1982.
SOURCE: ANSI B1.1-1982 revised

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* Thread diameter should be selected from column 1, 2 or 3; with preference being given in that order.

† Pitch 1.25 mm in combination with diameter 14 mm has been included for spark plug applications.

‡ Diameter 35 mm ha

External thread (bolt), mm Internal thread (nut), mm

Table 8.2.6 Limiting Dimensions of Standard Series Threads for Commercial Screws, Bolts, and Nuts

* Design form, see Figs. 2 and 5 of ANSI B1.13M-1979 (or Figs. 1 and 4 in 1983 revision).

† Required for high-strength applications where rounded root is specified.

SOURCE: [Appeared in ASME/SAE Interpretive document, Metric Screw Threads, B1.13 (Nov. 3, 1966), pp. 9, 10.] ISO 261-1973, reproduced by permission.

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Major diam, min

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and it is shown in [Fig. 8.2.1.](#page-11-0) The ISO thread series (see [Table 8.2.5\)](#page-13-0) are those published in ISO 261-1973. Increased overseas business sparked U.S. interest in metric screw threads, and the ANSI, through its Special Committee to Study Development of an Optimum Metric Fastener System, in joint action with an ISO working group (ISO/TC 1/TC 2), established compromise recommendations regarding metric screw threads. The approved results appear in ANSI B1.13-1979 [\(Table](#page-14-0) [8.2.6\)](#page-14-0). This ANSI metric thread series is essentially a selected subset (boxed-in portion o[f Table 8.2.5](#page-13-0)) of the larger ISO 261-1973 set. The M profiles of tolerance class 6H/6g are intended for metric applications where inch class 2A/2B has been used.

Metric Tolerance Classes for Threads Tolerance classes are a selected combination of tolerance grades and tolerance positions applied to length-of-engagement groups.

Tolerance grades are indicated as numbers for crest diameters of nut and bolt and for pitch diameters of nut and bolt. Tolerance is the acceptable variation permitted on any such diameter.

Tolerance positions are indicated as letters, and are allowances (fundamental deviations) as dictated by field usage or conditions. Capital letters are used for internal threads (nut) and lower case for external threads (bolt).

There are three established groups of length of thread engagement, S (short), N (normal), and L (long), for various diameter-pitch combinations. Normal length of thread engagement is calculated from the formula $N = 4.5pd^{0.2}$, where p is pitch and d is the smallest nominal size within each of a series of groupings of nominal sizes.

In conformance with coating (or plating) requirements and demands of ease of assembly, the following tolerance positions have been established:

See Table 8.2.7 for preferred tolerance classes.

Table 8.2.7 Preferred Tolerance Classes

ISO metric screw threads are designated by a set of number and letter symbols signifying, in sequence, metric symbol, nominal size, \times (symbol), pitch, tolerance grade (on pitch diameter), tolerance position (for pitch diameter), tolerance grade (on crest diameter), and tolerance position (for crest diameter).

EXAMPLE. $M6 \times 0.75$ -5g6g, where M = metric symbol; 6 = nominal size, \times = symbol; 0.75 = pitch-axial distance of adjacent threads measured between corresponding thread points (millimeters); $5 =$ tolerance grade (on pitch diameter); $g =$ tolerance position (for pitch diameter); 6 = tolerance grade (on crest diameter); $g =$ tolerance position (for crest diameter).

Power Transmission Screw Threads: Forms and Proportions

The **Acme** thread appears in four series [ANSI B1.8-1973 (revised 1988) and B1.5-1977]. Generalized dimensions for the series are given in Table 8.2.8.

The 29° general-purpose thread (Fig. 8.2.2) is used for all Acme thread applications outside of special design cases.

The 29° stub thread [\(Fig. 8.2.3\)](#page-16-0) is used for heavy-loading designs and where space constraints or economic factors make a shallow thread advantageous.

The 60° stub thread [\(Fig. 8.2.4\)](#page-16-0) finds special applications in the machine-tool industry.

The 10° modified square thre[ad \(Fig. 8.2](#page-16-0).5) is, for all practical purposes, equivalent to a ''square'' thread.

For selected Acme diameter-pitch combinations, se[e Table 8.2.9.](#page-16-0)

Fig. 8.2.2 29° Acme general-purpose thread.

NOTE: Fine quality applies to precision threads where little variation in fit character is permissible. Coarse quality applies to those threads which present manufacturing difficulties, such as the threading of hot-rolled bars or tapping deep blind holes.

SOURCE: ISO 261-1973, reproduced by permission.

Table 8.2.8 Acme Thread Series

 $(D = \text{outside diam}, p = \text{pitch}.$ All dimensions in inches.) (See Figs. 8.2.2 to 8.2.5.)

* A clearance of at least 0.010 in is added to *h* on threads of 10-pitch and coarser, and 0.005 in on finer pitches, to produce extra depth, thus avoiding interference with threads of mating parts of a minor or major diameters.

† Measured at crest of screw thread.

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| Size | Threads per inch |
|----------------|---------------------|----------------|---------------------|----------------|---------------------|----------------|---------------------|----------------|---------------------|
| $\frac{1}{4}$ | 16 | $\frac{5}{8}$ | | $1\frac{1}{4}$ | | $2^{1/4}$ | | | |
| $\frac{5}{16}$ | 14 | $^{3/4}$ | | $1\frac{3}{8}$ | | $2\frac{1}{2}$ | | $4\frac{1}{2}$ | |
| $\frac{3}{8}$ | | $\frac{7}{8}$ | | $1\frac{1}{2}$ | | $2^{3}/_{4}$ | | | |
| $\frac{7}{16}$ | 12 | | | $1\frac{3}{4}$ | | | | | |
| $\frac{1}{2}$ | 10 | $1\frac{1}{8}$ | | | | $3\frac{1}{2}$ | | | |

Table 8.2.9 Acme Thread Diameter-Pitch Combinations (Se[e Figs. 8.2.2](#page-15-0) to 8.2.5.)

Three classes (2G, 3G, 4G) of general-purpose threads have clearances on all diameters for free movement. A fourth class (5G) of general-purpose threads has no allowance or clearance on the pitch diameter for purposes of minimum end play or backlash.

Fig. 8.2.3 29° stub Acme thread.

Fig. 8.2.4 60° stub Acme thread.

Fig. 8.2.5 10° modified square thread.

High-Strength Bolting Screw Threads

High-strength bolting applications include pressure vessels, steel pipe flanges, fittings, valves, and other services. They can be used for either hot or cold surfaces where high tensile stresses are produced when the joints are made up. For sizes 1 in and smaller, the ANSI coarse-thread series is used. For larger sizes, the ANSI 8-pitch thread series is used (se[e Table 8.2.10\)](#page-17-0).

Screw Threads for Pipes

American National Standard Taper Pipe Thread (ANSI/ASME B1.20.1-1983) This thread is shown in Fig. 8.2.6. It is made to the following specifications: The taper is 1 in 16 or 0.75 in/ft. The basic length of the external taper thread is determined by $L_2 = p(0.8D + 6.8)$, where *D* is the basic outside diameter of the pipe (see [Table 8.2.11\)](#page-17-0). Thread designation and notation is written as: nominal size, number of threads per inch, thread series. For example: 3⁄8-18 NPT, 1⁄8-27 NPSC, $1/2$ -14 NPTR, $1/8$ -27 NPSM, $1/8$ -27 NPSL, 1-11.5 NPSH, where N = National (American) Standard, $T = \text{taper}$, $C = \text{coupling}$, $S = \text{straight}$, M = mechanical, L = locknut, H = hose coupling, and R = rail fittings. Where pressure-tight joints are required, it is intended that taper pipe threads be made up wrench-tight with a sealant. Descriptions of thread series include: $NPSM = free-fitting mechanical joints for fixtures,$ $NPSL =$ loose-fitting mechanical joints with locknuts, $NPSH =$ loosefitting mechanical joints for hose coupling.

Fig. 8.2.6 American National Standard taper pipe threads.

American National Standard Straight Pipe Thread (ANSI/ASME B1.20.1-1983) This thread can be used to advantage for the following: (1) pressure-tight joints with sealer; (2) pressuretight joints without sealer for drain plugs, filler plugs, etc.; (3) free-fitting mechanical joints for fixtures; (4) loose-fitting mechanical joints with locknuts; and (5) loose-fitting mechanical joints for hose couplings. Dimensions are shown in [Table 8.2.12.](#page-18-0)

American National Standard Dry-Seal Pipe Threads (ANSI B1.20.3-1976 (inch), ANSI B1.20.4-1976 (metric translation) Thread designation and notation include nominal size, number of threads per inch, thread series, class. For example, 1⁄8-27 NPTF-1, 1⁄8-27 NPTF-2, $\frac{1}{8}$ -27 PTF-SAE short, $\frac{1}{8}$ -27 NPSI, where N = National (American) standard, P = pipe, T = taper, S = straight, F = fuel and oil, I = intermediate. NPTF has two classes: class $1 =$ specific inspection of root and crest truncation *not* required; class $2 =$ specific inspection of root and crest truncation *is* required. The series includes: NPTF for all types of service; PTF-SAE short where clearance is not sufficient for full thread length as NPTF; NPSF, nontapered, economical to produce, and used with soft or ductile materials; NPSI nontapered, thick sections with little expansion.

Dry-seal pipe threads resemble tapered pipe threads except the form is truncated (see Fig. 8.2.7), and $L_4 = L_2 + 1$ (see Fig. 8.2.6). Although these threads are designed for nonlubricated joints, as in automobile work, under certain conditions a lubricant is used to prevent galling. [Table 8.2.13](#page-18-0) lists truncation values.

Tap drill sizes for tapered and straight pipe threads are listed in [Table](#page-19-0) [8.2.14.](#page-19-0)

Fig. 8.2.7 American National Standard dry-seal pipe thread.

Wrench bolt heads, nuts, and wrench openings have been standardized (ANSI 18.2-1972). Wrench openings are given in [Table 8.2.15;](#page-19-0) bolt head and nut dimensions are in [Table 8.2.16.](#page-20-0)

Machine Screws

Machine screws are defined according to head types as follows: **Flat Head** This screw has a flat surface for the top of the head with a

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Table 8.2.10 Screw Threads for High-Strength Bolting

(All dimensions in inches)

The Unified form of thread shall be used. Pitch diameter tolerances include errors of lead and angle. * The maximum pitch diameters of screws are smaller than the minimum pitch diameters of nuts by these amounts.

Table 8.2.11 ANSI Taper Pipe Thread

(All dimensions in inches) (Se[e Fig. 8.2.6.\)](#page-16-0)

Table 8.2.12 ANSI Straight Pipe Threads (All dimensions in inches)

Pressure-tight Pressure-tight

12 8 — — — — — — — — 12.6491 12.732 12.6686 12.574

countersink angle of 82°. It is standard for machine screws, cap screws, and wood screws.

Round Head This screw has a semielliptical head and is standard for machine screws, cap screws, and wood screws except that for the cap screw it is called *button head.*

Fillister Head This screw has a rounded surface for the top of the head, the remainder being cylindrical. The head is standard for machine screws and cap screws.

Oval Head This screw has a rounded surface for the top of the head and a countersink angle of 82°. It is standard for machine screws and wood screws.

Hexagon Head This screw has a hexagonal head for use with external wrenches. It is standard for machine screws.

Socket Head This screw has an internal hexagonal socket in the head for internal wrenching. It is standard for cap screws.

These screw heads are shown in Fig. 8.2.8; pertinent dimensions are in [Table 8.2.17.](#page-21-0) There are many more machine screw head shapes available to the designer for special purposes, and many are found in the literature. In addition, lots of different screw head configurations have been developed to render fasteners ''tamperproof''; these, too, are found in manufacturers' catalogs or the trade literature.

Eyebolts

Eyebolts are classified as rivet, nut, or screw, and can be had on a swivel. Se[e Fig. 8.2.9](#page-21-0) an[d Table 8.2.18.](#page-22-0) The safe working load may be obtained for each application by applying an appropriate factor of safety.

Driving recesses come in many forms and types and can be found in company catalog[s. Figure 8.2.10](#page-21-0) shows a representative set.

Setscrews are used for fastening collars, sheaves, gears, etc. to shafts to prevent relative rotation or translation. They are available in a variety of head and point styles, as shown in [Fig. 8.2.11.](#page-22-0) A complete tabulation of dimensions is found in ANSI/ASME B18.3-1982 (R86), ANSI 18.6.2-1977 (R93), and ANSI 18.6.3-1977 (R91). Holding power for various sizes is given in [Table 8.2.19.](#page-22-0)

Free-fitting (NPSM) Loose-fitting (NPSL)

Locking Fasteners

Locking fasteners are used to prevent loosening of a threaded fastener in service and are available in a wide variety differing vastly in design, performance, and function. Since each has special features which may make it of particular value in the solution of a given machine problem, it is important that great care be exercised in the selection of a particular

Table 8.2.13 ANSI Dry-Seal Pipe Threads* (Se[e Fig. 8.2.7.](#page-16-0))

* The *truncation* and *width-of-flat* proportions listed above are also valid in the metric system

Fig. 8.2.8 Machine screw heads. (*a*) Flat; (*b*) fillister; (*c*) round; (*d*) oval; (*e*) hexagonal; (*f*) socket.

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* Column 4 values equal column 2 values minus column 1 values.

t Some drill sizes listed may not be standard drills, and in some cases, standard metric drill sizes may be closer to the theoretical inch drill size and standard inch drill sizes may be closer
to the theoretical metric dr

‡ Column 6 values equal column 3 values minus column 1 values.
§ Column 10 values equal column 8 values minus column 1 values.
SOURCE: ANSI B1.20.3-1976 and ANSI B1.20.4-1976, reproduced by permission.

Table 8.2.15 Wrench Bolt Heads, Nuts, and Wrench Openings (All dimensions in inches)

Wrenches shall be marked with the ''nominal size of wrench'' which is equal to the basic or maximum width across flats of the corresponding bolt head or nut. Allowance (min clearance) between maximum width across flats of nut or bolt head and jaws of wrench equals $1.005W + 0.001$. Tolerance on wrench opening equals plus $0.005W + 0.004$ from minimum (W equals nominal size of wr

Table 8.2.16 Width Across Flats of Bolt Heads and Nuts

(All dimensions in inches)

Regular bolt heads are for general use. Unfinished bolt heads are not finished on any surface. Semifinished bolt heads are finished under head.
Regular nuts are for general use. Semifinished nuts are finished on bearing su

design in order that its properties may be fully utilized. These fasteners may be divided into six groups, as follows: seating lock, spring stop nut, interference, wedge, blind, and quick-release. The **seating-lock type** locks only when firmly seated and is therefore free-running on the bolt. The **spring stop-nut type** of fastener functions by a spring action clamping down upon the bolt. The **prevailing torque type** locks by elastic or plastic flow of a portion of the fastener material. A recent development employs an adhesive coating applied to the threads. The **wedge type** locks by relative wedging of either elements or nut and bolt. The **blind type** usually utilizes spring action of the fastener, and the **quick-release type** utilizes a quarter-turn release device. An example of each is shown in [Fig. 8.2.12.](#page-23-0)

One such specification developed for prevailing torque fasteners by the Industrial Fasteners Institute is based on locking torque and may form a precedent for other types of fasteners as well.

Coach and lag screws find application in wood, or in masonry with an expansion anchor. [Figure 8.2.13](#page-25-0)*a* shows two types, and [Table 8.2.20](#page-23-0) lists pertinent dimensions.

Wood screws [ANSI B18.22.1-1975 (R81)] are made in lengths from $\frac{1}{4}$ to 5 in for steel and from $\frac{1}{4}$ to $\frac{31}{2}$ in for brass screws, increasing by $\frac{1}{8}$ in up to 1 in, by $\frac{1}{4}$ in up to 3 in, and by $\frac{1}{2}$ in up to 5 in. Sizes are given in [Table 8.2.21.](#page-23-0) Screws are made with flat, round, or oval heads[. Figure](#page-25-0) [8.2.13](#page-25-0)*b* shows several heads.

Washers [ANSI B18.22.1-1975 (R81)] for bolts and lag screws, either round or square, are made to the dimensions given i[n Table 8.2.22.](#page-23-0) For other types of washers, se[e Fig. 8.2.14](#page-25-0)*a* and *b*.

Self-tapping screws are available in three types. **Thread-forming** tapping screws plastically displace material adjacent to the pilot hole. **Thread-cutting** tapping screws have cutting edges and chip cavities (flutes) and form a mating thread by removing material adjacent to the pilot hole. Thread-cutting screws are generally used to join thicker and harder materials and require a lower driving torque than thread-forming screws. **Metallic drive** screws are forced into the material by pressure and are intended for making permanent fastenings. These three types are further classified on the basis of thread and point form as shown in [Table 8.2.23.](#page-24-0) In addition to these body forms, a number of different

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| | | | Machine screws | | | |
|-------------------------|------------|----------------|--------------------|-----------------|-----------|--------------------------------|
| Nominal size | Screw diam | Flat head | Round head | Fillister head | Oval head | Hexagonal head across flats |
| \overline{c} | 0.086 | 0.172 | 0.162 | 0.140 | 0.172 | 0.125 |
| 3 | 0.099 | 0.199 | 0.187 | 0.161 | 0.199 | 0.187 |
| $\overline{\mathbf{4}}$ | 0.112 | 0.225 | 0.211 | 0.183 | 0.225 | 0.187 |
| 5 | 0.125 | 0.252 | 0.236 | 0.205 | 0.252 | 0.187 |
| 6 | 0.138 | 0.279 | 0.260 | 0.226 | 0.279 | 0.250 |
| 8 | 0.164 | 0.332 | 0.309 | 0.270 | 0.332 | 0.250 |
| 10 | 0.190 | 0.385 | 0.359 | 0.313 | 0.385 | 0.312 |
| 12 | 0.216 | 0.438 | 0.408 | 0.357 | 0.438 | 0.312 |
| $\frac{1}{4}$ | 0.250 | 0.507 | 0.472 | 0.414 | 0.507 | 0.375 |
| $\frac{5}{16}$ | 0.3125 | 0.636 | 0.591 | 0.519 | 0.636 | 0.500 |
| $\frac{3}{8}$ | 0.375 | 0.762 | 0.708 | 0.622 | 0.762 | 0.562 |
| | | | Cap screws | | | |
| Nominal | | | | | | |
| size | Screw diam | Flat head | Button head | Fillister head | | Socket head |
| $\frac{1}{4}$ | 0.250 | $\frac{1}{2}$ | $\frac{7}{16}$ | $\frac{3}{8}$ | | $\frac{3}{8}$ |
| $\frac{5}{16}$ | 0.3125 | $\frac{5}{8}$ | $\frac{9}{16}$ | $\frac{7}{16}$ | | $\frac{7}{16}$ |
| $\frac{3}{8}$ | 0.375 | $^{3}/_{4}$ | $\frac{5}{8}$ | $\frac{9}{16}$ | | $\frac{9}{16}$ |
| $\frac{7}{16}$ | 0.4375 | 13/16 | $^{3}/_{4}$ | $\frac{5}{8}$ | | $\frac{5}{8}$ |
| $\frac{1}{2}$ | 0.500 | $\frac{7}{8}$ | 13/16 | $^{3/4}$ | | $\frac{3}{4}$ |
| $\frac{9}{16}$ | 0.5625 | 1 | 15/16 | 13/16 | | 13/16 |
| $5/8$ | 0.625 | $1\frac{1}{8}$ | 1 | $\frac{7}{8}$ | | $\frac{7}{8}$ |
| $^{3/4}$ | 0.750 | $1\frac{3}{8}$ | $1\frac{1}{4}$ | 1 | | 1 |
| $\frac{7}{8}$ | | | | $1\frac{1}{8}$ | | $1\frac{1}{8}$ |
| 1 | | | | $1\frac{5}{16}$ | | $1\frac{5}{16}$ |

Table 8.2.17 Head Diameters (Maximum), In

head types are available. Basic dimensional data are given in [Table](#page-25-0) [8.2.24.](#page-25-0)

Carriage bolts have been standardized in ANSI B18.5-1971, revised 1990. They come in styles shown in [Fig. 8.2.15.](#page-26-0) The range of bolt diameters is no. 10 (= 0.19 in) to 1 in, no. 10 to $\frac{3}{4}$ in, no. 10 to $\frac{1}{2}$ in, and no. 10 to 3⁄4 in, respectively.

Materials, Strength, and Service Adaptability of Bolts and Screws Materials

[Table 8.2.25](#page-25-0) shows the relationship between selected metric bolt classes and SAE and ASTM grades. The first number of a metric bolt class equals the minimum tensile strength (ultimate) in megapascals (MPa) divided by 100, and the second number is the approximate ratio between minimum yield and minimum ultimate strengths.

Fig. 8.2.10 Driving recesses. *(Adapted, with permission, from Machine Design.)*

EXAMPLE. Class 5.8 has a minimum ultimate strength of approximately 500 MPa and a minimum yield strength approximately 80 percent of minimum ultimate strength.

Strength The fillet between head and body, the thread runout point, and the first thread to engage the nut all create stress concentrations causing local stresses much greater than the average tensile stress in the bolt body. The complexity of the stress patterns renders ineffective the ordinary design calculations based on yield or ultimate stresses. Bolt strengths are therefore determined by laboratory tests on bolt-nut assemblies and published as **proof loads.** Fastener manufacturers are required to periodically repeat such tests to ensure that their products meet the original standards.

In order that a bolted joint remain firmly clamped while carrying its external load *P*, the bolt must be tightened first with sufficient torque to induce an initial tensile preload F_i . The total load F_B experienced by the bolt is then $F_B = F_i + \varepsilon P$. The fractional multiplier ε is given by $\varepsilon =$

SCREW FASTENINGS 8-23

(Thomas Laughlin Co., Portland, Me.) (All dimensions in inches)

(Se[e Fig. 8.2.9.\)](#page-21-0)

NOTES: 1. Torsional holding power in inch-pounds is equal to one-half of the axial holding power times the shaft diameter in inches.

2. Experimental data were obtained by seating an alloy-steel cup-point setscrew against a steel shaft with a hardness of Rockwell C 15. Screw threads were class 3A, tapped holes were class 2B. Holding power was defined as the minimum load necessary to produce 0.01 in of relative movement between the shaft and the collar.

3. Cone points will develop a slightly greater holding power; flat, dog, and oval points, slightly less.

4. Shaft hardness should be at least 10 Rockwell C points less than the setscrew point. 5. Holding power is proportional to seating torque. Torsional holding power is increased

about 6% by use of a flat on the shaft.

6. Data by F. R. Kull, Fasteners Book Issue, *Mach. Des.,* Mar. 11, 1965.

Hollow Hollow oval point flat point

Fig. 8.2.11 Setscrews.

 $K_B/(K_B + K_M)$, where K_B = elastic constant of the bolt and $1/K_M$ = $1/K_N + 1/K_W + 1/K_G + 1/K_J$. K_N = elastic constant of the nut; K_W = elastic constant of the washer; K_G = elastic constant of the gasket; K_J = elastic constant of the clamped surfaces or joint.

By manipulation, the fractional multiplier can be written $\varepsilon =$ $1/(1 + K_M/K_B)$. When K_M/K_B approaches 0, $\varepsilon \rightarrow 1$. When K_M/K_B approaches infinity, $\varepsilon \to 0$. Generally, K_N , K_W , and K_J are much stiffer than K_B , while K_G can vary from very soft to very stiff. In a metal-tometal joint, K_G is effectively infinity, which causes K_M to approach infinity and ε to approach 0. On the other hand, for a very soft gasketed joint, $K_M \rightarrow 0$ and $\varepsilon \rightarrow 1$. For a metal-to-metal joint, then, $F_B =$ $F_i + 0 \times P = F_i$; thus no fluctuating load component enters the bolt. In that case, the bolt remains at *static force* F_i at all times, and the static design will suffice. For a very soft gasketed joint, $F_B = F_i + 1 \times P =$ $F_i + P$, which means that if *P* is a dynamically fluctuating load, it will be superimposed onto the static value of F_i . Accordingly, one must use the *fatigue design* for the bolt. Of course, for conditions between $\varepsilon = 0$ and $\varepsilon = 1$, the load within the bolt body is $F_B = F_i + \varepsilon P$, and again the *fatigue design* must be used.

In general, one wants as much preload as a bolt and joint will tolerate, without damaging the clamped parts, encouraging stress corrosion, or reducing fatigue life. For ungasketed, unpressurized joints under static loads using high-quality bolt materials, such as SAE 3 or better, the preload should be about 90 percent of proof load.

The **proof strength** is the stress obtained by dividing **proof load** by **stress area.** Stress area is somewhat larger than the root area and can be found in thread tables, or calculated approximately from a diameter which is the mean of the root and pitch diameters.

Initial sizing of bolts can be made by calculating area = $(\% \times \text{proof})$ load)/(proof strength)[. See Table 8.2.26](#page-26-0) for typical physical properties.

NOTE. In European practice, proof stress of a given grade is independent of diameter and is accomplished by varying chemical composition with diameters.

Hollow half dog point

Square head cone point

Square head cup point

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Fig. 8.2.12 Locking fasteners.

General Notes on the Design of Bolted Joints

Bolts subjected to shock and sudden change in load are found to be more serviceable when the unthreaded portion of the bolt is turned down or drilled to the area of the root of the thread. The drilled bolt is stronger in torsion than the turned-down bolt.

When a **number of bolts** are **employed in fastening** together two parts of a machine, such as a cylinder and cylinder head, the load carried by each bolt depends on its relative tightness, the tighter bolts carrying the

Table 8.2.20 Coach and Lag Screws

greater loads. When the conditions of assembly result in differences in tightness, lower working stresses must be used in designing the bolts than otherwise are necessary. On the other hand, it may be desirable to have the bolts the weakest part of the machine, since their breakage from overload in the machine may result in a minimum replacement cost. In such cases, the breaking load of the bolts may well be equal to the load which causes the weakest member of the machine connected to be stressed up to the elastic limit.

Table 8.2.21 American National Standard Wood Screws

Table 8.2.22 Dimensions of Steel Washers, in

SCREW FASTENINGS 8-25

Table 8.2.23 Tapping Screw Forms

SOURCE: *Mach. Des.,* Mar. 11, 1965.

Bolts screwed up tight have an initial stress due to the tightening (preload) before any external load is applied to the machine member. The initial tensile load due to screwing up for a tight joint varies approximately as the diameter of the bolt, and may be estimated at 16,000 lb/in of diameter. The actual value depends upon the applied torque and the efficiency of the screw threads. Applying this rule to bolts of 1-in diam or less results in excessively high stresses, thus demonstrating why bolts of small diameter frequently fail during assembly. It is advisable to use as large-diameter bolts as possible in pressure-tight joints requiring high tightening loads.

In pressure-tight joints without a gasket the force on the bolt under load is essentially never greater than the initial tightening load. When a gasket is used, the total bolt force is approximately equal to the initial tightening load plus the external load. In the first case, deviations from the rule are a result of elastic behavior of the joint faces without a gasket, and inelastic behavior of the gasket in the latter case. The fol-

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Table 8.2.24 Self-Tapping Screws

lowing generalization will serve as a guide. If the bolt is more yielding than the connecting members, it should be designed simply to resist the initial tension or the external load, whichever is greater. If the probable yielding of the bolt is 50 to 100 percent of that of the connected members, take the resultant bolt load as the initial tension plus one-half the external load. If the yielding of the connected members is probably four to five times that of the bolt (as when certain packings are used), take the resultant bolt load as the initial tension plus three-fourths the external load.

Table 8.2.25 ISO Metric Fastener Materials

screws.

SOURCE: Bickford, ''An Introduction to the Design and Behavior of Bolted Joints,'' Marcel Dekker, 1981; reproduced by permission. See Appendix G for additional metric materials.

In cases where bolts are subjected to cyclic loading, an increase in the initial tightening load decreases the operating stress range. In certain applications it is customary to fix the tightening load as a fraction of the yield-point load of the bolt.

C

C

Fig. 8.2.14*b* Toothed lock washers.

RIVET FASTENINGS 8-27

Core Proof Tensile Yield^d hardness,
trength, strength, Strength, Rockwell SAE ASTM Metric*^c* Nominal strength, strength, strength, Rockwell grade grade grade diameter, in kpsi kpsi kpsi min/max Products*^e* 1 A307 4.6 $\frac{1}{4}$ thru 1¹/₂ 33 60 36 B70/B100 B, Sc, St 2 5.8 $\frac{1}{4}$ thru $\frac{3}{4}$ 55 74 57 B80/B100 B, Sc, St 4.6 Over $\frac{3}{4}$ thru $\frac{1}{2}$ 33 60 36 B70/B100 B, Sc, St 4 8.9 $\frac{1}{4}$ thru $\frac{1}{2}$ 65^f 115 100 C22/C32 St 5 A449 or A325 8.8 1⁄4 thru 1 85 120 92 C25/C34 B, Sc, St type 1 7.8 Over 1 thru 1¹/₂ 74 105 81 C19/C30 B, Sc, St 8.6 Over $1\frac{1}{2}$ to 3 55 90 58 B, Sc, St 5.1 8.8 No. 6 thru ⁵/₈ 85 120 C25/C40 Se 8.8 No. 6 thru $\frac{1}{2}$ 85 120 C25/C40 B, Sc, St 5.2 A325 type 2 8.8 $\frac{1}{4}$ thru 1 85 120 92 C26/C36 B, Sc 7*^g* 10.9 3⁄4 thru 11⁄2 105 133 115 C28/C34 B, Sc 8 A354 Grade BD 10.9 $\frac{1}{4}$ thru $\frac{1}{2}$ 120 150 130 C33/C39 B, Sc, St 8.1 10.9 $\frac{1}{4}$ thru $\frac{1}{2}$ 120 150 130 C32/C38 St 8.2 10.9 $\frac{1}{4}$ thru 1 120 150 130 C35/C42 B, Sc A574 12.9 0 thru ¹/₂ 140 180 160 C39/C45 SHCS 12.9 ⁵⁄8 thru 1¹/₂ 135 170 160 C37/C45 SHCS

Table 8.2.26*a* **Specifications and Identification Markings for Bolts, Screws, Studs, Sems,***^a* **and U Bolts***^b* (Multiply the strengths in kpsi by 6.89 to get the strength in MPa.)

NOTE: Company catalogs should be consulted regarding *proof loads*. However, approximate values of proof loads may be calculated from: proof load = proof strength \times stress area. *^a* Sems are screw and washer assemblies.

^b Compiled from ANSI/SAE J429j; ANSI B18.3.1-1978; and ASTM A307, A325, A354, A449, and A574.

Example a both capacity and x is approximately 0.01 S_{ut} in MPa and x is the ratio of the minimum S_y to S_{ut}.
^d Yield strength is stress at which a permanent set of 0.2% of gage length occurs.

 $B = \text{ bolt}$, $\overrightarrow{Sc} = \text{Screws}$, $\overrightarrow{St} = \text{studs}$, $\overrightarrow{Se} = \text{sems}$, and $\overrightarrow{SHCS} = \text{socket head cap screws}$.

^f Entry appears to be in error but conforms to the standard, ANSI/SAE J429j.

^g Grade 7 bolts and screws are roll-threaded after heat treatment.

SOURCE: Shigley and Mitchell, ''Mechanical Engineering Design,'' 4th ed., McGraw-Hill, 1983, by permission.

In order to avoid the possibility of bolt failure in pressure-tight joints and to obtain uniformity in bolt loads, some means of determining initial bolt load **(preload)** is desirable. Calibrated torque wrenches are available for this purpose, reading directly in inch-pounds or inchounces. Inaccuracies in initial bolt load are possible even when using a torque wrench, owing to variations in the coefficient of friction between the nut and the bolt and, further, between the nut or bolthead and the abutting surface.

An exact method to determine the preload in a bolt requires that the bolt elongation be measured. For a through bolt in which both ends are accessible, the elongation is measured, and the preload force *P* is obtained from the relationship

$$
P = A E e \div l
$$

where $E =$ modulus of elasticity, $l =$ original length, $A =$ crosssectional area, $e =$ elongation. In cases where both ends of the bolt are not accessible, strain-gage techniques may be employed to determine the strain in the bolt, and thence the preload.

High-strength bolts designated ASTM A325 and A490 are almost exclusively employed in the assembly of structural steel members, but they are applied in mechanical assemblies such as flanged joints. The direct tension indicator (DTI) [\(Fig. 8.2.16\)](#page-28-0), for use with high-strength bolts, allows **bolt preload** to be applied rapidly and simply. The device is a hardened washer with embossed protrusion[s \(Fig. 8.2.1](#page-28-0)6*a*). Tightening the bolt causes the protrusions to flatten and results in a decrease in the gap between washer and bolthead. The prescribed degree of bolttightening load, or preload, is obtained when the gap is reduced to a predetermined amoun[t \(Fig. 8.2.16](#page-28-0)*c*). A feeler gage of a given thickness is used to determine when the gap has been closed to the prescribed amount [\(Fig. 8.2.16](#page-28-0)*b* and *c*). With a paired bolt and DTI, the degree of gap closure is proportional to bolt preload. The system is reported to provide bolt-preload force accuracy within $+15$ percent of that prescribed [\(Fig. 8.2.16](#page-28-0)*d*). The devices are available in both inch and metric series and are covered under ASTM F959 and F959M.

Preload-indicating bolts and nuts provide visual assurance of preload in that tightening to the desired preload causes the wavy flange to flatten flush with the clamped assembly [\(Fig. 8.2.17\)](#page-28-0).

In drilling and tapping cast iron for steel studs, it is necessary to tap to a

Fig. 8.2.15 Carriage bolts.

depth equal to $1\frac{1}{2}$ times the stud diameter so that the strength of the cast-iron threads in shear may equal the tensile strength of the stud. Drill sizes and depths of hole and thread are given in [Table 8.2.27.](#page-29-0)

It is not good practice to drill holes to be tapped through the metal into pressure spaces, for even though the bolt fits tightly, leakage will result that is difficult to eliminate.

Screw thread inserts made of high-strength material [\(Fig. 8.2.18\)](#page-28-0) are useful in many cases to provide increased thread strength and life. Soft or ductile materials tapped to receive thread inserts exhibit improved load-carrying capacity under static and dynamic loading conditions. Holes in which threads have been stripped or otherwise damaged can be restored through the use of thread inserts.

Holes for thread inserts are drilled oversize and specially tapped to receive the insert selected to mate with the threaded fastener used. The standard material for inserts is 18-8 stainless steel, but other materials are available, such as phosphor bronze and Inconel. Recommended insert lengths are given in [Table 8.2.28.](#page-29-0)

Drill Sizes Unified thread taps are listed i[n Table 8.2.29.](#page-29-0)

RIVET FASTENINGS

Forms and Proportion of Rivets The forms and proportions of small and large rivets have been standardized and conform to ANSI B18.1.1-1972 (R89) and B18.1.2-1972 (R89) [\(Figs. 8.2.19](#page-28-0)*a* and *b*).

Materials Specifications for Rivets and Plates See Sec. 6 and 12.2. **Conventional signs** to indicate the form of the head to be used and Copyright (C) 1999 by The McGraw-Hill Companies, Inc. All rights reserved. Use of this product is subject to the terms of its License Agreement. [Click here to view.](#page-0-0)

SOURCE: ANSI B18.2.1–1981 (R92), Appendix III, p. 41. By permission.

RIVET FASTENINGS 8-29

DTI Gaps To Give Required Minimum Bolt Tension

Minimum Bolt Tensions

With average gaps equal or less than above, bolt tensions will be greater than in adjacent listing

(d)

whether the rivet is to be driven in the shop or the field at the time of erection are given i[n Fig. 8.2.20.](#page-29-0) **Rivet lengths** and **grips** are shown in Fig. 8.2.19*b*.

For **structural riveting,** see Sec. 12.2.

Punched vs. Drilled Plates Holes in plates forming parts of riveted structures are punched, punched and reamed, or drilled. Punching, while

Fig. 8.2.17 Load-indicating wavy-flange bolt (or nut).

cheaper, is objectionable. The holes in different plates cannot be spaced with sufficient accuracy to register perfectly on being assembled. If the hole is punched out, say $\frac{1}{16}$ in smaller than is required and then reamed to size, the metal injury by cold flow during punching will be removed. Drilling, while more expensive, is more accurate and does not injure the metal.

Tubular Rivets

In tubular rivets, the end opposite the head is made with an axial hole (partway) to form a thin-walled, easily upsettable end. As the material at the edge of the rivet hole is rolled over against the surface of the joint, a **clinch** is formed [\(Fig. 8.2.21](#page-30-0)*a*).

Two-part tubular rivets have a thin-walled head with attached thinwalled rivet body and a separate thin-walled expandable plug. The head-body is inserted through a hole in the joint from one side, and the plug from the other. By holding an anvil against the plug bottom and

8-30 MACHINE ELEMENTS

Table 8.2.27 Depths to Drill and Tap Cast Iron for Studs

| Diam of stud, in | $^{1/4}$ | $^{5/16}$ | $\frac{3}{8}$ | $\frac{1}{6}$ | $\frac{1}{2}$ | $\frac{9}{16}$ | 5/8 | | | |
|---------------------|----------------|-----------------|----------------|---------------|---------------|----------------|-----------------|----------------|-----------------|----------------|
| Diam of drill, in | 13/64 | $\frac{17}{64}$ | $\frac{5}{16}$ | $\frac{3}{8}$ | 27/64 | 31/64 | 17/32 | 41/64 | | 55/64 |
| Depth of thread, in | $\frac{3}{8}$ | 15/32 | $\frac{9}{16}$ | 21/32 | | 27/32 | 15/16 | $1\frac{1}{8}$ | 15/16 | $1\frac{1}{2}$ |
| Depth to drill, in | $\frac{7}{16}$ | $\frac{17}{32}$ | $\frac{5}{8}$ | 23/32 | 27/32 | 15/16 | $1\frac{1}{32}$ | $1\frac{1}{4}$ | $\frac{17}{16}$ | $1\frac{5}{8}$ |

Table 8.2.28 Screw-Thread Insert Lengths (Heli-Coil Corp.)

hammering on the head, the plug is caused to expand within the head, thus locking both parts together [\(Fig. 8.2.21](#page-30-0)*a*).

Blind Rivets

Blind rivets are inserted and set all from one side of a structure. This is accomplished by mechanically expanding, through the use of the rivet's built-in mandrel, the back (blind side) of the rivet into a bulb or upset head after insertion. Blind rivets include the *pull type* and *drive-pin type.*

The pull-type rivet is available in two configurations: a self-plugging type and a pull-through type. In the self-plugging type, part of the mandrel remains permanently in the rivet body after setting, contributing additional shear strength to the fastener. In the pull-through type, the entire mandrel is pulled through, leaving the installed rivet empty.

In a drive-pin rivet, the rivet body is slotted. A pin is driven forward into the rivet, causing both flaring of the rivet body and upset of the blind side [\(Fig. 8.2.21](#page-30-0)*b*).

Fig. 8.2.19*a* Rivet heads.

Fig. 8.2.19*b* Rivet length and grip.

Fig. 8.2.20 Conventional signs for rivets.

Table 8.2.29 Tap-Drill Sizes for American National Standard Screw Threads (The sizes listed are the commercial tap drills to produce approx 75% full thread)

| Size | | Coarse-thread series | | Fine-thread series | | Coarse-thread series | | Fine-thread series | |
|--------------------------------|---------------------|-------------------------|---------------------|-----------------------|----------------|-------------------------|-------------------|-----------------------|-------------------|
| | Threads per inch | Tap drill size | Threads per inch | Tap drill size | Size | Threads per inch | Tap drill size | Threads per inch | Tap drill size |
| No. 0 | | | 80 | $^{3}/_{64}$ | $^{3}/_{4}$ | 10 | 21/32 | 16 | 11/16 |
| No. 1 | 64 | No. 53 | 72 | No. 53 | $\frac{7}{8}$ | 9 | 49/64 | 14 | 13/16 |
| No. 2 | 56 | No. 50 | 64 | No. 50 | | 8 | $\frac{7}{8}$ | 14 | 15/16 |
| $\overline{\mathbf{3}}$ No. | 48 | No. 47 | 56 | No. 45 | $1\frac{1}{8}$ | 7 | 63/64 | 12 | $1\frac{3}{64}$ |
| No. 4 | 40 | No. 43 | 48 | No. 42 | $1\frac{1}{4}$ | 7 | $1\frac{7}{64}$ | 12 | $1^{11}/_{64}$ |
| No. 5 | 40 | No. 38 | 44 | No. 37 | $1\frac{3}{8}$ | 6 | $1\frac{7}{32}$ | 12 | $1^{19}/_{64}$ |
| No. 6 | 32 | No. 36 | 40 | No. 33 | $1\frac{1}{2}$ | 6 | $1^{21}/_{64}$ | 12 | $1^{27}/_{64}$ |
| No. 8 | 32 | No. 29 | 36 | No. 29 | $1\frac{3}{4}$ | 5 | $1^{35}/_{64}$ | | |
| No. 10 | 24 | No. 25 | 32 | No. 21 | 2 | $4\frac{1}{2}$ | $1^{25/32}$ | | |
| No. 12 | 24 | No. 16 | 28 | No. 14 | $2\frac{1}{4}$ | $4\frac{1}{2}$ | $2\frac{1}{32}$ | | |
| $\frac{1}{4}$ | 20 | No. 7 | 28 | No. 3 | $2\frac{1}{2}$ | 4 | $2\frac{1}{4}$ | | |
| $\frac{5}{16}$ | 18 | F | 24 | I | $2^{3}/_{4}$ | $\overline{4}$ | $2\frac{1}{2}$ | | |
| $\frac{3}{8}$ | 16 | $\frac{5}{16}$ | 24 | Q | 3 | $\overline{4}$ | $2^{3/4}$ | | |
| $\frac{7}{16}$ | 14 | U | 20 | 25/64 | $3\frac{1}{4}$ | $\overline{4}$ | $\overline{3}$ | | |
| $\frac{1}{2}$ | 13 | 27/64 | 20 | 29/64 | $3\frac{1}{2}$ | $\overline{4}$ | $3\frac{1}{4}$ | | |
| $\frac{9}{16}$ | 12 | 31/64 | 18 | 33/64 | $3\frac{3}{4}$ | $\overline{4}$ | $3\frac{1}{2}$ | | |
| $\frac{5}{8}$ | 11 | 17/32 | 18 | 37/64 | 4 | 4 | $3^{3}/_{4}$ | | |

Fig. 8.2.21*a* Tubular rivets.

KEYS, PINS, AND COTTERS

Keys and key seats have been standardized and are listed in ANSI B17.1-1967 (R89). Descriptions of the principal key types follow.

Woodruff keys [ANSI B17.2-1967 (R90)] are made to facilitate removal of pulleys from shafts. They should not be used as sliding keys. Cutters for milling out the key seats, as well as special machines for using the cutters, are to be had from the manufacturer. Where the hub of the gear or pulley is relatively long, two keys should be used. Slightly rounding the corners or ends of these keys will obviate any difficulty met with in removing pulleys from shafts. The key is shown in Fig. 8.2.22 and the dimensions in [Table 8.2.30.](#page-31-0)

Square and flat plain taper keys have the same dimensions as gib-head keys [\(Table 8.2.31](#page-31-0)) up to the dotted line of Fig. 8.2.23. **Gib-head keys** (Fig. 8.2.23) are necessary when the smaller end is inaccessible for drifting out and the larger end is accessible. It can be used, with care,

Fig. 8.2.22 Woodruff key.

Fig. 8.2.23 Gib-head taper stock key.

with all sizes of shafts. Its use is forbidden in certain jobs and places for safety reasons. Proportions are given in [Table 8.2.31.](#page-31-0)

The minimum stock length of keys is 4 times the key width, and maximum stock length of keys is 16 times the key width. The increments of increase of length are 2 times the width.

Sunk keys are made to the form and dimensions given i[n Fig. 8.2.24](#page-32-0) an[d Table 8.2.32.](#page-32-0) These keys are adapted particularly to the case of fitting adjacent parts with neither end of the key accessible. **Feather keys** prevent parts from turning on a shaft while allowing them to move in a lengthwise direction. They are of the forms shown i[n Fig. 8.2.25](#page-32-0) with dimensions as given i[n Table 8.2.32.](#page-32-0)

In **transmitting large torques,** it is customary to use two or more keys.

8-32 MACHINE ELEMENTS

Table 8.2.30 Woodruff Key Dimensions [ANSI B17.2-1967 (R90)] (All dimensions in inches)

Numbers indicate the nominal key dimensions. The last two digits give the nominal diameter (B) in eighths of an inch, and the digits preceding the last two give the nominal width (A) in thirty-seconds of an inch. Thus, 20

Another means for fastening gears, pulleys flanges, etc., to shafts is through the use of mating pairs of tapered sleeves known as **grip springs**. A set of sleeves is shown i[n Fig. 8.2.26.](#page-32-0) For further references see data issued by the Ringfeder Corp., Westwood, NJ.

Tapered pins [\(Fig. 8.2.27\)](#page-32-0) can be used to transmit very small torques or for positioning. They should be fitted so that the parts are drawn together to prevent their working loose when the pin is driven home. [Table 8.2.33](#page-33-0) gives dimensions of Morse tapered pins.

The Groov-Pin Corp., New Jersey, has developed a special **grooved**

pin [\(Fig. 8.2.28\)](#page-32-0) which may be used instead of smooth taper pins in certain cases.

Straight pins, likewise, are used for transmission of light torques or for positioning. **Spring pins** have come into wide use recently. Two types shown i[n Figs. 8.2.29](#page-32-0) and 8.2.30 deform elastically in the radial direction when driven; the resiliency of the pin material locks the pin in place. They can replace straight and taper pins and combine the advantages of both, i.e., simple tooling, ease of removal, reusability, ability to be driven from either side.

Table 8.2.31 Dimensions of Square and Flat Gib-Head Taper Stock Keys, in

| | | | Square type | | | | | Flat type | | | | |
|--------------------------------|-------------------|--|-----------------|-------------------|----------------------------------|-------------------|-------------------------------|-----------------|----------------|----------------------------------|----------------------|--------------------------|
| Shaft diam | | Key | | Gib head | | | Key | | Gib head | | | Tolerance |
| | Max width W | Height at large end, $\dagger H$ | Height C | Length D | Height edge of chamfer E | Max width W | Height at large end,† Η | Height C | Length D | Height edge of chamfer E | On width $(-)$ | On height $^{(+)}$ |
| $\frac{1}{2} - \frac{9}{16}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{4}$ | $\frac{7}{32}$ | $\frac{5}{32}$ | $\frac{1}{8}$ | 3/32 | $\frac{3}{16}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | 0.0020 | 0.0020 |
| $\frac{5}{8} - \frac{7}{8}$ | $\frac{3}{16}$ | $\frac{3}{16}$ | $\frac{5}{16}$ | $\frac{9}{32}$ | $\frac{7}{32}$ | $\frac{3}{16}$ | $\frac{1}{8}$ | $\frac{1}{4}$ | $\frac{3}{16}$ | $\frac{5}{32}$ | 0.0020 | 0.0020 |
| $\frac{15}{16} - \frac{11}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{7}{16}$ | 11/32 | 11/32 | $\frac{1}{4}$ | $\frac{3}{16}$ | $\frac{5}{16}$ | $\frac{1}{4}$ | $\frac{3}{16}$ | 0.0020 | 0.0020 |
| $1\frac{5}{16} - 1\frac{3}{8}$ | $\frac{5}{16}$ | $\frac{5}{16}$ | $\frac{9}{16}$ | 13/32 | 13/32 | $\frac{5}{16}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{5}{16}$ | $\frac{1}{4}$ | 0.0020 | 0.0020 |
| $1\frac{7}{6} - 1\frac{3}{4}$ | $\frac{3}{8}$ | $\frac{3}{8}$ | 11/16 | 15/32 | 15/32 | $\frac{3}{8}$ | $\frac{1}{4}$ | $\frac{7}{16}$ | $\frac{3}{8}$ | $\frac{5}{16}$ | 0.0020 | 0.0020 |
| $1^{13}/_{16} - 2^{1}/_{4}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{7}{8}$ | 19/32 | $\frac{5}{8}$ | $\frac{1}{2}$ | $\frac{3}{8}$ | $\frac{5}{8}$ | $\frac{1}{2}$ | $\frac{7}{16}$ | 0.0025 | 0.0025 |
| $2\frac{5}{16} - 2\frac{3}{4}$ | $\frac{5}{8}$ | $5/8$ | $1\frac{1}{16}$ | 23/32 | $^{3}/_{4}$ | $5/8$ | $\frac{7}{16}$ | $^{3/4}$ | $\frac{5}{8}$ | $\frac{1}{2}$ | 0.0025 | 0.0025 |
| $2\frac{7}{8} - 3\frac{1}{4}$ | $\frac{3}{4}$ | $^{3/4}$ | $1\frac{1}{4}$ | $\frac{7}{8}$ | $\frac{7}{8}$ | $^{3}/_{4}$ | $\frac{1}{2}$ | $\frac{7}{8}$ | $^{3/4}$ | $\frac{5}{8}$ | 0.0025 | 0.0025 |
| $3\frac{3}{8}-3\frac{3}{4}$ | $\frac{7}{8}$ | $\frac{7}{8}$ | $1\frac{1}{2}$ | | | $\frac{7}{8}$ | $5/8$ | $1\frac{1}{16}$ | $\frac{7}{8}$ | $^{3}/_{4}$ | 0.0030 | 0.0030 |
| $3\frac{7}{8}-4\frac{1}{2}$ | | | $1\frac{3}{4}$ | $1\frac{3}{16}$ | $1\frac{3}{16}$ | | $^{3}/_{4}$ | $1\frac{1}{4}$ | | 13/16 | 0.0030 | 0.0030 |
| $43/4 - 51/2$ | $1\frac{1}{4}$ | $1\frac{1}{4}$ | \overline{c} | $1\frac{7}{16}$ | $1\frac{7}{16}$ | $1\frac{1}{4}$ | $\frac{7}{8}$ | $1\frac{1}{2}$ | $1\frac{1}{4}$ | | 0.0030 | 0.0030 |
| $5\frac{3}{4}-6$ | $1\frac{1}{2}$ | $1\frac{1}{2}$ | $2\frac{1}{2}$ | 1 ³ /4 | $1\frac{3}{4}$ | $1\frac{1}{2}$ | | $1^{3/4}$ | $1\frac{1}{2}$ | $1\frac{1}{4}$ | 0.0030 | 0.0030 |

* Stock keys are applicable to the general run of work and the tolerances have been set accordingly. They are not intended to cover the finer applications where a closer fit may be required. † This height of the key is measured at the distance *W* equal to the width of the key, from the gib head.

SPLINES 8-33

Cotter pins (Fig. 8.2.31) are used to secure or lock nuts, clevises, etc. Driven into holes in the shaft, the eye prevents complete passage, and the split ends, deformed after insertion, prevent withdrawal.

Fig. 8.2.24 Sunk key.

Fig. 8.2.25 Feather key.

Fig. 8.2.26 Grip springs.

When two rods are to be joined so as to permit movement at the joint, a round pin is used in place of a cotter. In such cases, the proportions may be as shown in Fig. 8.2.32 (knuckle joint).

Table 8.2.32 Dimensions of Sunk Keys (All dimensions in inches. Letters refer to Fig. 8.2.24)

Fig. 8.2.27 Taper pins.

Fig. 8.2.28 Grooved pins. **Fig. 8.2.29** Roll pin.

Fig. 8.2.30 Spiral pins. **Fig. 8.2.31** Cotter pin.

Fig. 8.2.32 Knuckle joint.

SPLINES

Involute spline proportions, dimensions, fits, and tolerances are given in detail in ANSI B92.1-1970. External and internal involute splines (Fig. 8.2.33) have the same general form as involute gear teeth, except that the teeth are one-half the depth of standard gear teeth and the pressure angle is 30°. The spline is designated by a fraction in which the numerator is the diametral pitch and the denominator is always twice the numerator.

Fig. 8.2.33 Involute spline.

8-34 MACHINE ELEMENTS

There are 17 series, as follows: 2.5/5, 3/6, 4/8, 5/10, 6/12, 8/16, 10/20, 12/24, 16/32, 20/40, 24/48, 32/64, 40/80, 48/96, 64/128, 80/160, 128/256. The number of teeth within each series varies from 6 to 50. Both a flat-root and a fillet-root type are provided. There are three **types of fits:** (1) **major diameter**—fit controlled by varying the major diameter of the external spline; (2) **sides of teeth**—fit controlled by varying tooth thickness and customarily used for fillet-root splines; (3) **minor diameter**—fit controlled by varying the minor diameter of the internal spline. Each type of fit is further divided into three classes: (*a*) **sliding** clearance at all points; (*b*) **close**—close on either major diameter, sides of teeth, or minor diameter; (*c*) **press**—interference on either the major diameter, sides of teeth, or minor diameter. Important basic formulas for tooth proportions are:

Flat and Fillet Roots

$$
D = N/P
$$

\n $p = \pi/P$
\n $t = p/2$
\n $a = 0.5000/P$
\n D_O (external) = $\frac{N+1}{P}$
\nTIF (internal) = $\frac{N+1}{P}$
\n $D_R = \frac{N+1}{P}$ (minor-diameter fits only)
\nTIF (external) = $\frac{N-1}{P}$

 $b = 0.600/P + 0.002$ (For major-diameter fits, the internal spline dedendum is the same as the addendum; for minor-diameter fits, the dedendum of the external spline is the same as the addendum.)

Fillet Root Only

Internal spline dimensions are basic while external spline dimensions are varied to control fit.

The advantages of involute splines are: (1) maximum strength at the minor diameter, (2) self-centering equalizes bearing and stresses among all teeth, and (3) ease of manufacture through the use of standard gearcutting tools and methods.

The design of involute splines is critical in shear. The torque capacity may be determined by the formula $T = LD^2S_s/1.2732$, where $L =$ spline length, $D =$ pitch diam, $S_s =$ allowable shear stress.

Parallel-side splines have been standardized by the SAE for 4, 6, 10, and 16 spline fittings. They are shown in Fig. 8.2.34; pertinent data are in [Tables 8.2.34](#page-34-0) and 8.2.35.

DRY AND VISCOUS COUPLINGS

A **coupling** makes a semipermanent connection between two shafts. They are of three main types: **rigid, flexible,** and **fluid.**

Rigid Couplings

Rigid couplings are used only on shafts which are perfectly aligned. The **flanged-face coupling** [\(Fig. 8.2.35\)](#page-34-0) is the simplest of these. The flanges must be keyed to the shafts. The **keyless compression coupling** [\(Fig.](#page-34-0) [8.2.36\)](#page-34-0) affords a simple means for connecting abutting shafts without the necessity of key seats on the shafts. When drawn over the slotted tapered sleeve the two flanges automatically center the shafts and provide sufficient contact pressure to transmit medium or light loads. **Ribbed-clamp couplings** [\(Fig. 8.2.37\)](#page-34-0) are split longitudinally and are bored to the shaft diameter with a shim separating the two halves. It is necessary to key the shafts to the coupling.

Flexible Couplings

Flexible couplings are designed to connect shafts which are misaligned either laterally or angularly. A secondary benefit is the absorption of

DRY AND VISCOUS COUPLINGS 8-35

Table 8.2.34 Dimensions of Spline Fittings, in (SAE Standard)

* Tolerance allowed of -0.001 in for shafts 3⁄4 to 13⁄4 in, inclusive; of -0.002 for shafts 2 to 3 in, inclusive; -0.003 in for shafts 31/2 to 6 in, inclusive, for 4-, 6-,

and 10-spline fittings; tolerance of -0.003 in allowed for all sizes of 16-spline fittings.
† Tolerance allowed of -0.002 in for shafts 34 in to 134 in, inclusive; of -0.003 in for shafts 2 to 6 in, inclusive, for 4- -0.003 allowed for all sizes of 16-spline fittings.

Table 8.2.35 Spline Proportions

| No. of | W | Permanent fit | | To slide when not under load | | To slide under load | | |
|---------|--------------|---------------|--------|---------------------------------|--------|---------------------|--------|--|
| splines | for all fits | | | h. | | | d | |
| 4 | 0.241D | 0.075D | 0.850D | 0.125D | 0.750D | | | |
| 6 | 0.250D | 0.050D | 0.900D | 0.075D | 0.850D | 0.100D | 0.800D | |
| 10 | 0.156D | 0.045D | 0.910D | 0.070D | 0.860D | 0.095D | 0.810D | |
| 16 | 0.098D | 0.045D | 0.910D | 0.070D | 0.860D | 0.095D | 0.810D | |

impacts due to fluctuations in shaft torque or angular speed. The **Oldham,** or **double-slider, coupling** (Fig. 8.2.38) may be used to connect shafts which have only lateral misalignment. The **''Fast'' flexible coupling** [\(Fig. 8.2.39\)](#page-35-0) consists of two hubs each keyed to its respective shaft. Each hub has generated splines cut at the maximum possible

Fig. 8.2.35 Flanged face coupling.

Fig. 8.2.36 Keyless compression coupling.

distance from the shaft end. Surrounding the hubs is a casing or sleeve which is split transversely and bolted by means of flanges. Each half of this sleeve has generated internal splines cut on its bore at the end opposite to the flange. These internal splines permit a definite error of alignment between the two shafts.

Another type, the Waldron coupling (Midland-Ross Corp.), is shown in [Fig. 8.2.40.](#page-35-0)

The chain coupling shown i[n Fig. 8.2.41](#page-35-0) uses silent chain, but stan-

dard roller chain can be used with the proper mating sprockets. Nylon links enveloping the sprockets are another variation of the chain coupling.

| ٦ | o | 6 | |
|---|---|---|--|
| | | | |

Fig. 8.2.37 Ribbed-clamp coupling.

Steelflex couplings [\(Fig. 8.2.42\)](#page-35-0) are made with two grooved steel hubs keyed to their respective shafts. Connection between the two halves is secured by a specially tempered alloy-steel member called the ''grid.''

Fig. 8.2.38 Double-slider coupling.

In the rubber flexible coupling shown in [Fig. 8.2.43,](#page-35-0) the torque is transmitted through a comparatively soft rubber section acting in shear. The type i[n Fig. 8.2.4](#page-35-0)4 loads the intermediate rubber member in compression. Both types permit reasonable shaft misalignment and are recommended for light loads only.

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Fig. 8.2.39 "Fast" flexible coupling.

Universal joints are used to connect shafts with much larger values of misalignment than can be tolerated by the other types of flexible couplings. Shaft angles up to 30° may be used. The Hooke's-type joint (Fig. 8.2.45) suffers a loss in efficiency with increasing angle which

Fig. 8.2.40 Waldron coupling.

may be approximated for angles up to 15° by the following relation: efficiency = $100(1 - 0.003\theta)$, where θ is the angle between the shafts. The velocity ratio between input and output shafts with a single universal joint is equal to

 $\omega_2 / \omega_1 = \cos \theta / 1 - \sin^2 \theta \sin^2 (\alpha + 90^\circ)$

where ω_2 and ω_1 are the angular velocities of the driven and driving shafts respectively, θ is the angle between the shafts, and α is the angu-

Fig. 8.2.41 Chain coupling.

lar displacement of the driving shaft from the position where the pins on the drive-shaft yoke lie in the plane of the two shafts. A velocity ratio of 1 may be obtained at any angle using two Hooke's-type joints and an intermediate shaft. The intermediate shaft must make equal angles with the main shafts, and the driving pins on the yokes attached to the intermediate shaft must be set parallel to each other.

Fig. 8.2.42 Falk Steelflex coupling.

The Bendix-Weiss ''rolling-ball'' universal joint provides constant angular velocity. Torque is transmitted between two yokes through a set of four balls such that the centers of all four balls lie in a plane which bisects the angle between the shafts. Other variations of constant velocity universal joints are found in the Rzeppa, Tracta, and double Cardan types.

Fig. 8.2.43 Rubber flexible coupling, shear type.

Fig. 8.2.44 Rubber flexible coupling, compression type.

Fig. 8.2.45 Hooke's universal joint.

Fluid Couplings

(See also Sec. 11.)

Fluid couplings (Fig. 8.2.46) have two basic parts—the input member, or impeller, and the output member, or runner. There is no mechanical connection between the two shafts, power being transmitted by kinetic energy in the operating fluid. The impeller *B* is fastened to the flywheel *A* and turns at engine speed. As this speed increases, fluid within the impeller moves toward the outer periphery because of centrifugal force. The circular shape of the impeller directs the fluid toward the runner *C*, where its kinetic energy is absorbed as torque delivered by shaft *D*. The positive pressure behind the fluid causes flow to continue toward the hub and back through the impeller. The toroidal space in both the impeller and runner is divided into compartments by a series of flat radial vanes.

Fig. 8.2.46*a* Fluid coupling. (*A*) Flywheel; (*B*) impeller; (*C*) runner; (*D*) output shaft.

Fig. 8.2.46*b* Schematic of viscous coupling.

The torque capacity of a fluid coupling with a full-load slip of about 2.5 percent is $T = 0.09n^2D^5$, where *n* is the impeller speed, hundreds of r/min, and *D* is the outside diameter, ft. The output torque is equal to the input torque over the entire range of input-output speed ratios. Thus the prime mover can be operated at its most effective speed regardless of the speed of the output shaft. Other advantages are that the prime mover cannot be stalled by application of load and that there is no transmission of shock loads or torsional vibration between the connected shafts.

> A **hydraulic torque converter** (Fig. 8.2.47) is similar in form to the hydraulic coupling, with the addition of a set of stationary guide vans, the reactor, interposed between the runner and the impeller. All blades in a converter have compound curvature. This curvature is designed to control the direction of fluid flow. Kinetic energy is therefore transferred as a result of both a scalar and vectorial change in fluid velocity. The blades are designed such that the fluid will be moving in a direction parallel to the blade surface at the entrance (Fig. 8.2.48) to each section. With a design having fixed blading, this can be true at only one value of runner and impeller velocity, called the design point. Several design modifications are possible to overcome this difficulty. The angle of the blades can be made adjustable, and the elements can be

Fig. 8.2.47 Hydraulic torque converter. (*A*) Flywheel; (*B*) impeller; (*C*) runner; (*D*) output shaft; (*E*) reactor.

divided into sections operating independently of each other according to the load requirements. Other refinements include the addition of multiple stages in the runner and reactor stages as in steam reaction turbines (see Sec. 9). The advantages of a torque converter are the ability to multiply starting torque 5 to 6 times and to serve as a stepless transmission. As in the coupling, torque varies as the square of speed and the fifth power of diameter.

Fig. 8.2.48 Schematic of converter blading. (1) Absolute fluid velocity; (2) velocity vector—converter elements; (3) fluid velocity relative to converter elements.

Optimum efficiency (Fig. 8.2.49) over the range of input-output speed ratios is obtained by a combination converter coupling. When the output speed rises to the point where the torque multiplication factor is 1.0, the clutch point, the torque reaction on the reactor element reverses direction. If the reactor is mounted to freewheel in this opposite direction, the unit will act as a coupling over the higher speed ranges. An automatic friction clutch (see ''Clutches,'' below) set to engage at or near the clutch point will also eliminate the poor efficiency of the converter at high output speeds.

Fig. 8.2.49 Hydraulic coupling characteristic curves. *(Heldt, ''Torque Converters and Transmissions,'' Chilton.)*

Viscous couplings are becoming major players in mainstream frontwheel-drive applications and are already used in four-wheel-drive vehicles.

Torque transmission in a viscous coupling relies on shearing forces in an entrapped fluid between axially positioned disks rotating at different angular velocities [\(Fig. 8.2.46](#page-35-0)*b*), all encased in a lifetime leakproof housing. A hub carries the so-called inner disks while the housing carries the so-called outer disks. Silicone is the working fluid.

Operation of the coupling is in normal (slipping) mode when torque is being generated by viscous shear. However, prolonged slipping under severe starting conditions causes heat-up, which in turn causes the fluid, which has a high coefficient of thermal expansion, to expand considerably with increasing temperature. It then fills the entire available space, causing a rapid pressure increase, which in turn forces the disks together into metal-to-metal frictional contact. Torque transmission now increases substantially. This self-induced torque amplification is known as the **hump effect.** The point at which the hump occurs can be set by the design and coupling setup. Under extreme conditions, 100 percent lockup occurs, thus providing a self-protecting relief from overheating as fluid shear vanishes. This effect is especially useful in autos using viscous couplings in their limited-slip differentials, when one wheel is on low-friction surfaces such as ice. The viscous coupling transfers torque to the other gripping wheel. This effect is also useful when one is driving up slopes with uneven surface conditions, such as rain or snow, or on very rough surfaces. Such viscous coupling differentials have allowed a weight and cost reduction of about 60 percent. A fuller account can be found in Barlage, Viscous Couplings Enter Main Stream Vehicles, *Mech. Eng.,* Oct. 1993.

CLUTCHES

Clutches are couplings which permit the disengagement of the coupled shafts during rotation.

Positive clutches are designed to transmit torque without slip. The **jaw clutch** is the most common type of positive clutch. These are made with **square jaws** [\(Fig. 8.2.50\)](#page-37-0) for driving in both directions or **spiral jaws** [\(Fig. 8.2.51](#page-37-0)) for unidirectional drive. Engagement speed should be limited to 10 r/min for square jaws and 150 r/min for spiral jaws. If disengagement under load is required, the jaws should be finish-machined and lubricated.

Friction clutches are designed to reduce coupling shock by slipping during the engagement period. They also serve as safety devices by slippping when the torque exceeds their maximum rating. They may be

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divided into two main groups, **axial** and **rim clutches,** according to the direction of contact pressure.

The **cone clutch** (Fig. 8.2.52) and the **disk clutch** (Fig. 8.2.53) are examples of axial clutches. The disk clutch may consist of either a

Fig. 8.2.51 Spiral-jaw clutch.

single plate or multiple disks. Table 8.2.36 lists typical friction materials and important design data. The torque capacity of a disk clutch is given by $\hat{T} = 0.5$ *if* $F_a D_m$, where *T* is the torque, *i* the number of pairs of contact surfaces, f the applicable coefficient of friction, F_a the axial

Fig. 8.2.52 Cone clutch.

engaging force, and D_m the mean diameter of the clutch facing. The spring forces holding a disk clutch in engagement are usually of relatively high value, as given by the allowable contact pressures. In order to lower the force required at the operating lever, elaborate linkages are required, usually having lever ratios in the range of 10 to 12. As these linkages must rotate with the clutch, they must be adequately balanced and the effect of centrifugal forces must be considered. Disk clutches are often run wet, either immersed in oil or in a spray. The advantages are reduced wear, smoother action, and lower operating temperatures. Disk clutches are often operated automatically by either air or hydraulic cylinders as, for examples, in automobile automatic transmissions.

Fig. 8.2.53 Multidisk clutch.

Fig. 8.2.55 Overrunning clutch.

SOURCE: Maleev, *Machine Design,* International Textbook, by permission.

HYDRAULIC POWER TRANSMISSION 8-39

Rim clutches may be subdivided into two groups: (1) those employing either a band or block [\(Fig. 8.2.54\)](#page-37-0) in contact with the rim and (2) overrunning clutches [\(Fig. 8.2.55\)](#page-37-0) employing the wedging action of a roller or sprag. Clutches in the second category will automatically engage in one direction and freewheel in the other.

HYDRAULIC POWER TRANSMISSION

Hydraulic power transmission systems comprise machinery and auxiliary components which function to generate, transmit, control, and utilize hydraulic power. The **working fluid,** a pressurized incompressible liquid, is usually either a petroleum base or a fire-resistant type. The latter are water and oil emulsions, glycol-water mixtures, or synthetic liquids such as silicones or phosphate esters.

Liquid is pressurized in a **pump** by virtue of its resistance to flow; the pressure difference between pump inlet and outlet results in flow. Most hydraulic applications employ positive-displacement pumps of the gear, vane, screw, or piston type; piston pumps are axial, radial, or reciprocating (see Sec. 14).

Power is transmitted from pump to controls and point of application through a combination of **conduit and fittings** appropriate to the particular application. Flow characteristics of hydraulic circuits take into account fluid properties, pressure drop, flow rate, and pressure-surging tendencies. Conduit systems must be designed to minimize changes in flow velocity, velocity distribution, and random fluid eddies, all of which dissipate energy and result in pressure drops in the circuit (see Sec. 3). Pipe, tubing, and flexible hose are used as hydraulic power conduits; suitable fittings are available for all types and for transition from one type to another.

Controls are generally interposed along the conduit between the pump and point of application (i.e., an actuator or motor), and act to control pressure, volume, or flow direction.

Fig. 8.2.56 Relief valve.

Fig. 8.2.57 Reducing valve.

Pressure control valves, of which an ordinary safety valve is a common type (normally closed), include relief and reducing valves and pressure switches (Figs. 8.2.56 and 8.2.57). Pressure valves, normally closed, can be used to control sequential operations in a hydraulic circuit. **Flow control valves** throttle flow to or bypass flow around the unit being controlled, resulting in pressure drop and temperature increase as pressure energy is dissipated. Figure 8.2.58 shows a simple needle valve with variable orifice usable as a flow control valve. **Directional control valves** serve primarily to direct hydraulic fluid to the point of application. Directional control valves with rotary and sliding spools are shown in Figs. 8.2.59 and 8.2.60.

Fig. 8.2.58 Needle valve.

Fig. 8.2.59 Rotary-spool directional flow valve.

| 7///2 | \$ 绕绕: | |
|-------|--------|--|

Fig. 8.2.60 Sliding-spool directional flow valve.

A poppet (valve) mechanism is shown in Fig. 8.2.61, a diaphragm valve in Fig. 8.2.62, and a shear valve in Fig. 8.2.63.

Accumulators are effectively ''hydraulic flywheels'' which store potential energy by accumulating a quantity of pressurized hydraulic fluid

Fig. 8.2.61 Poppet valve.

in a suitable enclosed vessel. The bag type shown i[n Fig. 8.2.64](#page-39-0) uses pressurized gas inside the bag working against the hydraulic fluid outside the bag[. Figure 8.2.65 s](#page-39-0)hows a piston accumulator.

Pressurized hydraulic fluid acting against an **actuator** or motor converts fluid pressure energy into mechanical energy. Motors providing

continuous rotation have operating characteristics closely related to their pump counterparts. A linear actuator, or cylinder [\(Fig. 8.2.66\)](#page-39-0), provides straight-line reciprocating motion; a rotary actuator [\(Fig.](#page-39-0) [8.2.67\)](#page-39-0) provides arcuate oscillatory moti[on. Figure 8.2.](#page-39-0)68 shows a oneshot booster (linear motion) which can be used to deliver sprays through a nozzle.

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Hydraulic fluids (liquids and air) are conducted in **pipe, tubing,** or **flexible hose.** Hose is used when the lines must flex or in applications in which fixed, rigid conduit is unsuitable. Table 8.2.37 lists SAE standard hoses. Maximum recommended operating pressure for a broad range of

Fig. 8.2.64 Bag accumulator.

industrial applications is approximately 25 percent of rated bursting pressure. Due consideration must be given to the operating-temperature range; most applications fall in the range from -40 to 200°F $(-40 \text{ to } 95^{\circ}$ C). Higher operating temperatures can be accommodated with appropriate materials.

Hose fittings are of the screw-type or swaged, depending on the particular application and operating pressure and temperature. A broad variety of hose-end fittings is available from the industry.

Pipe has the advantage of being relatively cheap, is applied mainly in straight

runs, and is usually of steel. Fittings for pipe are either standard pipe fittings for fairly low pressures or more elaborate ones suited to leakproof high-pressure operation.

Fig. 8.2.65 Piston accumulator.

Fig. 8.2.66 Linear actuator or hydraulic cylinder.

Tubing is more easily bent into neat forms to fit between inlet and outlet connections. Steel and stainless-steel tubing is used for the highest-pressure applications; aluminum, plastic, and copper tubing is also used as appropriate for the operating conditions of pressure and temperature. Copper tubing hastens the oxidation of oil-base hydraulic fluids; accordingly, its use should be restricted either to air lines or with liquids which will not be affected by copper in the operating range.

Vane and seal

Fig. 8.2.67 Rotary actuator.

Fig. 8.2.68 One-shot booster.

Table 8.2.37 SAE Standard Hoses

Tube fittings for permanent connections allow for brazed or welded joints. For temporary or separable applications, **flared** or **flareless fittings** are employed (Figs. $8.2.69$ and $8.2.70$). ANSI B116.1-1974 and B116.2-1974 pertain to tube fittings. The variety of fittings available is vast; the designer is advised to refer to manufacturers' literature for specifics.

Fig. 8.2.69 Flared tube fittings. (*a*) A 45° flared fitting; (*b*) Triple-lok flared fitting. *(Parker-Hannafin Co.)*

Fig. 8.2.70 Ferulok flareless tube fitting. *(Parker-Hannafin Co.)*

Parameters entering into the design of a hydraulic system are volume of flow per unit time, operating pressure and temperature, viscosity characteristics of the fluid within the operating range, and compatibility of the fluid/conduit material.

Flow velocity in suction lines is generally in the range of 1 to 5 ft/s (0.3 to 1.5 m/s); in discharge lines it ranges from 10 to 25 ft/s $(3 \text{ to } 8 \text{ m/s})$.

The pipe or tubing is under internal pressure. Selection of material and wall thickness follows from suitable equations (see Sec. 5). Safety factors range from 6 to 10 or higher, depending on the severity of the application (i.e., vibration, shock, pressure surges, possibility of physical abuse, etc.). JIC specifications provide a guide to the designer of hydraulic systems.

BRAKES

Brakes may be classified as: (1) rim type—internally expanding or externally contracting shoes, (2) band type, (3) cone type, (4) disk or axial type, (5) miscellaneous.

Rim Type—Internal Shoe(s) [\(Fig. 8.2.71\)](#page-40-0)

$$
F = \begin{cases} \frac{M_N - M\mu}{d} \\ \frac{M_N + M\mu}{d} \end{cases}
$$

clockwise rotation

counterclockwise rotation

where

$$
M\mu = \frac{\mu P_a Br}{\sin \theta_a} \int_{\theta_1}^{\theta_2} (\sin \theta)(r - d \cos \theta) d\theta
$$

 $B =$ face width of frictional material; $P_a =$ maximum pressure; θ_a = angle to point of maximum pressure (if $\theta_2 > 90^\circ$; then $\theta_a = 90^\circ$; $\ddot{\theta_2}$ < 90°, then $\dot{\theta}_a = \theta_2$); μ = coefficient of friction; *r* = radius of drum; $d =$ distance from drum center to brake pivot;

$$
M_N = \frac{P_a B r d}{\sin \theta_a} \int_{\theta_1}^{\theta_2} \sin^2 \theta \, d\theta
$$

and torque on drum is

$$
T = \frac{\mu P_a B r^2 (\cos \theta_1 - \cos \theta_2)}{\sin \theta_a}
$$

Self-locking of the brake $(F = 0)$ will occur for clockwise rotation when $M_N = M\mu$. This self-energizing phenomenon can be used to advantage without actual locking if μ is replaced by a larger value μ' so that 1.25 $\mu \leq \mu' \leq 1.50$, from which the pivot position *a* can be solved.

Fig. 8.2.71 Rim brake: internal friction shoe.

In automative use there are two shoes made to pivot in opposition, so that self-energization is present and can be used to great advantage (Fig. 8.2.72).

Fig. 8.2.72 Internal brake.

Rim Type—External Shoe(s) (Fig. 8.2.73)

The equations for M_N and $M\mu$ are the same as above:

$$
F = \begin{cases} \frac{M_N + M\mu}{d} & \text{clockwise rotation} \\ \frac{M_N - M\mu}{d} & \text{counterclockwise rotation} \end{cases}
$$

Self-locking $(F = 0)$ can occur for counterclockwise rotation at $M_N = M\mu$.

Fig. 8.2.73 Rim brake: external friction shoe.

Band Type (Fig. 8.2.74*a*, *b*, and *c*)

Flexible band brakes are used in power excavators and in hoisting. The bands are usually of an asbestos fabric, sometimes reinforced with copper wire and impregnated with asphalt.

In Fig. 8.2.74*a*, $F =$ force at end of brake handle; $P =$ tangential force at rim of wheel; $f =$ coefficient of friction of materials in contact;

Fig. 8.2.74 Band brakes.

 $a =$ angle of wrap of band, deg; $T_1 =$ total tension in band on tight side; T_2 = total tension in band on slack side. Then $T_1 - T_2 = P$ and $T_1 / T_2 = 10^{0.0076fa} = 10^b$, where $b = 0.0076fa$. Also, $T_2 = P/(10^b-1)$ and $T_1 = P \times 10^{b} / (10^{b} - 1)$. The values of $10^{0.0076fa}$ are given in [Fig. 8.2.90](#page-52-0) for *a* in radians.

For the arrangement shown in Fig. 8.2.74*a*,

and
$$
FA = T_2B = PB/(10^b - 1)
$$

 $F = PB/[A(10^b - 1)]$

For the construction illustrated in Fig. 8.2.74*b*,

$$
F = PB / \{A[10^b / (10^b - 1)]\}
$$

For the differential brake shown in Fig. 8.2.74*c*,

$$
F = (P/A)[(B_2 - 10^b B_1)/(10^b - 1)]
$$

In this arrangement, the quantity $10^bB₁$ must always be less than $B₂$, or the band will grip the wheel and the brake, or part of the mechanism to which it is attached, will rupture.

It is usual in practice to have the leverage ratio *A*/*B* for band brakes about 10 : 1.

If *f* for wood on iron is taken at 0.3 and the angle of wrap for the band is 270 $^{\circ}$, i.e., subtends three-fourths of the circumference, then $10^b = 4$ approx; the loads required for a given torque will be as follows for the cases just considered and for the leverage ratios stated above:

In the case of Fig. 8.2.74*c*, the dimension B_2 must be greater than $B_1 \times 10^b$. Accordingly, B_1 is taken as $\frac{1}{4}$, *A* as 10, and, since $10^b = 4$, B_2 is taken as $1\frac{1}{2}$.

The principal function of a brake is to absorb energy. This energy appears at the surface of the brake as heat, which must be carried away

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at a sufficiently rapid rate to prevent burning of the wooden blocks. Suitable proportions may be arrived at as follows:

Let $p =$ unit pressure on brake surface, $lb/in^2 = R$ (reaction against block)/area of block; $v =$ velocity of brake rim surface, ft/s = $2\pi rn/60$, where $n =$ speed of brake wheel, r/min. Then $pv =$ work absorbed per in² of brake surface per second, and $pv \le 1,000$ for intermittent applications of load with comparatively long periods of rest and poor means for carrying away heat (wooden blocks); $pv \le 500$ for continuous application of load and poor means for carrying away heat (wooden blocks); $pv \leq 1,400$ for continuous application of load with effective means for carrying away heat (oil bath).

Cone Brake (see Fig. 8.2.75)

Uniform Wear

$$
F = \frac{\pi P_a d}{2} (D - d)
$$

$$
T = \frac{\pi \mu P_a d}{8 \sin \alpha} (D^2 - d)
$$

where P_a = maximum pressure occurring at $d/2$.

Fig. 8.2.75 Cone break.

Figure 8.2.76 shows a cone brake arrangement used for lowering heavy loads.

Fig. 8.2.76 Cone brake for lowering loads.

Disk Brakes (see Fig. 8.2.77)

Disk brakes are free from ''centrifugal'' effects, can have large frictional areas contained in small space, have better heat dissipation qualities than the rim type, and enjoy a favorable pressure distribution. **Uniform Wear**

$$
F = \frac{\pi P_a d}{2} (D - d)
$$

$$
T = \frac{F\mu}{4} (D + d)
$$

Uniform Pressure

$$
F = \frac{\pi P_a}{4} (D^2 - d^2)
$$

$$
T = \frac{F\mu}{3} \times \frac{D^3 - d^3}{D^2 - d^2}
$$

These relations apply to a single surface of contact. For caliper disk, or multidisk brakes, the above relations are applied for each surface of contact.

Fig. 8.2.77 Disk brake.

Selected friction materials and properties are listed i[n Table 8.2.38.](#page-42-0) Frequently disk brakes are made as shown in Fig. 8.2.78. The pinion *Q* engages the gear in the drum (not shown). When the load is to be raised, power is applied through the gear and the connection between *B* and *C* is accomplished by the advancing of *B* along *A* and the clamping of the friction disks *D* and *D* and the ratchet wheel *E*. The reversal of the motor disconnects *B* and *C*. In lowering the load, only as much reversal of rotation of the gear is given as is needed to reduce the force in the friction disks so that the load may be lowered under control.

Fig. 8.2.78 Disk brake.

A **multidisk brake** is shown in Fig. 8.2.79. This type of construction results in an increase in the number of friction faces. The drum shaft is geared to the pinion *A*, while the motive power for driving comes through the gear *G*. In raising the load, direct connection is had between *G, B,* and *A*. In lowering, *B* moves relatively to *G* and forces the friction plates together, those plates fast to *E* being held stationary by the pawl on *E*. In the figure, there are three plates fast to *E*, one fast to *G*, and one fast to *C*.

Fig. 8.2.79 Multidisk brake.

Eddy-current brakes [\(Fig. 8.2.80\)](#page-42-0) are used with flywheels where quick braking is essential, and where large kinetic energy of the rotating

SHRINK, PRESS, DRIVE, AND RUNNING FITS 8-43

Table 8.2.38 Selected Friction Materials and Properties

masses precludes the use of block brakes due to excessive heating, as in reversible rolling mills. A number of poles *a* are electrically excited (north and south in turn) and create a magnetic flux which permeates the gap and the iron of the rim, causing eddy current. The flywheel energy

Fig. 8.2.80 Eddy-current brake.

is converted through these currents into heat. The hand brake *b* may be used for quicker stopping when the speed of the wheel is considerably decreased; i.e., when the eddy-current brake is inefficient. Two brakes are provided to avoid bending forces on the shaft.

Electric brakes are often used in cranes, bridges, turntables, and machine tools, where an automatic application of the brake is important as soon as power is cut off. The brake force is supplied by an adjustable spring which is counteracted by the force of a solenoid or a centrifugal thrustor. Interruption of current automatically applies the springactivated brake shoes. Figures 8.2.81 and 8.2.82 show these types of electric brake.

Fig. 8.2.81 Solenoid-type electric brake.

Fig. 8.2.82 Thrustor-type electric brake.

SHRINK, PRESS, DRIVE, AND RUNNING FITS

Inch Systems ANSI B4.1-1967 (R87) recommends preferred sizes, allowances, and tolerances for fits between plain cylindrical parts. Such fits include bearing, shrink and drive fits, etc. Terms used in describing fits are defined as follows: **Allowance:** minimum clearance (positive allowance) or maximum interference (negative allowance) between mating parts. **Tolerance:** total permissible variation of size. **Limits of size:** applicable maximum and minimum sizes. **Clearance fit:** one having limits of size so prescribed that a clearance always results when mating parts are assembled. **Interference fit:** In this case, limits are so prescribed that interference always results on assembly. **Transition fit:** This may have either a clearance or an interference on assembly. **Basic size:** one from which limits of size are derived by the application of allowances and tolerances. **Unilateral tolerance:** In this case a variation in size is permitted in only one direction from the basic size.

Fits are divided into the following general classifications: (1) running and sliding fits, (2) locational clearance fits, (3) transition fits, (4) locational interference fits, and (5) force or shrink fits.

1. **Running and sliding fits.** These are intended to provide similar running performance with suitable lubrication allowance throughout the range of sizes. These fits are further subdivided into the following classes:

Class RC1: close-sliding fits. Intended for accurate location of parts which must assemble without perceptible play.

Class RC2: sliding fits. Parts made with this fit move and turn easily but are not intended to run freely; also, in larger sizes they may seize under small temperature changes.

Class RC3: precision-running fits. These are intended for precision work at slow speeds and light journal pressures but are not suitable where appreciable temperature differences are encountered.

Class RC4: close-running fits. For running fits on accurate machinery with moderate surface speeds and journal pressures, where accurate location and minimum play is desired.

Classes RC5 and RC6: medium-running fits. For higher running speeds or heavy journal pressures.

Class RC7: free-running fits. For use where accuracy is not essential, or where large temperature variations are likely to be present, or both.

Classes RC8 and RC9: loose-running fits. For use with materials such as cold-rolled shafting or tubing made to commercial tolerances.

Limits of clearance given in ANSI B4.1-1967 (R87) for each of these classes are given i[n Table 8.2.39.](#page-43-0) Hole and shaft tolerances are listed on a unilateral tolerance basis in this reference to give the clearance limits o[f Table 8.2.39,](#page-43-0) the hole size being the basic size.

2. **Locational clearance fits.** These are intended for normally stationary parts which can, however, be freely assembled or disassembled. These are subdivided into various classes which run from snug fits for parts requiring accuracy of location, through medium clearance fits (spigots) to the looser fastener fits where freedom of assembly is of prime importance.

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Table 8.2.39 Limits of Clearance for Running and Sliding Fits (Basic Hole) (Limits are in thousandths of an inch on diameter)

| Nominal size | | Class | | | | | | | | | | | | |
|---------------|------|-------|------|-----|-----|-----------------|------|------|------|--|--|--|--|--|
| range, in | RC1 | RC2 | RC3 | RC4 | RC5 | RC ₆ | RC7 | RC8 | RC9 | | | | | |
| $0 - 0.12$ | 0.1 | 0.1 | 0.3 | 0.3 | 0.6 | 0.6 | 1.0 | 2.5 | 4.0 | | | | | |
| | 0.45 | 0.55 | 0.95 | 1.3 | 1.6 | 2.2 | 2.6 | 5.1 | 8.1 | | | | | |
| $0.12 - 0.24$ | 1.5 | 0.15 | 0.4 | 0.4 | 0.8 | 0.8 | 1.2 | 2.8 | 4.5 | | | | | |
| | 0.5 | 0.65 | 1.2 | 1.6 | 2.0 | 2.7 | 3.1 | 5.8 | 9.0 | | | | | |
| $0.24 - 0.40$ | 0.2 | 0.2 | 0.5 | 0.5 | 1.0 | 1.0 | 1.6 | 3.0 | 5.0 | | | | | |
| | 0.6 | 0.85 | 1.5 | 2.0 | 2.5 | 3.3 | 3.9 | 6.6 | 10.7 | | | | | |
| $0.40 - 0.71$ | 0.25 | 0.25 | 0.6 | 0.6 | 1.2 | 1.2 | 2.0 | 3.5 | 6.0 | | | | | |
| | 0.75 | 0.95 | 1.7 | 2.3 | 2.9 | 3.8 | 4.6 | 7.9 | 12.8 | | | | | |
| $0.71 - 1.19$ | 0.3 | 0.3 | 0.8 | 0.8 | 1.6 | 1.6 | 2.5 | 4.5 | 7.0 | | | | | |
| | 0.95 | 1.2 | 2.1 | 2.8 | 3.6 | 4.8 | 5.7 | 10.0 | 15.5 | | | | | |
| $1.19 - 1.97$ | 0.4 | 0.4 | 1.0 | 1.0 | 2.0 | 2.0 | 3.0 | 5.0 | 8.0 | | | | | |
| | 1.1 | 1.4 | 2.6 | 3.6 | 4.6 | 6.1 | 7.1 | 11.5 | 18.0 | | | | | |
| $1.97 - 3.15$ | 0.4 | 0.4 | 1.2 | 1.2 | 2.5 | 2.5 | 4.0 | 6.0 | 9.0 | | | | | |
| | 1.2 | 1.6 | 3.1 | 4.2 | 5.5 | 7.3 | 8.8 | 13.5 | 20.5 | | | | | |
| $3.15 - 4.73$ | 0.5 | 0.5 | 1.4 | 1.4 | 3.0 | 3.0 | 5.0 | 7.0 | 10.0 | | | | | |
| | 1.5 | 2.0 | 3.7 | 5.0 | 6.6 | 8.7 | 10.7 | 15.5 | 24.0 | | | | | |

3. **Transition fits.** These are for applications where accuracy of location is important, but a small amount of either clearance or interference is permissible.

4. **Locational interference fits.** Used where accuracy of location is of prime importance and for parts requiring rigidity and alignment with no special requirements for bore pressure.

Data on clearance limits, interference limits, and hole and shaft diameter tolerances for locational clearance fits, transition fits, and locational interference fits are given in ANSI B4.1-1967 (R87).

5. **Force or shrink fits.** These are characterized by approximately constant bore pressures throughout the range of sizes; interference varies almost directly as the diameter, and the differences between maximum and minimum values of interference are small. These are divided into the following classes:

Class FN1: light-drive fits. For applications requiring light assembly pressures (thin sections, long fits, cast-iron external members).

Class FN2: medium-drive fits. Suitable for ordinary steel parts or for shrink fits on light sections. These are about the tightest fits that can be used on high-grade cast-iron external members.

Class FN3: heavy-drive fits. For heavier steel parts or shrink fits in medium sections.

Classes FN4 and FN5: force fits. These are suitable for parts which can be highly stressed. Shrink fits are used instead of press fits in cases where the heavy pressing forces required for mounting are impractical.

In Table 8.2.40 are listed the limits of interference (maximum and minimum values) for the above classes of force or shrink fits for various diameters, as given in ANSI B4.1-1967 (R87). Hole and shaft tolerances to give these interference limits are also listed in this reference.

Metric System ANSI B4.2-1978 (R94) and ANSI B4.3-1978 (R94) define limits and fits for cylindrical parts, and provide tables listing preferred values.

The standard ANSI B4.2-1978 (R94) is essentially in accord with ISO R286.

ANSI B4.2 provides 22 basic deviations, each for the shaft (a to z plus js), and the hole (A to Z plus Js). International has 18 tolerance grades: IT 01, IT 0, and IT 1 through 16.

IT grades are roughly applied as follows: measuring tools, 01 to 7; fits, 5 to 11; material, 8 to 14; and large manufacturing tolerances, 12 to 16. Se[e Table 8.2.42](#page-44-0) for metric preferred fits.

Basic size—The basic size is the same for both members of a fit, and is the size to which limits or deviations are assigned. It is designated by 40 in 40H7.

Table 8.2.40 Limits of Interference for Force and Shrink Fits (Limits are in thousandths of an inch on diameter)

Deviation—The algebraic difference between a size and the corresponding basic size.

Upper deviation—The algebraic difference between the maximum limit of size and the corresponding basic size.

Lower deviation—The algebraic difference between the minimum limit of size and the corresponding basic size.

Fundamental deviation—That one of the two deviations closest to the basic size. It is designated by the letter H in 40H7.

Tolerance—The difference between the maximum and minimum size limits on a part.

International tolerance grade (IT)—A group of tolerances which vary depending on the basic size, but which provide the same relative level of accuracy within a grade. It is designated by 7 in 40H7 (IT 7).

Tolerance zone—A zone representing the tolerance and its position in relation to the basic size. The symbol consists of the fundamental deviation letter and the tolerance grade number (i.e., H7).

Hole basis—The system of fits where the minimum hole size is basic. The fundamental deviation for a hole basis system is H.

Shaft basis—Maximum shaft size is basic in this system. Fundamental deviation is h. NOTE: Capital letters refer to the hole and lowercase letters to the shaft.

Clearance fit—A fit in which there is clearance in the assembly for all tolerance conditions.

Interference fit—A fit in which there is interference for all tolerance conditions. Table 8.2.41 lists preferred metric sizes. Table 8.2.42 lists preferred tolerance zone combinations for clearance, transition and interference fits[. Table 8.2.43](#page-45-0) lists dimensions for the grades corresponding to preferred fits. [Table 8.2.44](#page-47-0)*a* and *b* lists limits (numerical) of preferred hole-basis clearance, transitions, and interference fits.

Stresses Produced by Shrink or Press Fit

STEEL HUB ON STEEL SHAFT. The maximum equivalent stress, pounds per square inch, set up by a given press-fit allowance (in inches per inch of shaft diameter) is equal to $3x \times 10^7$, where *x* is the allowance per inch of shaft diameter (Baugher, *Trans. ASME,* 1931, p. 85). The press-fit pressures set up between a steel hub and shaft, for various ratios *d/D* between shaft and hub outside diameters, are given i[n Fig. 8.2.83.](#page-45-0) These

SOURCE: ANSI B 4.2-1978 (R94), reproduced by permission.

curves are accurate to 5 percent even if the shaft is hollow, provided the inside shaft diameter is not over 25 percent of the outside. The equivalent stress given above is based on the maximum shear theory and is numerically equal to the radial-fit pressure added to the tangential tension in the hub. Where the shaft is hollow, with an inside diameter equal to more than about 25 percent of the outside diameter, the allowance in inches per inch to obtain an equivalent hub stress of 30,000 lb/in2 may be determined by using Lamé's thick-cylinder formulas (*Jour. Appl.*

Transition fit for basic sizes in range from 0 through 3 mm.

SOURCE: ANSI B4.2-1978 (R94), reproduced by permission.

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Table 8.2.43 International Tolerance Grades

| Basic sizes | | | | | | | | | |
|--------------------|----------------|----------------------|-------|-----------------|-----------------|-------------|-------|--|--|
| | Up to and | Tolerance grades, mm | | | | | | | |
| Over | including | IT ₆ | IT7 | IT ₈ | IT ₉ | IT10 | IT11 | | |
| $\mathbf{0}$ | 3 | 0.006 | 0.010 | 0.014 | 0.025 | 0.040 | 0.060 | | |
| 3 | 6 | 0.008 | 0.012 | 0.018 | 0.030 | 0.048 | 0.075 | | |
| 6 | 10 | 0.009 | 0.015 | 0.022 | 0.036 | 0.058 | 0.090 | | |
| 10 | 18 | 0.011 | 0.018 | 0.027 | 0.043 | 0.070 | 0.110 | | |
| 18 | 30 | 0.013 | 0.021 | 0.033 | 0.052 | 0.084 | 0.130 | | |
| 30 | 50 | 0.016 | 0.025 | 0.039 | 0.062 | 0.100 | 0.160 | | |
| 50 | 80 | 0.019 | 0.030 | 0.046 | 0.074 | 0.120 | 0.190 | | |
| 80 | 120 | 0.022 | 0.035 | 0.054 | 0.087 | 0.140 | 0.220 | | |
| 120 | 180 | 0.025 | 0.040 | 0.063 | 0.100 | 0.160 | 0.250 | | |
| 180 | 250 | 0.029 | 0.046 | 0.072 | 0.115 | 0.185 | 0.290 | | |
| 250 | 315 | 0.032 | 0.052 | 0.081 | 0.130 | 0.210 | 0.320 | | |
| 315 | 400 | 0.036 | 0.057 | 0.089 | 0.140 | 0.230 | 0.360 | | |
| 400 | 500 | 0.040 | 0.063 | 0.097 | 0.155 | 0.250 | 0.400 | | |
| 500 | 630 | 0.044 | 0.070 | 0.110 | 0.175 | 0.280 | 0.440 | | |
| 630 | 800 | 0.050 | 0.080 | 0.125 | 0.200 | 0.320 | 0.500 | | |
| 800 | 1,000 | 0.056 | 0.090 | 0.140 | 0.230 | 0.360 | 0.560 | | |
| 1,000 | 1,250 | 0.066 | 0.105 | 0.165 | 0.260 | 0.420 | 0.660 | | |
| 1,250 | 1,600 | 0.078 | 0.125 | 0.195 | 0.310 | 0.500 | 0.780 | | |
| 1,600 | 2,000 | 0.092 | 0.150 | 0.230 | 0.370 | 0.600 | 0.920 | | |
| 2,000 | 2,500 | 0.110 | 0.175 | 0.280 | 0.440 | 0.700 | 1.100 | | |
| 2,500 | 3,150 | 0.135 | 0.210 | 0.330 | 0.540 | 0.860 | 1.350 | | |

SOURCE: ANSI B4.2-1978 (R94), reproduced by permission.

Mech., 1937, p. A-185). It should be noted that these curves hold only when the maximum equivalent stress is below the yield point; above the yield point, plastic flow occurs and the stresses are less than calculated.

Fig. 8.2.83 Press-fit pressures between steel hub and shaft.

Cast-Iron Hub on Steel Shaft Where the shaft is solid, or hollow with an inside diameter not over 25 percent of the outside diameter, Fig. 8.2.84 may be used to determine maximum tensile stresses in the castiron hub, resulting from the press-fit allowance; for various ratios *d/D*, Fig. 8.2.85 gives the press-fit pressures. These curves are based on a modulus of elasticity of 30×10^6 lb/in² for steel and 15×10^6 for cast iron. For a hollow shaft with an inside diameter more than about 1⁄4 the outside, the Lamé formulas may be used.

Pressure Required in Making Press Fits The force required to press a hub on the shaft is given by $\pi f p dl$, where *l* is length of fit, *p* the unit press-fit pressure between shaft and hub, *f* the coefficient of friction, and *d* the shaft diameter. Values of *f* varying from 0.03 to 0.33 have been reported, the lower values being due to yielding of the hub as a consequence of too high a fit allowance; the average is around 0.10 to 0.15. (For additional data see Horger and Nelson, ''Design Data and Methods,'' ASME, 1953, pp. 87–91.)

Fig. 8.2.84 Variation of tensile stress in cast-iron hub in press-fit allowance.

Fig. 8.2.85 Press-fit pressures between cast-iron hub and shaft.

Torsional Holding Ability The torque required to cause complete slippage of a press fit is given by $T = \frac{1}{2} \pi f p l d^2$. Local slippage will usually occur near the end of the fit at much lower torques. If the torque is alternating, stress concentration and rubbing corrosion will occur at the hub face so that, eventually, fatigue failure may occur at considerably lower torques. Only in cases of static torque application is it justifiable to use ultimate torque as a basis for design.

A designer can often improve shrink-, press-, and slip-fit cylindrical assemblies with adhesives. When applied, adhesives can achieve high frictional force with attendant greater torque transmission without extra bulk, and thus augment or even replace press fits, compensate for differential thermal expansion, make fits with leakproof seals, eliminate backlash and clearance, etc.

The adhesives used are the anaerobic (see Sec. 6.8, ''Adhesives'') variety, such as Loctite products. Such adhesives destabilize and tend to harden when deprived of oxygen. Design suggestions on the use of such adhesives appear in industrial catalogs.

SHAFTS, AXLES, AND CRANKS

Most shafts are subject to combined bending and torsion, either of which may be steady or variable. Impact conditions, such as sudden starting and stopping, will cause momentary peak stresses greater than those related to the steady or variable portions of operation.

Design of shafts requires a theory of failure to express a stress in terms of loads and shaft dimensions, and an allowable stress as fixed by material strength and safety factor. Maximum shear theory of failure and distortion energy theory of failure are the two most commonly used in shaft design. Material strengths can be estimated from any one of several analytic representations of combined-load fatigue test data, starting from the linear (Soderberg, modified Goodman) which tend to give conservative designs to the nonlinear (Gerber parabolic, quadratic, Kececioglu, Bagci) which tend to give less conservative designs.

When linear representations of material strengths are used, and where both bending and torsion stresses have steady and variable components, the maximum shear theory and the distortion energy theory lead to

somewhat similar formulations:
\n
$$
d = \left\{ \varepsilon \frac{n}{\pi} \left[\left(\frac{T_a}{S_{se}} + \frac{T_m}{S_{sy}} \right)^2 + \left(\frac{M_a}{S_{se}} + \frac{M_m}{S_{sy}} \right)^2 \right]^{1/2} \right\}^{1/3}
$$

where $\varepsilon = 32$ (maximum shear theory) or 48 (distortion energy theory); $d =$ shaft diameter; $n =$ safety factor; $T_a =$ amplitude torque $= (T_{\text{max}}$ T_{\min})/2; T_m = mean torque = $(T_{\max} + T_{\min})/2$; M_a = amplitude bending moment = $(M_{\text{max}} - M_{\text{min}})/2$; M_m = mean bending moment = $(M_{\text{max}} +$ $M_{\text{min}}/2$; S_{sy} = yield point in shear; S_{se} = completely corrected shear endurance limit = $S_{se}^{'}k_{a}k_{b}k_{c}k_{d}/K_{f}$; $S_{se}^{'}$ = statistical average endurance limit of mirror finish, standard size, laboratory test specimen at standard room temperature; k_a = surface factor, a decimal to adjust S'_e for other than mirror finish; k_b = size factor, a decimal to adjust S'_e for other than standard test size; k_c = reliability factor, a decimal to adjust S'_{se} to other than its implied statistical average of 50 percent safe, 50 percent fail rate (50 percent reliability); k_d = temperature factor, decimal, to adjust S'_{se} to other than room temperature; $K_f = 1 + q(K_f - 1) =$ actual or fatigue stress concentration factor, a number greater than unity to adjust the nominal stress implied by T_a and M_a to a peak stress as induced by stress-raising conditions such as holes, fillets, keyways, press fits, etc. (K_f for T_a need not necessarily be the same as K_f for M_a); $q =$ notch sensitivity; K_t = theoretical or geometric stress concentration factor.

For specific values of endurance limits and various factors the reader is referred to the technical literature (e.g., ASTM, NASA technical reports, ASME technical papers) or various books [e.g., ''Machinery's Handbook'' (Industrial Press, New York) and machine design textbooks].

If one allows for a variation of at least 15 percent, the following approximation is useful for the endurance limit in bending: $S_e' = 0.5S_{ui}$. This becomes for maximum shear theory $S'_{se} = 0.5(0.5S_{ut})$ and for distortion energy theory $S'_{se} = 0.577(0.5S_{ut})$.

Representative or approximate values for the various factors mentioned above were abstracted from Shigley, ''Mechanical Engineering Design,'' McGraw-Hill, and appear below with permission.

Surface Factor *ka*

Size Factor *kb*

$$
k_b = \begin{cases} 0.869d^{-0.097} & 0.3 \text{ in} < d \le 10 \text{ in} \\ 1 & d \le 0.3 \text{ in or } d \le 8 \text{ mm} \\ 1.189d^{-0.097} & 8 \text{ mm} < d < 250 \text{ mm} \end{cases}
$$

Reliability Factor *kc*

Temperature Factor k_d

Notch Sensitivity *q*

Se[e Table 8.2.45](#page-49-0) for fatigue stress concentration factors for plain press fits.

A general representation of material strengths (Marin, Design for Fatigue Loading, *Mach. Des.* **29,** no. 4, Feb. 21, 1957, pp. 128–131, and

series of the same title) is given as
\n
$$
\left(\frac{S_a}{S_e}\right)^m + \left(\frac{K S_m}{S_{ut}}\right)^p = 1
$$

where S_a = variable portion of material strength; S_m = mean portion of material strength; $\overline{S_e}$ = adjusted endurance limit; S_{ut} = ultimate strength[. Table 8.2.46](#page-49-0) lists the constants *m, K,* and *P* for various failure criteria.

For purposes of design, safety factors are introduced into the equation resulting in: $\overline{\left(\right. }$ $\frac{\sigma'_{a,p}}{S_e/n_{se}}$ $+$ $($ $\frac{K\,\sigma_{m,p}^\prime}{S_{ut}^{}/n_{ut}^{}}\bigg)$

 $K\,\sigma_{m,p}^{\prime}$

 $P = 1$

m

 $\sigma^{\prime}_{a,p}$

where

$$
\sigma'_{a,p} = \frac{1}{\pi d^3} \sqrt{(32n_{Ma}M_a)^2 + 3(16n_{\tau a}T_a)^2}
$$

$$
\sigma'_{m,p} = \frac{1}{\pi d^3} \sqrt{(32n_{Mm}M_m)^2 + 3(16n_{\tau m}T_m)^2}
$$

and n_{ij} = safety factor pertaining to a particular stress (that is, n_a = safety factor for amplitude shear stress).

Stiffness of shafting may become important where critical speeds, vibration, etc., may occur. Also, the lack of sufficient stiffness in shafts may give rise to bearing troubles. Critical speeds of shafts in torsion or bending and shaft deflections may be calculated using the methods of Sec. 5. For shafts of variable diameter see Spotts, ''Design of Machine Elements,'' Prentice-Hall. In order to avoid trouble where sleeve bearings are used, the angular deflections at the bearings in general must be kept within certain limits. One rule is to make the shaft deflection over the bearing width equal to a small fraction of the oil-film thickness. Note that since stiffness is proportional to the modulus of elasticity, alloy-steel shafts are no stiffer than carbon-steel shafts of the same diameter.

Crankshafts For calculating the torsional stiffness of crankshafts, the formulas given in Sec. 5 may be used.

SHAFTS, AXLES, AND CRANKS 8-47

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8-50 MACHINE ELEMENTS

Marine-engine shafts and **diesel-engine crankshafts** should be designed not only for strength but for avoidance of critical speed. (See Applied Mechanics, *Trans. ASME,* **50,** no. 8, for methods of calculating critical speeds of diesel engines.)

Table 8.2.46 Constants for Use in $(S_a/S_e)^m + (KS_m/S_{ut})^p = 1$

| Failure theory | K | | m |
|----------------------|--|---|----|
| Soderberg | S_{ut}/S_{v} | | |
| Bagci | S_{ut}/S_{v} | | |
| Modified Goodman | | | |
| Gerber parabolic | | 2 | |
| Kececioglu | | 2 | m† |
| Quadratic (elliptic) | | 2 | |
| $\dagger m =$ | 0.8914 UNS G 10180 $H_R = 130$ 0.9266 UNS G 10380 $H_R = 164$ 1.0176 UNS G 41300 $H_R = 207$ 0.9685 UNS G 43400 $H_R = 233$ | | |

PULLEYS, SHEAVES, AND FLYWHEELS

Arms of pulleys, sheaves, and flywheels are subjected to stresses due to condition of founding, to details of construction (such as split or solid), and to conditions of service, which are difficult to analyze. For these reasons, no accurate stress relations can be established, and the following formulas must be understood to be only approximately correct. It has been established experimentally by Benjamin (*Am. Mach.,* Sept. 22, 1898) that thin-rim pulleys do not distribute equal loads to the several pulley arms. For these, it will be safe to assume the tangential force on the pulley rim as acting on half of the number of arms. Pulleys with comparatively thick rims, such as engine band wheels, have all the arms taking the load. Furthermore, while the stress action in the arms is similar to that in a beam fixed at both ends, the amount of restraint at the rim depending on the rim's elasticity, it may nevertheless be assumed for purposes of design that cantilever action is predominant. The bending moment at the hub in arms of thin-rim pulleys will be $M =$ *PL*/($\frac{1}{2}N$), where *M* = bending moment, in · lb; *P* = tangential load on the rim, lb; $L =$ length of the arm, in; and $N =$ number of arms. For thick-rim pulleys and flywheels, $M = PL/N$.

For arms of elliptical section having a width of two times the thickness, where $E =$ width of arm section at the rim, in, and $s_t =$ intensity of tensile stress, lb/in2

$$
E = \sqrt[3]{40PL/(s_tN)}
$$
 (thin rim) = $\sqrt[3]{20PL/(s_tN)}$ (thick rim)

For single-thickness belts, *P* may be taken as 50*B* lb and for doublethickness belts $P = 75B$ lb, where *B* is the width of pulley face, in. Then $E = k \times \sqrt[3]{BL/(s_rN)}$, where *k* has the following values: for thin rim, single belt, 13; thin rim, double belt, 15; thick rim, single belt, 10; thick rim, double belt, 12. For cast iron of good quality, s_t due to bending may be taken at 1,500 to 2,000. The arm section at the rim may be made from $\frac{2}{3}$ to $\frac{3}{4}$ the dimensions at the hub.

For high-speed pulleys and flywheels, it becomes necessary to check the arm for tension due to rim expansion. It will be safe to assume that each arm is in tension due to one-half the centrifugal force of that portion of the rim which it supports. That is, $T = As_t = Wv^2/(2NgR)$, lb, where $T =$ tension in arm, lb; $N =$ number of arms; $v =$ speed of rim, ft/s; $R =$ radius of pulley, ft; $A =$ area of arm section, in²; $W =$ weight of pulley rim, lb; and s_t = intensity of tensile stress in arm section, lb/in², whence $s_t = W R n^{2}/(6,800N)$, where $n = r/min$ of pulley.

Arms of flywheels having heavy rims may be subjected to severe stress action due to the inertia of the rim at sudden load changes. There being no means of predicting the probable maximum to which the inertia may rise, it will be safe to make the arms equal in strength to 3⁄4 of the shaft strength in torsion. Accordingly, for elliptical arm sections,

$$
N \times 0.5E^3 s_t = \frac{3}{4} \times 2s_s d^3 \qquad \text{or} \qquad E = 1.4d^3 \overline{s_s \langle s_t N \rangle}
$$

For steel shafts with $s_s = 8,000$ and cast-iron arms with $s = 1,500$,

$$
E = 2.4d/\sqrt[3]{N} = 1.3d
$$
 (for 6 arms) = 1.2d (for 8 arms)

where $2E =$ width of elliptical arm section at hub, in (thickness $= E$), and $d =$ shaft diameter, in.

Rims of belted pulleys cast whole may have the following proportions (see Fig. 8.2.86):

 $t_2 = \frac{3}{4}h + 0.005D$ $t_1 = 2t_2 + C$ $W = \frac{9}{8}B$ to $\frac{5}{4}B$

where $h =$ belt thickness, $C = \frac{1}{24}W$, and $B =$ belt width, all in inches.

Fig. 8.2.86 Rims for belted pulleys.

Engine band wheels, flywheels, and pulleys run at **high speeds** are subjected to the following stress actions in the rim:

Considering the rim as a free ring, i.e., without arm restraint, and made of cast iron or steel, $s_t = v^2/10$ (approx), where s_t = intensity of tensile stress, $1b/in^2$, and $v = rim$ speed, ft/s. For beam action between the arms of a solid rim, $M = P l/12$ (approx), where $M =$ bending moment in rim, in \cdot lb; *P* = centrifugal force of that portion of rim between arms, lb, and $l =$ length of rim between arms, in; from which $s_t = WR^2n^2/(450N^2Z)$, where $W =$ weight of entire rim, lb; $R =$ radius of wheel, ft; $n = r/min$ of wheel; and $Z =$ section modulus of rim section, in3. In case the rim section is of the forms shown in Fig. 8.2.86, care must be taken that the flanges do not reduce the section modulus from that of the rectangular section. For **split rims** fastened with bolts the stress analysis is as follows:

Let *w* = weight of rim portion, lb (with length L, in) lb; w_1 = weight of lug, lb; L_1 = lever arm of lug, in; and s_t = intensity of tensile stress lb/in² in rim section joining arm. Then $s_t = 0.00034n^2R(w_1L_1 + wL/2)/Z$, where $n = r/\text{min}$ of wheel; $R =$ wheel radius, ft; and $Z =$ section modulus of

rim section, in³. The above equation gives the value of s_t for bending when the bolts are loose, which is the worst possible condition that may arise. On this basis of analysis, s_t should not be greater than 8,000 lb/in². The stress due to bending in addition to the stress due to rim expansion as analyzed previously will be the probable maximum intensity of stress for which the rim should be checked for strength. The flange bolts, because of their position, do not materially relieve the bending action. In case a tie rod leads from the flange to the hub, it will be *safe* to consider it as an additional factor of safety. When the tie rod is kept tight, it very materially strengthens the rim.

A more accurate method for calculating maximum stresses due to centrifugal force in flywheels with arms cast integral with the rim is given by Timoshenko, ''Strength of Materials,'' Pt. II, 1941, p. 98. More exact equations for calculating stresses in the arms of flywheels and pulleys due to a combination of belt pull, centrifugal force, and changes in velocity are given by Heusinger, *Forschung,* 1938, p. 197. In both treatments, shrinkage stresses in the arms due to casting are neglected.

Large flywheels for high rim speeds and severe working conditions (as for rolling-mill service) have been made from flat-rolled steel plates with holes bored for the shaft. A group of such plates may be welded together by circumferential welds to form a large flywheel. By this means, the welds do not carry direct centrifugal loads, but serve merely to hold the parts in position. Flywheels up to 15-ft diam for rolling-mill service have been constructed in this way.

BELT DRIVES

Flat-Belt Drives

The primary drawback of flat belts is their reliance on belt tension to produce frictional grip over the pulleys. Such high tension can shorten bearing life. Also, tracking may be a problem. However, flat belts, being thin, are not subject to centrifugal loads and so work well over small pulleys at high speeds in ranges exceeding 9,000 ft/min. In light service flat belts can make effective clutching drives. Flat-belt drives have efficiencies of about 90 percent, which compares favorably to geared drives. Flat belts are also quiet and can absorb torsional vibration readily.

Leather belting has an ultimate tensile strength ranging from 3,000 to 5,000 lb/in2. Average values of breaking strength of good oak-tanned belting (determined by Benjamin) are as follows: single (double) in solid leather 900 (1,400); at riveted joint 600 (1,200); at laced joint 350 lb/in of width. Well-made cemented joints have strengths equal to the belt, leather-laced and riveted joints about one-third to two-thirds as strong, and wire-laced joints about 85 to 95 percent as strong.

Rubber belting is made from fabric or cord impregnated and bound together by vulcanized rubber compounds. The fabric or cord may be of cotton or rayon. Nylon cord and steel cord or cable are also available. Advantages are high tensile strength, strength to hold metal fasteners satisfactorily, and resistance to deterioration by moisture. The best rubber fabric construction for most types of service is made from hard or tight-woven fabric with a ''skim coat'' or thin layer of rubber between plies. The cord type of construction allows the use of smaller pulley diameters than the fabric type, and also develops less stretch in service. It must be used in the endless form, except in cases where the oil-field type of clamp may be used.

Initial tensions in rubber belts run from 15 to 25 lb/ply/in width. A common rule is to cut belts 1 percent less than the minimum tape-line measurement around the pulleys. For heavy loads, a $1\frac{1}{2}$ percent allowance is usually required, although, because of shrinkage, less initial tension is required for wet or damp conditions. Initial tensions of 25 lb/ply/in may overload shafts or bearings. Maximum safe tightside tensions for rubber belts are as follows:

Centrifugal forces at high speeds require higher tight-side tensions to carry rated horsepower.

Rubber belting may be bought in endless form or made endless in the field by means of a vulcanized splice produced by a portable electric vulcanizer. For endless belts the drive should provide take-up of 2 to 4 percent to allow for length variation as received and for stretch in service. The amount of take-up will vary with the type of belt used. For certain drives, it is possible to use endless belts with no provision for take-up, but this involves a heavier belt and a higher initial unit tension than would be the case otherwise. Ultimate tensile strength of rubber belting varies from 280 to 600 lb or more per inch width per ply. The weight varies from 0.02 to 0.03 or more lb/in width/ply. Belts with steel reinforcement are considerably heavier. For horsepower ratings of rubber belts, se[e Table 8.2.47](#page-51-0)*c*.

Arrangements for Belt Drives In belt drives, the centerline of the belt advancing on the pulley should lie in a plane passing through the midsection of the pulley at right angles to the shaft. Shafts inclined to each other require connections as shown i[n Fig. 8.2.87](#page-52-0)*a*. In case guide pulleys are needed their positions can be determined as shown in [Fig.](#page-52-0) [8.2.87](#page-52-0)*a*, *b*, and *c*. In [Fig. 8.2.87](#page-52-0)*d* the center circles of the two pulleys to be connected are set in correct relative position in two planes, *a* being the angle between the planes ($=$ supplement of angle between shafts). If any two points as *E* and *F* are assumed on the line of intersection *MN* of the planes, and tangents *EG, EH, FJ,* and *FK* are drawn from them to the circles, the center circles of the guide pulleys must be so arranged that these tangents are also tangents to them, as shown. In other words, the middle planes of the guide pulleys must lie in the planes *GEH* and *JFK*.

| | | Squirrel-cage ac motor | | Single- | DC | Diesel engine, | |
|-------------------------------------|---------------------------------|------------------------|---|-----------------------------|--------------------------|--|--|
| Application | Normal torque, line start | High torque | Wound rotor ac motor (slip ring) | phase capacitor motor | shunt- wound motor | 4 or more cyl, above 700 r/min | |
| Agitators | $1.0 - 1.2$ | $1.2 - 1.4$ | 1.2 | | | | |
| Compressors | $1.2 - 1.4$ | | 1.4 | 1.2 | 1.2 | 1.2 | |
| Belt conveyors (ore, coal, sand) | | 1.4 | | | 1.2 | | |
| Screw conveyors | | 1.8 | | | 1.6 | | |
| Crushing machinery | | 1.6 | 1.4 | | | $1.4 - 1.6$ | |
| Fans, centrifugal | 1.2 | | 1.4 | | 1.4 | 1.4 | |
| Fans, propeller | 1.4 | 2.0 | 1.6 | | 1.6 | 1.6 | |
| Generators and exciters | 1.2 | | _ | _ | 1.2 | 2.0 | |
| Line shafts | 1.4 | | 1.4 | 1.4 | 1.4 | 1.6 | |
| Machine tools | $1.0 - 1.2$ | | $1.2 - 1.4$ | 1.0 | $1.0 - 1.2$ | | |
| Pumps, centrifugal | 1.2 | 1.4 | 1.4 | 1.2 | 1.2 | | |
| Pumps, reciprocating | $1.2 - 1.4$ | | $1.4 - 1.6$ | | | $1.8 - 2.0$ | |

Table 8.2.47*a* **Service Factors** *S*

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Table 8.2.47*b* **Arc of Contact Factor** *K***—Rubber Belts**

When these conditions are met, the belts will run in either direction on the pulleys.

To avoid the necessity of taking up the **slack** in belts which have become stretched and permanently lengthened, a **belt tightener** such as shown i[n Fig. 8.2.88 m](#page-52-0)ay be employed. It should be placed on the slack side of the belt and nearer the driving pulley than the driven pulley. Pivoted motor drives may also be used to maintain belt tightness with minimum initial tension.

Length of Belt for a Given Drive The length of an **open belt** for a given drive is equal to $L = 2C + 1.57(D + d) + (D - d)^2/(4C)$, where \bar{L} = length of belt, in; *D* = diam of large pulley, in; *d* = diam of small pulley, in; and $C =$ distance between pulley centers, in. Center

distance *C* is given by $C = 0.25b + 0.25 \sqrt{b^2 - 2(D - d)^2}$, where $b = L - 1.57(D + d)$. When a crossed belt is used, the length in $L =$ $2C + 1.57(D + d) + (D + d)^2/(4C)$.

Step or Cone Pulleys For belts operating on step pulleys, the pulley diameters must be such that the belt will fit over any pair with equal tightness. With **crossed belts,** it will be apparent from the equation for length of belt that the sum of the pulley diameters need only be constant in order that the belt may fit with equal tightness on each pair of pulleys. With open belts, the length is a function of both the sum and the difference of the pulley diameters; hence no direct solution of the problem is possible, but a graphical approach can be of use.

A graphical method devised by Smith (*Trans. ASME,* 10) is shown in Fig. 8.2.89. Let *A* and *B* be the centers of any pair of pulleys in the set, the diameters of which are known or assumed. Bisect *AB* in *C*, and draw *CD* at right angles to *AB*. Take $CD = 0.314$ times the center distance *L*, and draw a circle tangent to the belt line *EF*. The belt line of any other pair of pulleys in the set will then be tangent to this circle. If the angle

Table 8.2.47*d* **Minimum Pulley Diameters—Rubber Belts, in**

EF makes with *AB* is greater than 18°, draw a tangent to the circle *D*, making an angle of 18° with *AB*; and from a center on *CD* distant 0.298*L* above *C*, draw an arc tangent to this 18° line. All belt lines with angles greater than 18° will be tangent to this last drawn arc.

Fig. 8.2.87 Arrangements for flat-belt drives.

A very slight error in a graphical solution drawn to any scale much under full size will introduce an error seriously affecting the equality of belt tensions on the various pairs of pulleys in the set, and where much power is to be transmitted it is advisable to calculate the pulley diameters from the following **formulas** derived from Burmester's graphical method (''Lehrbuch der Mechanik'').

Fig. 8.2.88 Belt tightener. **Fig. 8.2.89** Symbols for cone pulley graphical method.

Let D_1 and D_2 be, respectively, the diameters of the smaller and larger pulleys of a pair, $n = D_2/D_1$, and $l =$ distance between shaft centers, all in inches. Also let $m = 1.58114l - D_0$, where $D_0 =$ diam of both pulleys for a speed ratio $n = 1$. Then $(D_1 + m)^2 + (nD_1 + m)^2 = 5l^2$. First settle on values of D_0 , *l*, and *n*, and then substitute in the equation and solve for D_1 . The diameter D_2 of the other pulley of the pair will then be nD_1 . The values are correct to the fourth decimal place.

The speeds given by cone pulleys should increase in a **geometric ratio;** i.e., each speed should be multiplied by a constant *a* in order to obtain the next higher speed. Let n_1 and n_2 be, respectively, the lowest and highest speeds (r/min) desired and *k* the number of speed changes. Then $a = \sqrt[k]{\frac{k}{n_2/n_1}}$. In practice, *a* ranges from 1.25 up to 1.75 and even 2. The ideal value for *a* in machine-tool practice, according to Carl G. Barth, would be 1.189. In the example below, this would mean the use of 18 speeds instead of 8.

EXAMPLE. Let $n_1 = 16$, $n_2 = 400$, and $k = 8$, to be obtained with four pairs of pulleys and a back gear. From formula, $a = \sqrt{25} = 1.584$, whence speeds will be

16, $(16 \times 1.584 =) 25.34$, $(25.34 \times 1.584 =) 40.14$, and similarly 63.57, 100.7, 159.5, 252.6, and 400. The first four speeds are with the back gear in; hence the back-gear ratio must be $100.7 \div 16 = 6.29$.

Transmission of Power by Flat Belts The theory of flat-belt drives takes into account changes in belt tension caused by friction forces between belt and pulley, which, in turn, cause belt elongation or contraction, thus inducing relative movement between belt and pulley. The transmission of power is a complex affair. A lengthy mathematical presentation can be found in Firbank, ''Mechanics of the Flat Belt Drive,'' ASME Paper 72-PTG-21. A simpler, more conventional analysis used for many years yields highly serviceable designs.

The turning force (tangential) on the rim of a pulley driven by a flat belt is equal to $T_1 - T_2$, where T_1 and T_2 are, respectively, the tensions in the driving (tight) side and following (slack) side of the belt. (For the relations of T_1 and T_2 at low peripheral speeds, see Sec. 3.) Log $(T_1/T_2) = 0.0076fa$ when the effect of centrifugal force is neglected and $T_1/T_2 = 10^{0.0076fa}$. Figure 8.2.90 gives values of this function. When the speeds are high, however, the relations of T_1 to T_2 are modified by centrifugal stresses in the belt, in which case $log(T_1/T_2)$ = $0.0076f(1 - x)a$, where $f =$ coefficient of friction between the belt and pulley surface, $a =$ angle of wrap, and $x = 12wv^2/(gt)$ in which $w =$

Fig. 8.2.90 Values of $10^{0.0076fa}$.

weight of 1 in³ of belt material, lb; $v =$ belt speed, ft/s; $g = 32.2$ ft/s²; and $t =$ allowable working tension, lb/in². Values of *x* for leather belting (with $w = 0.035$ and $t = 300$) are as follows:

Researches by Barth (*Trans. ASME,* 1909) seem to show that *f* is a function of the belt velocity, varying according to the formula $f =$ $0.54 - 140/(500 + V)$ for leather belts on iron pulleys, where $V =$ belt velocity for ft/min. For practical design, however, the following values of *f* may be used: for leather belts on cast-iron pulleys, $f =$ 0.30; on wooden pulleys, $f = 0.45$; on paper pulleys, $f = 0.55$. The treatment of belts with belt dressing, pulleys with cork inserts, and dampness are all factors which greatly modify these values, tending to make them higher.

The **arc of contact** on the smaller of two pulleys connected by an open belt, in degrees, is approximately equal to $180 - 60(D - d)$ */l*, where *D* and *d* are the larger and smaller pulley diameters and *l* the distance between their shaft centers, all in inches. This formula gives an error not exceeding 0.5 percent.

Selecting a Belt Selecting an appropriate belt involves calculating horsepower per inch of belt width as follows:

$$
hp/in = (demanded hp \times S)/(K \times W)
$$

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where demanded hp = horsepower required by the job at hand; $S =$ service factor; $K = arc$ factor; $W =$ proposed belt width (determined from pulley width). One enters a belt manufacturer's catalog with *hp/in, belt speed,* and *small pulley diameter,* then selects that belt which has a matching maximum hp/in rating. See [Table 8.2.47](#page-50-0)*a, b, c,* and *d* for typical values of *S, K,* hp/in ratings, and minimum pulley diameters.

V-Belt Drives

V-belt drives are widely used in power transmission, despite the fact that they may range in efficiency from about 70 to 96 percent. Such drives consist essentially of endless belts of trapezoidal cross section which ride in V-shaped pulley grooves (se[e Fig. 8.2.93](#page-56-0)*a*). The belts are formed of cord and fabric, impregnated with rubber, the cord material being cotton, rayon, synthetic, or steel. V-belt drives are quiet, able to absorb shock and operate at low bearing pressures. A V belt should ride with the top surface approximately flush with the top of the pulley groove; clearance should be present between the belt base and the base of the groove so that the belt rides on the groove walls. The friction between belt and groove walls is greatly enhanced beyond normal values because sheave groove angles are made somewhat less than beltsection angles, causing the belt to wedge itself into the groove. See [Table 8.2.56](#page-57-0)*a* for standard groove dimensions of sheaves.

The cross section and lengths of V belts have been standardized by ANSI in both inch and SI (metric) units, while ANSI and SAE have standardized the special category of automobile belts, again in both units. Standard designations are shown in Table 8.2.48, which also includes minimum sheave diameters. V belts are specified by combining a standard designation (from Table 8.2.48) and a belt length; inside length for the inch system, and pitch (effective) length for metric system.

Table 8.2.48 V-Belt Standard Designations—A Selection

| | | Inch standard | | Metric standard | |
|----------------|----------------|--------------------------------------|---------|--------------------------------------|--|
| Type | Section | Minimum sheave diameter, in | Section | Minimum sheave diameter, mm | |
| Heavy-duty | А | 3.0 | 13 C | 80 | |
| | B | 5.4 | 16 C | 140 | |
| | \overline{C} | 9.0 | 22 C | 214 | |
| | D | 13.0 | 32 C | 355 | |
| | E | 21.04 | | | |
| Automotive | 0.25 | 2.25 | 6 A | 57 | |
| | 0.315 | 2.25 | 8 A | 57 | |
| | 0.380 | 2.40 | 10 A | 61 | |
| | 0.440 | 2.75 | 11 A | 70 | |
| | 0.500 | 3.00 | 13 A | 76 | |
| | 11/16 | 3.00 | 15 A | 76 | |
| | $^{3/4}$ | 3.00 | 17 A | 76 | |
| | $\frac{7}{8}$ | 3.50 | 20 A | 89 | |
| | 1.0 | 4.00 | 23 A | 102 | |
| Heavy-duty | 3V | 2.65 | | | |
| narrow | 5 V | 7.1 | | | |
| | 8 V | 12.3 | | | |
| Notched narrow | 3 VX | 2.2 | | | |
| | 5 VX | 4.4 | | | |
| Light-duty | 2L | 0.8 | | | |
| | 3L | 1.5 | | | |
| | 4L | 2.5 | | | |
| | 5L | 3.5 | | | |
| Synchronous | MXL | | | | |
| belts | XL | | | | |
| | L | | | | |
| | H | | | | |
| | XH | | | | |
| | XXH | | | | |

NOTE: The use of smaller sheaves than minimum will tend to shorten belt life. SOURCE: Compiled from ANSI/RMA IP-20, 21, 22, 23, 24, 25, 26; ANSI/SAE J636C. Sheaves are specified by their pitch diameters, which are used for velocity ratio calculations in which case inside belt lengths must be converted to pitch lengths for computational purposes. Pitch lengths are calculated by adding a conversion factor to inside length (i.e., $L_n =$ $L_s + \Delta$). See Table 8.2.49 for conversion factors. Table 8.2.50 lists standard inside inch lengths L_s and [Table 8.2.51](#page-54-0) lists standard metric pitch (effective) lengths L_n .

Table 8.2.49 Length Conversion Factors Δ

| Belt section | Size interval | Conversion factor | Belt section | Size interval | Conversion factor |
|-----------------|------------------|----------------------|-----------------|------------------|----------------------|
| А | $26 - 128$ | 1.3 | D | $120 - 210$ | 3.3 |
| B | $35 - 210$ | 1.8 | D | \geq 240 | 0.8 |
| В | ≥ 240 | 0.3 | E | $180 - 210$ | 4.5 |
| | $51 - 210$ | 2.9 | E | ≥ 240 | 1.0 |
| | \geq 240 | 0.9 | | | |

SOURCE: Adapted from ANSI/RMA IP-20-1977 (R88) by permission.

Table 8.2.50 Standard Lengths *Ls* **, in, and Length Correction Factors** *K***² : Conventional Heavy-Duty V Belts**

SOURCE: ANSI/RMA IP-20-1977 (R88), reproduced by permission.

SOURCE: ANSI/RMA IP-20-1988 revised, reproduced by permission.

For given large and small sheave diameters and center-to-center distance, the needed V-belt length can be computed from

$$
L_p = 2C + 1.57(D + d) + \frac{(D - d)^2}{4C}
$$

$$
C = \frac{K + \sqrt{K^2 - 32(D - d)^2}}{16}
$$

$$
K = 4L_p - 6.28(D + d)
$$

where $C =$ center-to-center distance; $D =$ pitch diameter of large sheave; $d =$ pitch diameter of small sheave; $L_p =$ pitch (effective) length.

Arc of contact on the smaller sheave (degrees) is approximately

$$
\theta = 180 - \frac{60(D - d)}{C}
$$

Transmission of Power by V Belts Unfortunately there is no theory or mathematical analysis that is able to explain all experimental results reliably. Empirical formulations based on experimental results, however, do provide very serviceable design procedures, and together with data published in V-belt manufacturers' catalogs provide the engineer with the necessary V-belt selection tools.

For satisfactory performance under most conditions, ANSI provides the following empirical single V-belt power-rating formulation (inch

and metric units) for 180° arc of contact and average belt length:
\n
$$
H_r = \left(C_1 - \frac{C_2}{d} - C_3(r - d)^2 - C_4 \log rd \right) rd + C_2r \left(1 - \frac{1}{K_A} \right)
$$

where H_r = rated horsepower for inch units (rated power kW for metric units); C_1 , C_2 , C_3 , C_4 = constants from Table 8.2.53; $r = r/min$ of high-speed shaft times 10^{-3} ; K_A = speed ratio factor from Table 8.2.52; $d =$ pitch diameter of small sheave, in (mm).

Selecting a Belt Selecting an appropriate belt involves calculating horsepower per belt as follows:

 NH_r = (demanded hp $\times K_s$)/(K_1K_2)

where $H_r = h p/b$ elt rating, either from ANSI formulation above, or from manufacturer's catalog ([see Table 8.2.5](#page-55-0)5); demanded hp $=$ horsepower required by the job at hand; K_s = service factor accounting for driver and driven machine characteristics regarding such things as shock, torque level, and torque uniformity (see Table 8.2.54); K_1 = angle of contact correction factor (se[e Fig. 8.2.91](#page-55-0)*a*); K_2 = length correction factor (se[e Tables 8.2.50](#page-53-0) and 8.2.51); $N =$ number of belts.

Se[e Fig. 8.2.91](#page-55-0)*b* for selection of V-belt cross section.

V band belts, effectively joined V belts, serve the function of multiple single V belts (se[e Fig. 8.2.93](#page-56-0)*b*).

Long center distances are not recommended for V belts because excess slack-side vibration shortens belt life. In general $D \leq C \leq$ $3(D + d)$. If longer center distances are needed, then link-type V belts can be used effectively.

Since belt-drive capacity is normally limited by slippage of the smaller sheave, V-belt drives can sometimes be used with a flat, larger pulley rather than with a grooved sheave, with little loss in capacity. For instance the flat surface of the flywheel in a large punch press can serve such a purpose. The practical range of application is when speed ratio is over 3 : 1, and center distance is equal to or slightly less than the diameter of the large pulley.

Table 8.2.52 Approximate Speed-Ratio Factor K_A for Use in **Power-Rating Formulation**

| D/d range | K_A | D/d range | K_A |
|---------------|--------|---------------|--------|
| $1.00 - 1.01$ | 1.0000 | $1.15 - 1.20$ | 1.0586 |
| $1.02 - 1.04$ | 1.0112 | $1.21 - 1.27$ | 1.0711 |
| $1.05 - 1.07$ | 1.0226 | $1.28 - 1.39$ | 1.0840 |
| $1.08 - 1.10$ | 1.0344 | $1.40 - 1.64$ | 1.0972 |
| $1.11 - 1.14$ | 1.0463 | Over 1.64 | 1.1106 |

SOURCE: Adapted from ANSI/RMA IP-20-1977 (R88), by permission.

Table 8.2.53 Constants C_1 , C_2 , C_3 , C_4 for Use in **Power-Rating Formulation**

SOURCE: Compiled from ANSI/RMA IP-20-1977 (R88), by permission.

Table 8.2.54 Approximate Service Factor *Ks* **for V-Belt Drives**

| | Load | | | | | | |
|--|----------------------------|--------------------------|----------------------------|----------------------------|--|--|--|
| Power source torque | Uniform | Light shock | Medium shock | Heavy shock | | | |
| Average or normal Nonuniform or heavy | $1.0 - 1.2$ $1.1 - 1.3$ | $1.1 - 1.3$ $12 - 14$ | $1.2 - 1.4$ $1.4 - 1.6$ | $1.3 - 1.5$ $1.5 - 1.8$ | | | |

SOURCE: Adapted from ANSI/RMA IP-20-1977 (R88), by permission.

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Speed_s

* For footnote see end of table on next page.

In general the V-belting of skew shafts is discouraged because of the decrease in life of the belts, but where design demands such arrangements, special deep-groove sheaves are used. In such cases center distances should comply with the following:

where $W =$ width of group of individual belts. Selected values of *W* are shown in [Table 8.2.56](#page-58-0)*d*.

Fig. 8.2.91 a Angle-of-contact correction factor, where $A =$ grooved sheave to grooved pulley distance (V to V) and $B =$ grooved sheave to flat-face pulley distance (V to flat).

Fig. 8.2.91*b* V-belt section for required horsepower ratings. Letters A, B, C, D, E refer to belt cross section. (Se[e Table 8.2.54](#page-54-0) for service factor.)

[Figure 8.2.92](#page-56-0) shows a 90° turn arrangement, from which it can be seen that the horizontal shaft should lie some distance *Z* higher than the center of the vertical-shaft sheav[e. Table 8.2.56](#page-58-0)*c* lists the values of *Z* for various center distances in a 90° turn arrangement.

Cogged V belts have cogs molded integrally on the underside of the belt [\(Fig. 8.2.94](#page-56-0)*a*). Sheaves can be up to 25 percent smaller in diameter with cogged belts because of the greater flexibility inherent in the cogged construction. An extension of the cogged belt mating with a sheave or pulley notched at the same pitch as the cogs leads to a drive particularly useful for timing purposes.

| Speed of faster Belt shaft, | | | Rated horsepower per belt for small sheave pitch diameter, in | | | | | | Additional horsepower per belt for speed ratio | | | | |
|---|-------|--------|---|----------|-------|--------|--------|-------|--|---------------|---------------|---------------|---------------|
| section | r/min | 12.00 | 14.00 | 16.00 | 18.00 | 20.00 | 22.00 | 24.00 | $1.02 - 1.04$ | $1.08 - 1.10$ | $1.15 - 1.20$ | $1.28 - 1.39$ | 1.65 - over |
| D | 50 | 1.96 | 2.52 | 3.08 | 3.64 | 4.18 | 4.73 | 5.27 | 0.02 | 0.06 | 0.10 | 0.13 | 0.17 |
| | 200 | 6.28 | 8.27 | 10.24 | 12.17 | 14.08 | 15.97 | 17.83 | 0.08 | 0.23 | 0.38 | 0.54 | 0.69 |
| | 400 | 10.89 | 14.55 | 18.12 | 21.61 | 25.02 | 28.35 | 31.58 | 0.15 | 0.46 | 0.77 | 1.08 | 1.38 |
| | 600 | 14.67 | 19.75 | 24.64 | 29.33 | 33.82 | 38.10 | 42.15 | 0.23 | 0.69 | 1.15 | 1.61 | 2.07 |
| | 800 | 17.70 | 23.91 | 29.75 | 35.21 | 40.24 | 44.83 | 48.94 | 0.31 | 0.92 | 1.54 | 2.15 | 2.77 |
| | 1,000 | 19.93 | 26.94 | 33.30 | 38.96 | 43.86 | 47.93 | 51.12 | 0.38 | 1.15 | 1.92 | 2.69 | 3.46 |
| | 1,200 | 21.32 | 28.71 | 35.05 | 40.24 | 44.18* | | | 0.46 | 1.39 | 2.31 | 3.23 | 4.15 |
| | 1,400 | 21.76 | 29.05 | 34.76* | | | | | 0.54 | 1.62 | 2.69 | 3.77 | 4.84 |
| | 1,600 | 21.16 | 27.81* | | | | | | 0.62 | 1.85 | 3.08 | 4.30 | 5.53 |
| | 1,800 | 19.41 | | | | | | | 0.69 | 2.08 | 3.46 | 4.84 | 6.22 |
| | 1,950 | 17.28* | | | | | | | 0.75 | 2.25 | 3.75 | 5.25 | 6.74 |
| | | 18.00 | 21.00 | 24.00 | 27.00 | 30.00 | 33.00 | 36.00 | | | | | |
| E | 50 | 4.52 | 5.72 | 6.91 | 8.08 | 9.23 | 10.38 | 11.52 | 0.04 | 0.11 | 0.18 | 0.26 | 0.33 |
| | 100 | 8.21 | 10.46 | 12.68 | 14.87 | 17.04 | 19.19 | 21.31 | 0.07 | 0.22 | 0.37 | 0.51 | 0.66 |
| | 200 | 14.68 | 18.86 | 22.97 | 27.00 | 30.96 | 34.86 | 38.68 | 0.15 | 0.44 | 0.73 | 1.03 | 1.32 |
| | 300 | 20.37 | 26.29 | 32.05 | 37.67 | 43.13 | 48.43 | 53.58 | 0.22 | 0.66 | 1.10 | 1.54 | 1.98 |
| | 400 | 25.42 | 32.87 | 40.05 | 46.95 | 53.55 | 59.84 | 65.82 | 0.29 | $0.88\,$ | 1.47 | 2.06 | 2.64 |
| | 500 | 29.86 | 38.62 | 46.92 | 54.74 | 62.05 | 68.81 | 75.00 | 0.37 | 1.10 | 1.84 | 2.57 | 3.30 |
| | 600 | 33.68 | 43.47 | 52.55 | 60.87 | 68.36 | 74.97 | 80.63 | 0.44 | 1.32 | 2.20 | 3.08 | 3.96 |
| | 700 | 36.84 | 47.36 | 56.83 | 65.15 | 72.22 | 77.93* | | 0.51 | 1.54 | 2.57 | 3.60 | 4.62 |
| | 800 | 39.29 | 50.20 | 59.61 | 67.36 | 73.30* | | | 0.59 | 1.76 | 2.94 | 4.11 | 5.28 |
| | 900 | 40.97 | 51.89 | 60.73 | | | | | 0.66 | 1.98 | 3.30 | 4.63 | 5.94 |
| | 1,000 | 41.84 | 52.32 | $60.04*$ | | | | | 0.73 | 2.21 | 3.67 | 5.14 | 6.60 |
| | 1,100 | 41.81 | 51.40* | | | | | | 0.81 | 2.43 | 4.04 | 5.65 | 7.26 |
| | 1,200 | 40.83 | | | | | | | 0.88 | 2.65 | 4.41 | 6.17 | 7.93 |
| | 1,300 | 38.84* | | | | | | | 0.95 | 2.87 | 4.77 | 6.68 | 8.59 |

Table 8.2.55 Horsepower Ratings of V Belts (*Continued***)**

* Rim speed above 6,000 ft/min. Special sheaves may be necessary. SOURCE: Compiled from ANSI/RMA IP-20-1988 revised, by permission.

Ribbed V belts are really flat belts molded integrally with longitudinal ribbing on the underside (Fig. 8.2.94*b*). Traction is provided principally by friction between the ribs and sheave grooves rather than by wedging action between the two, as in conventional V-belt operation. The flat

Fig. 8.2.92 Quarter-turn drive for V belts.

upper portion transmits the tensile belt loads. Ribbed belts serve well when substituted for multiple V-belt drives and for all practical purposes eliminate the necessity for belt-matching in multiple V-belt drives.

Fig. 8.2.94 Special V belts. (*a*) Cogged V belt; (*b*) ribbed V belt.

Adjustable Motor Bases

To maintain proper belt tensions on short center distances, an adjustable motor base is often used. Figure 8.2.95 shows an embodiment of such a base made by the Automatic Motor Base Co., in which adjustment for proper belt tension is made by turning a screw which opens or closes the center distance between pulleys, as required. The carriage portion of the base is spring loaded so that after the initial adjustment for belt tension

Fig. 8.2.95 Adjustable motor base.

* The *a* values shown for the A/B combination sheaves are the geometrically derived values. These values may be different than those shown in manufacturers' catalogs.

SOURCE: ''Dayco Engineering Guide for V-Belt Drives,'' Dayco Corp., Dayton, OH, 1981, reprinted by permission.

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| | Deep groove dimensions | | | | | | | | | |
|------------------|--|---|-------------------------------------|----------------|-------|-----------------|-------------------------------|--|--|--|
| Cross section | Outside diameter range | Groove angle $\alpha \pm 0.33^{\circ}$ | b_e | h_{g} min | 2a | $S_e \pm 0.025$ | S_e | | | |
| A | Up through 5.96 Over 5.96 | 34 38 | 0.539 ± 0.005 0.611 | 0.615 | 0.560 | 0.750 | $+0.090$ 0.438 -0.062 | | | |
| B | Up through 7.71 Over 7.71 | 34 38 | 0.747 ± 0.006 0.774 | 0.730 | 0.710 | 0.875 | $+0.120$ 0.562 -0.065 | | | |
| \mathcal{C} | Up through 9.00 Over 9.00 to and incl. 13.01 | 34 36 | 1.066 $+0.007$ 1.085 | 1.055 | 1.010 | 1.250 | $+0.160$ 0.812 -0.070 | | | |
| | Over 13.01 | 38 | 1.105 | | | | | | | |
| D | Up through 14.42 Over 14.42 to and incl. 18.43 Over 18.43 | 34 36 38 | 1.513 1.541 ± 0.008 1.569 | 1.435 | 1.430 | 1.750 | $+0.220$ 1.062 -0.080 | | | |
| E | Up through 25.69 Over 25.69 | 36 38 | 1.816 $+0.010$ 1.849 | 1.715 | 1.690 | 2.062 | $+0.280$ 1.312 -0.090 | | | |

Table 8.2.56*b* **Classical Deep Groove Sheave Dimensions, in**

SOURCE: ''Dayco Engineering Guide for V-Belt Drives,'' Dayco Corp., Dayton, OH, 1981, reprinted by permission.

SOURCE: ''Dayco Engineering Guide for V-Belt Drives,'' Dayco Corp., Dayton, OH, 1981, reprinted by permission.

Table 8.2.56*d* **Width** *W* **of Set of Belts Using Deep-Groove Sheaves, in**

| No. of belts | | V-belt cross section | | | | | | | | | |
|-----------------|-----|----------------------|------|-----|-----|------|------|--|--|--|--|
| | 3V | 5V | 8V | А | B | C | D | | | | |
| | 0.4 | 0.6 | 1.0 | 0.5 | 0.7 | 0.9 | 1.3 | | | | |
| 2 | 0.9 | 1.4 | 2.3 | 1.3 | 1.6 | 2.2 | 3.1 | | | | |
| 3 | 1.4 | 2.2 | 3.6 | 2.0 | 2.5 | 3.4 | 4.8 | | | | |
| 4 | 1.9 | 3.0 | 4.0 | 2.8 | 3.3 | 4.7 | 6.6 | | | | |
| 5 | 2.4 | 3.8 | 6.2 | 3.5 | 4.2 | 5.9 | 8.3 | | | | |
| 6 | 2.9 | 4.7 | 7.6 | 4.3 | 5.1 | 7.2 | 10.1 | | | | |
| 7 | 3.4 | 5.5 | 8.9 | 5.0 | 6.0 | 8.4 | 11.8 | | | | |
| 8 | 3.9 | 6.3 | 10.2 | 5.8 | 6.8 | 9.7 | 13.6 | | | | |
| 9 | 4.4 | 7.1 | 11.5 | 6.5 | 7.7 | 10.9 | 15.3 | | | | |
| 10 | 4.9 | 7.9 | 12.8 | 7.3 | 8.6 | 12.2 | 17.1 | | | | |

SOURCE: ''Dayco Engineering Guide for V-Belt Drives,'' Dayco Corp., Dayton, OH, 1981, reprinted by permission.

has been made by the screw, the spring will compensate for a normal amount of stretch in the belts. When there is more stretch than can be accommodated by the spring, the screw is turned to provide the necessary belt tensions. The carriage can be moved while the unit is in operation, and the motor base is provided for vertical as well as horizontal mounting.

CHAIN DRIVES

Roller-Chain Drives

The advantages of finished steel roller chains are high efficiency (around 98 to 99 percent), no slippage, no initial tension required, and chains may travel in either direction. The basic construction of roller chains is shown in Fig. 8.2.96 and [Table 8.2.57.](#page-59-0)

The shorter the pitch, the higher the permissible operating speed of roller chains. Horsepower capacity in excess of that provided by a single chain may be had by the use of multiple chains, which are essentially parallel single chains assembled on pins common to all strands. Because of its lightness in relation to tensile strength, the effect of centrifugal pull does not need to be considered; even at the unusual speed of 6,000 ft/min, this pull is only 3 percent of the ultimate tensile strength.

Fig. 8.2.96 Roller chain construction.

Sprocket wheels with fewer than 16 teeth may be used for relatively slow speeds, but 18 to 24 teeth are desirable for high-speed service. Sprockets with fewer than 25 teeth, running at speeds above 500 or 600 r/min, should be heat-treated to give a tough wear-resistant surface testing between 35 and 45 on the Rockwell C hardness scale.

If the speed ratio requires the larger sprocket to have as many as 128 teeth, or more than eight times the number on the smaller sprocket, it is usually better, with few exceptions, to make the desired reduction in two or more steps. The ANSI tooth form ASME B29.1 M-1993 allows roller chain to adjust itself to a larger pitch circle as the pitch of the chain elongates owing to natural wear in the pin-bushing joints. The greater the number of teeth, the sooner the chain will ride out too near the ends of the teeth.

Idler sprockets may be used on either side of the standard roller chain,

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Table 8.2.57 Roller-Chain Data and Dimensions, in*

* For conversion to metric units (mm) multiply table values by 25.4.

CHAIN DRIVES 8-61

Table 8.2.58 Selected Values of Horsepower Ratings of Roller Chains (*Continued***)**

NOTE: The sections separated by heavy lines denote the method of lubrication as follows: type A (left section), manual; type B (middle section), bath or disk; type C (right section), oil stream. SOURCE: Supplementary section of ANSI B29.1-1975 (R93), adapted by permission.

to take up slack, to guide the chain around obstructions, to change the direction of rotation of a driven shaft, or to provide more wrap on another sprocket. Idlers should not run faster than the speeds recommended as maximum for other sprockets with the same number of teeth. It is desirable that idlers have at least two teeth in mesh with the chain, and it is advisable, though not necessary, to have an idler contact the idle span of chain.

Horsepower ratings are based upon the number of teeth and the rotative speed of the smaller sprocket, either driver or follower. The pinbushing bearing area, as it affects allowable working load, is the important factor for medium and higher speeds. For extremely slow speeds, the chain selection may be based upon the ultimate tensile strength of the chain. For chain speeds of 25 ft/min and less, the chain pull should be not more than $\frac{1}{5}$ of the ultimate tensile strength; for 50 ft/min, $\frac{1}{6}$; for

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100 ft/min, 1⁄7; for 150 ft/min, 1⁄8; for 200 ft/min, 1⁄9; and for 250 ft/ min, 1⁄10 of the ultimate tensile strength.

Ratings for **multiple-strand chains** are proportional to the number of strands. The recommended numbers of strands for multiple chains are 2, 3, 4, 6, 8, 10, 12, 16, 20, and 24, with the maximum overall width in any case limited to 24 in.

The **horsepower ratings** i[n Table 8.2.58](#page-59-0) are modified by the **service factors** in Table 8.2.59. Thus for a drive having a nominal rating of 3 hp, subject to heavy shock, abnormal conditions, 24-h/day operation, the chain rating obtained fro[m Table 8.2.58](#page-59-0) should be at least $3 \times 1.7 =$ 5.1 hp.

Table 8.2.59 Service Factors for Roller Chains

| | Load | | | | | | |
|---|--------|-------------------|----------------|--|--|--|--|
| Power source | Smooth | Moderate shock | Heavy shock | | | | |
| Internal combustion engine with hydraulic drive | 1.0 | 1.2 | 1.4 | | | | |
| Electric motor or turbine | 1.0 | 1.3 | 1.5 | | | | |
| Internal combustion engine with mechanical drive | 12 | 1.4 | 17 | | | | |

SOURCE: ANSI B29.1-1975, adapted by permission.

Chain-Length Calculations Referring to Fig. 8.2.97, $L =$ length of chain, in; $P =$ pitch of chain, in; R and $r =$ pitch radii of large and small sprockets, respectively, in; $D =$ center distance, in; $A =$ tangent length, in; $a =$ angle between tangent and centerline; *N* and $n =$ number

Fig. 8.2.97 Symbols for chain length calculations.

of teeth on larger and smaller sprockets, respectively; $180 + 2a$ and $180 - 2a$ are angles of contact on larger and smaller sprockets, respectively, deg.

$$
a = \sin^{-1}[(R - r)/D] \qquad A = D \cos a
$$

$$
L = NP(180 + 2a)/360 + nP(180 - 2a)/360 + 2D\cos a
$$

If L_p = length of chain in pitches and D_p = center distance in pitches,

$$
L_p = (N + n)/2 + a(N - n)/180 + 2D_p \cos a
$$

Avoiding the use of trigonometric tables,

$$
L_p = 2C + (N + n)/2 + K(N - n)^2/C
$$

where C is the center distance in pitches and K is a variable depending upon the value of $(N - n)/C$. Values of *K* are as follows:

Formulas for chain length on multisprocket drives are cumbersome except when all sprockets are the same size and on the same side of the chain. For this condition, the chain length in pitches is equal to the sum of the consecutive center distances in pitches plus the number of teeth on one sprocket.

Actual chain lengths should be in even numbers of pitches. When necessary, an odd number of pitches may be secured by the use of an offset link, but such links should be avoided if possible. An offset link is one pitch; half roller link at one end and half pin link at the other end. If center distances are to be nonadjustable, they should be selected to give an initial snug fit for an even number of pitches of chain. For the average application, a center distance equal to 40 ± 10 pitches of chain represents good practice.

There should be at least 120° of wrap in the arc of contact on a power sprocket. For ratios of $3:1$ or less, the wrap will be 120° or more for any center distance or number of teeth. To secure a wrap of 120° or more, for ratios greater than $3:1$, the center distance must be not less than the difference between the pitch diameters of the two sprockets.

Sprocket Diameters $N =$ number of teeth; $P =$ pitch of chain, in; $D =$ diameter of roller, in. The pitch of a standard roller chain is measured from the center of a pin to the center of an adjacent pin.

Pitch diam =
$$
P/\sin \frac{180}{N}
$$

\nBottom diam = pitch diam - D
\nOutside diam = $P\left(0.6 + \cot \frac{180}{N}\right)$
\nCaliper diam = $\left(\text{pitch diam} \times \cos \frac{90}{N}\right) - D$

The exact bottom diameter cannot be measured for an odd number of teeth, but it can be checked by measuring the distance (caliper diameter) between bottoms of the two tooth spaces nearest opposite to each other. Bottom and caliper diameters must not be oversize—all tolerances must be negative. ANSI negative tolerance = $0.003 + 0.001P\sqrt{N}$ in.

Design of Sprocket Teeth for Roller Chains The **section profile** for the teeth of roller chain sprockets, recommended by ANSI, has the proportions shown in Fig. 8.2.98. Let $P =$ chain pitch; $W =$ chain width (length of roller); $n =$ number of strands of multiple chain; $M =$ overall width of tooth profile section; $H =$ nominal thickness of the link plate, all in inches. Referring to Fig. 8.2.98, $T = 0.93W - 0.006$, for

Fig. 8.2.98 Sprocket tooth sections.

single-strand chain; $= 0.90W - 0.006$, for double- and triple-strand chains; $= 0.88W - 0.006$, for quadruple- or quintuple-strand chains; and $= 0.86W - 0.006$, for sextuple-strand chain and over. $C = 0.5P$. $E = \frac{1}{8}P$. $R(\text{min}) = 1.063P$. $Q = 0.5P$. $A = W + 4.15H + 0.003$. $M = A(n - 1) + T$.

Inverted-tooth (silent) chain drives have a typical tooth form shown in Fig. 8.2.99. Such chains should be operated in an oil-retaining casing with provisions for lubrication. The use of offset links and chains with an uneven number of pitches should be avoided.

Horsepower ratings per inch of silent chain width, given in ANSI B29.2-1957 (R1971), for various chain pitches and speeds, are shown in

Fig. 8.2.99 Inverted tooth (silent-chain) drive.

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Table 8.2.60 Horsepower Rating per Inch of Chain Width, Silent-Chain Drive (Small Pitch)

* Type I: manual, brush, or oil cup. Type II: bath or disk. Type III: circulating pump. NOTE: For best results, smaller sprocket should have at least 21 teeth.

SOURCE: Adapted from ANSI B29.2M-1982.

Tables 8.2.60 and 8.2.61. These ratings are based on ideal drive conditions with relatively little shock or load variation, an average life of 20,000 h being assumed. In utilizing the horsepower ratings of the tables, the nominal horsepower of the drive should be multiplied by a service factor depending on the application. Maximum, or worst-case scenario, service factors are listed in [Table 8.2.62.](#page-63-0)

For details on lubrication, sprocket dimensions, etc., see ANSI B29.2M-1957(R71). In utilizing Tables 8.2.60 and 8.2.61 (for a complete set of values, see ANSI B29.2M-1982) the required chain width is obtained by dividing the design horsepower by the horsepower ratings given. For calculating silent-chain lengths, the procedure for rollerchain drives may be used.

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* Type I: manual, brush, or oil cup. Type II: bath or disk. Type III: circulating pump. NOTE: For best results, small sprocket should have at least 21 teeth. SOURCE: Adapted from ANSI B29.2-1982.

* The values shown are for the maximum worst-case scenario for each application. The table was assembled from ANSI B29.2M-1982, by permission. Because the listings above are maximum values, overdesign may result when they

ROTARY AND RECIPROCATING ELEMENTS

Slider Crank Mechanism

Kinematics The slider crank mechanism is widely used in automobile engines, punch presses, feeding mechanisms, etc. For such mechanisms, displacements, velocities, and accelerations of the parts are important design parameters. The basic mechanism is shown in Fig. 8.2.100. The slider displacement *x* is given by

$$
x = r \cos \theta + l\sqrt{1 - [(r/l) \sin \theta]^2}
$$

where $r =$ crank length, $l =$ connecting-rod length, $\theta =$ crank angle

measured from top dead center position. Slider velocity is given by
\n
$$
\dot{x} = V = -r\omega \left(\sin \theta + \frac{r \sin 2\theta}{2l \cos \beta} \right)
$$

where ω = instantaneous angular velocity of the crank at position θ and

$$
\cos \beta = \sqrt{1 - (r/l)^2 \sin^2 \theta}
$$

Silder acceleration is given by
\n
$$
a = \ddot{x} = -r\alpha \left(\sin \theta + \frac{r \sin 2\theta}{2 \cos \beta} \right)
$$
\n
$$
-r\omega^2 \left(\cos \theta + \frac{r \cos 2\theta}{2 \cos \beta} + \frac{r \sin^2 2\theta}{2 \cos^2 \beta} \right)
$$

where α = instantaneous angular acceleration of the crank at position θ .

Fig. 8.2.100 Basic slider-crank mechanism.

Forces Neglecting gravity effects, the forces in a mechanism arise from those produced by input and output forces or torques (herewith called static components). Such forces may be produced by driving motors, shaft loads, expanding cylinder gases, etc. The net forces on the various links cause accelerations of the mechanism's masses, and can be thought of as dynamic components. The static components must be borne by the various links, thus giving rise to internal stresses in those parts. The supporting bearings and slide surfaces also feel the effects of these components, as do the support frames. Stresses are also induced by the dynamic components in the links, and such components cause shaking forces and shaking moments in the support frame.

By building onto the basic mechanism appropriately designed countermasses, the support frame and its bearings can be relieved of a significant portion of the dynamic component effects, sometimes called inertia effects. The augmented mechanism is then considered to be ''balanced.'' The static components cannot be relieved by any means, so that the support frame and its bearings must be designed to carry safely the static component forces and not be overstressed. Figure 8.2.101 illustrates a common, simple form of approximate balancing. Sizing of the countermass is somewhat complicated because the total

Fig. 8.2.101 "Balanced" slider-crank mechanism where $T =$ center of mass, $S =$ center of mass of crank *A*, and $Q =$ center of mass of connecting rod *B*.

inertia effect is the vector sum of the separate link inertias, which change in magnitude and direction at each position of the crank. The countermass *D* is sized to contain sufficient mass to completely balance the crank plus an additional mass (effective mass) to ''balance'' the other links (connecting rod and slider). In simple form, the satisfying

ROTARY AND RECIPROCATING ELEMENTS 8-65

condition is approximately

$$
M_D e \omega^2 = M_A a \omega^2 + M_{\text{eff}} e \omega^2
$$

where $a =$ distance from crankshaft to center of mass of crank (note that most often *a* is approximately equal to the crank radius *r*); $e =$ distance from crankshaft to center of mass of countermass; M_{eff} = additional mass of countermass to ''balance'' connecting rod and slider.

From one-half to two-thirds the slider mass (e.g., $\frac{1}{2}M_c \leq M_{\text{eff}} \leq \frac{2}{3}M_c$) is usually added to the countermass for a single-cylinder engine. For critical field work, single and multiple slider crank mechanisms are dynamically balanced by experimental means.

Forces and Torques Figure 8.2.102*a* shows an exploded view of the slider crank mechanism and the various forces and torques on the links (neglecting gravity and weight effects). Inertial effects are shown as broken-line vectors and are manipulated in the same manner as the actual or real forces. The inertial effects are also known as **D'Alembert forces.** The meanings are as follows: $F_1 = -M_p e \omega^2$, parallel to crank *A*; $F_2 = -M_a e\alpha$, perpendicular to crank *A*; $F_3 = (z/l)F_9$; $F_4 =$ as found in Fig. 8.2.102*b*; $F_5 = F_2 - F_7$; $F_6 = F_1 - F_8$; $F_7 = -M_A r \omega^2$, parallel to crank *A*; $F_8 = -M_A r \alpha$, perpendicular to crank *A*; $F_9 = -M_B \times$ absolute acceleration of *Q*, where acceleration of point *Q* can be found

Fig. 8.2.102 (*a*) Forces and torques; (*b*) force polygons.

graphically by constructing an acceleration polygon of the mechanism (see for example Shigley, ''Kinematic Analysis of Mechanisms,'' McGraw-Hill); $F_{10} = (y/l)F_9$; $F_{11} = -M_c \times$ absolute acceleration of slider *x*; F_{12} = normal wall force (neglecting friction); $F =$ external force on slider's face, where the vector sum $F + F_4 + F_{10} + F_{11}$ + $F_{12} = 0$; *T* = external crankshaft torque, where the algebraic sum *T* + $F_3E + F_4W + F_2e + F_7a = 0$ (note that signs must reflect direction of torque); $T_t = F_3 E + F_w W =$ transmitted torque; $K =$ the effective location of force F_9 . The distance Δ of force F_9 from the center of mass of connecting rod *B* (see Fig. 8.2.102*a*) is given by $\Delta = J_{B(\text{cm})} \times$ angular acceleration of link $B/M_B \times$ absolute acceleration of point *Q*. Figure 8.2.102*b* shows the force polygons of the separate links of the mechanism.

Flywheel

One can surmise that both F and T may be functions of crank angle θ . Even if one or the other were deliberately kept constant, the remaining one would still be a function of θ . If a steady-speed crank is desired (ω = constant and α = zero), then external crankshaft torque *T* must be constantly adjusted to equal transmitted torque T_i . In such a situation a motor at the crankshaft would suffer fatigue effects. In a combustion engine the crankshaft would deliver a fluctuating torque to its load.

Inserting a flywheel at the crankshaft allows the peak and valley excursions of ω to be considerably reduced because of the flywheel's ability to absorb energy over periods when $T > T_t$ and to deliver back

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into the system such excess energy when $T < T_t$. Figure 8.2.103*a* illustrates the above concepts, also showing that over one cycle of a repeated event the excess $(+)$ energies and the deficient $(-)$ energies are equal. The greatest crank speed change tends to occur across a single large positive loop, as illustrated in Fig. 8.2.103*a*.

 (b)

Fig. 8.2.103 Sizing the flywheel. (*a*) Variation of torque and crank speed vs. crank angle, showing ΔE_{ab} ; (*b*) graphics for Wittenbauer's analysis.

Sizing the Flywheel For the single largest energy change we can write

$$
\Delta E_{ab} \int_a^b (T - T_t) d\theta = \frac{J_0}{2} (\omega_2^2 - \omega_1^2)
$$

$$
= \frac{J_0}{2} (\omega_2 - \omega_1)(\omega_2 + \omega_1)
$$

where J_0 = flywheel moment of inertia plus effective mechanism moment of inertia.

Define $\overline{\omega} \doteq (\omega_2 + \omega_1)/2$ and C_s = coefficient of speed fluctuation = $(\omega_2 - \omega_1)/\overline{\omega}$. Hence $\Delta E_{ab} = J_0 C_s \overline{\omega}^2$. Acceptable values of C_s are:

Evaluating ΔE_{ab} involves finding the integral

$$
\int_a^b (T-T_1) \, d\theta
$$

which can be done graphically or by a numerical technique such as Simpson's rule.

Wittenbauer's Analysis for Flywheel Performance This method does not involve more computation work than the one described above, but it is more accurate where the reciprocating parts are comparatively heavy. Wittenbauer's method avoids the inaccuracy resulting from the evaluation of the inertia forces on the reciprocating parts on the basis of the uniform nominal speed of rotation for the engine.

Let the crankpin velocity be represented by v_r and the velocity of any moving masses $(m_1, m_2, m_3, \text{ etc.})$ at any instant of phase be represented, respectively, by v_1 , v_2 , v_3 , etc. The kinetic energy of the entire engine system of moving masses may then be expressed as

$$
E = \frac{1}{2}(m_1v_1^2 + m_2v_2^2 + m_3v_3^2 + \cdots) = \frac{1}{2}M_r v_r^2
$$

or, the single reduced mass M_r at the crankpin which possesses the equivalent kinetic energy is

$$
M_r = [m_1(v_1/v_r)^2 + m_2(v_2/v_r)^2 + m_3(v_3/v_r)^2 + \cdots]
$$

In an engine mechanism, sufficiently accurate values of M_r can be obtained if the weight of the connecting rod is divided between the crankpin and the wrist pin so as to retain the center of gravity of the rod in its true position; usually 0.55 to 0.65 of the weight of the connecting rod should be placed on the crankpin, and 0.45 to 0.35 of the weight on the wrist pin. M_r is a variable in engine mechanisms on account of the reciprocating parts and should be found for a number of crank positions. It should include all moving masses except the flywheel.

The total energy *E* used in accelerating reciprocating parts from the beginning of the forward stroke up to any crank position can be obtained by finding from the indicator cards the total work done in the cylinder (on both sides of the piston) up to that time and subtracting from it the work done in overcoming the resisting torque, which may usually be assumed constant. The mean energy of the moving masses is $E_0 =$ $\frac{1}{2}M_r v_r^2$.

In Fig. 8.2.103*b*, the reduced weights of the moving masses $G_F + G_{F5}$ are plotted on the *X* axis corresponding to different crank positions. $G_F = gM_F$ is the reduced flywheel weight and $G_{r5} = gM_{r5}$ is the sum of the other reduced weights. Against each of these abscissas is plotted the energy *E* available for acceleration measured from the beginning of the forward stroke. The curve *O*123456 is the locus of these plotted points.

The diagram possesses the following property: Any straight line drawn from the origin *O* to any point in the curve is a measure of the velocity of the moving masses; tangents bounding the diagram measure the limits of velocity between which the crankpin will operate. The maximum linear velocity of the crankpin in feet per second is v_2 = $\sqrt{2g}$ tan a_2 , and the minimum velocity is $v_1 = \sqrt{2g}$ tan a_1 . Any desired change in v_1 and v_2 may be accomplished by changing the value of G_F , which means a change in the flywheel weight or a change in the flywheel weight reduced to the crankpin. As G_F is very large compared with G_r and the point 0 cannot be located on the diagram unless a very large drawing is made, the tangents are best formed by direct calculation:

$$
\tan \alpha_2 = \frac{v_r^2}{2g} (1 + k) \qquad \tan \alpha_1 = \frac{v_r^2}{2g} (1 - k)
$$

where *k* is the coefficient of velocity fluctuation. The two tangents *ss* and *tt* to the curve $O123456$, thus drawn, cut a distance ΔE and on the ordinate E_0 . The reduced flywheel weight is then found to be

$$
G_F(\Delta E)g/(v_r^2k)
$$

SPRINGS

It is assumed in the following formulas that the springs are in no case stressed beyond the elastic limit (i.e., that they are perfectly elastic) and that they are subject to Hooke's law.

Notation

 $P =$ safe load, lb

- $f =$ deflection for a given load *P*, in
- $l =$ length of spring, in
- $V =$ volume of spring, in³
- S_s = safe stress (due to bending), lb/in²
- S_v = safe shearing stress, lb/in²
- $U =$ resilience, in \cdot lb

For sheet metal and wire gages, ferrous and nonferrous, see [Table](#page-84-0) [8.2.76 a](#page-84-0)nd metal suppliers' catalogs.

The **work** in inch-pounds performed in **deflecting a spring** from 0 to *f* (spring duty) is $U = Pf/2 = s_s^2 V/(CE)$. This is based upon the assumption that the deflection is proportional to the load, and *C* is a constant dependent upon the shape of the springs.

The time of vibration T (in seconds) of a spring (weight not considered) is equal to that of a simple circular pendulum whose length l_0 equals the deflection *f* (in feet that is produced in the spring by the load *P*. $T = \pi \sqrt{l_0 / g}$, where $g =$ acceleration of gravity, ft/s².

Springs Subjected to Bending

1. **Rectangular plate spring** (Fig. 8.2.104).

$$
P = bh2Ss/(6l)
$$

\n
$$
I = bh3/12
$$

\n
$$
U = Pf/2 = VSs2/(18E)
$$

\n
$$
f = Pl3/(3EI) = 4Pl3/(bh3E) = 2l2Ss/(3hE)
$$

Fig. 8.2.105 Triangular plate

Fig. 8.2.104 Rectangular plate spring.

2. **Triangular plate spring** (Fig. 8.2.105). The elastic curve is a circular arc.

spring.

$$
P = bh2Ss/(6l)
$$

$$
I = bh3/12
$$

$$
U = Pf/2 = Ss2V/(6E)
$$

$$
f = Pl3/(2EI) = 6Pl3/(bh3E) = l2Ss/(hE)
$$

3. **Rectangular plate spring with end tapered** in the form of a cubic parabola (Fig. 8.2.106). The elastic curve is a circular arc; *P*, *I*, and *f* same as for triangular plate spring (Fig. 8.2.105); $U = Pf/2 = S_s^2 V/(9E)$. The strength and deflection of **single-leaf flat springs** of various forms

Table 8.2.63 Strength and Deflection of Single-Leaf Flat Springs

are given (Bruce, *Am. Mach.*, July 19, 1900) by the formulas $h = al^2/f$ and $b = cP l/h^2$. The volume of the spring is given by $V = vlbh$. The values of constants *a* and *c* and the resilience in inch-pounds per cubic inch are given in Table 8.2.63, in terms of the safe stress S_s . Values of v are given also.

Fig. 8.2.106 Rectangular plate spring: tapered end.

4. **Compound (leaf or laminated) springs.** If several springs of rectangular section are combined, the resulting compound spring should (1) form a beam of uniform strength that (2) does not open between the joints while bending (i.e., elastic curve must be a circular arc). Only the type immediately following meets both requirements, the others meeting only the second requirement.

5. **Laminated triangular plate spring** (Fig. 8.2.107). If the triangular plate spring shown at I is cut into an even number $(= 2n)$ of strips of equal width (in this case eight strips of width *b*/2), and these strips are combined, a laminated spring will be formed whose carrying capacity will equal that of the original uncut spring; or $P = nbh^2S_s/(6l)$; $n =$ $6P1/(bh^2S_s)$.

Fig. 8.2.107 Laminated triangular plate spring.

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6. **Laminated rectangular plate spring with lead ends tapered** in the form of a cubical parabola (Fig. 8.2.108); see case 3.

Fig. 8.2.108 Laminated rectangular plate spring with leaf end tapered.

7. **Laminated trapezoidal plate spring with leaf ends tapered** (Fig. 8.2.109). The ends of the leaves are trapezoidal and are tapered according to the formula

$$
z = \frac{h}{\sqrt[3]{1 + (b_1/b)(a/x - 1)}}
$$

8. **Semielliptic springs** (for locomotives, trucks, etc.). Referring to Fig. 8.2.110, the load 2*P* (lb) acting on the spring center band produces a tensional stress *P*/cos *a* in each of the inclined shackle links. This is resolved into the vertical force *P* and the horizontal force *P* tan *a*, which together produce a bending moment $M = P(l + p \tan a)$. The equations

Fig. 8.2.109 Laminated trapezoidal plate spring with leaf ends tapered.

given in (1), (2), and (3) apply to curved as well as straight springs. The bearing force $= 2P = (2nbh^2/6)[S_s/(l + p \tan a)]$, and the deflection $=$ $[6l^2/(nbh^3)]P(l + p \tan a)/E = l^2S_2/(hE).$

In addition to the bending moment, the leaves are subjected to the tension force *P* tan *a* and the transverse force *P*, which produce in the upper leaf an additional stress $S = P \tan a/(bh)$, as well as a transverse shearing stress.

Fig. 8.2.110 Semielliptic springs.

In determining the number of leaves *n* in a given spring, allowance should be made for an excess load on the spring caused by the vibration. This is usually done by decreasing the allowable stress about 15 percent.

The foregoing does not take account of initial stresses caused by the band. For more detailed information, see Wahl, ''Mechanical Springs,'' Penton.

9. **Elliptic springs.** Safe load $P = nbh^2S_y/(6l)$, where $l = \frac{1}{2}$ distance

between bolt eyes (less 1⁄2 length of center band, where used); deflection

$$
f = 4l^{2}S_{s}K/(hE), \text{ where}
$$
\n
$$
K = \frac{1}{(1-r)^{3}} \left[\frac{1-r^{2}}{2} - 2r(1-r) - r^{2} \ln r \right]
$$

r being the number of full-length leaves \div total number (*n*) of leaves in the spring. All dimensions in inches. For semielliptic springs, the deflection is only half as great. Safe load = $nbh^2S_s/(3l)$. (Peddle, *Am.*) *Mach.,* Apr. 17, 1913.)

Coiled Springs In these, the load is applied as a couple *Pr* which turns the spring while winding or holds it in place when wound up. If the spindle is not to be subjected to bending moment, *P* must be replaced by two equal and opposite forces $(P/2)$ acting at the circumference of a circle of radius *r*. The formulas are the same in both cases. The springs are assumed to be fixed at one end and free at the other. The bending moment acting on the section of least resistance is always *Pr*. The length of the straightened spring $=$ *l*. See Benjamin and French, Experiments on Helical Springs, *Trans. ASME,* **23**, p. 298.

For **heavy closely coiled helical springs** the usual formulas are inaccurate and result in stresses greatly in excess of those assumed. See Wahl, Stresses in Heavy Closely-Coiled Helical Springs, *Trans. ASME,* 1929. In springs 10 to 12 and 15 to 18, the quantity k is unity for lighter springs and has the stated values (supplied by Wahl) for heavy closely coiled springs.

10. **Spiral coiled springs of rectangular cross section** (Fig. 8.2.111).

$$
P = bh^2S_s/(6rk) \qquad I = bh^3/12 \qquad U = Pf/2 = S_s^2V/(6Ek^2) f = ra = Plr^2/(EI) = 12Plr^2/(Ebh^3) = 2rlS_s/(hEk)
$$

For heavy closely coiled springs, $k = (3c - 1)/(3c - 3)$, where $c =$ 2*R*/*h* and *R* is the minimum radius of curvature at the center of the spiral.

Fig. 8.2.111 Spiral coiled spring: rectangular cross section.

Fig. 8.2.112 Cylindrical helical spring: circular cross section.

11. **Cylindrical helical spring of circular cross section** (Fig. 8.2.112).

$$
P = \pi d^{3}S_{s}/(32rk) \qquad I = \pi d^{4}/64 \qquad U = Pf/2 = S_{s}^{2}V/(8Ek^{2})
$$

$$
f = ra = Plr^{2}/(EI) = 64Plr^{2}/(\pi Ed^{4}) = 2rlS_{s}/(dEk)
$$

For heavy closely coiled springs, $k = (4c - 1)/(4c - 4)$, where $c =$ 2*r*/*d*.

12. **Cylindrical helical spring of rectangular cross section** (Fig. 8.2.113).

 $P = bh^2S_s/(6rk)$ $I = bh^3/12$ $U = Pf/2 = S^2V/(8Ek^2)$ $f = ra = Plr^2/(EI) = 12Plr^2/(Ebh^3) = 2rlS/(hEk)$

For heavy closely coiled springs, $k = (3c - 1)/(3c - 3)$, where $c =$ 2*r*/*h*.

Fig. 8.2.113 Cylindrical helical spring: rectangular cross section.

Springs Subjected to Torsion

The statements made concerning coiled springs subjected to bending apply also to springs 13 and 14.

13. **Straight bar spring of circular cross section** (Fig. 8.2.114).

$$
P = \pi d^{3}S_{v}/(16r) = 0.1963d^{3}S_{v}/r \qquad U = Pf/2 = S_{v}^{2}V/(4G)
$$

$$
f = ra = 32r^{2}IP/(\pi d^{4}G) = 2rIS_{v}/(dG)
$$

14. **Straight bar spring of rectangular cross section** (Fig. 8.2.115).

 $P = 2b^2hS_v/(9r)$ $K = b/h$
 $4S_v^2V(K^2 + 1)/(45G)$ max when $K = 1$ $U = Pf/2 = 4S_v^2V(K^2 + 1)/(45G)$ max when $K = 1$ $f = ra = 3.6r^2lP(b^2 + h^2)/(b^3h^3G) = 0.8rlS_v(b^2 + h^2)/(bh^2G)$

Fig. 8.2.114 Straight bar spring: circular cross section.

Fig. 8.2.115 Straight bar spring: rectangular cross section.

Springs Loaded Axially in Either Tension or Compression

NOTE. For springs 15 to 18, $r =$ mean radius of coil; $n =$ number of coils.

15. **Cylindrical helical spring of circular cross section** (Fig. 8.2.116).

$$
P = \pi d^{3}S_{v}/(16rk) = 0.1963d^{3}S_{v}/(rk)
$$

\n
$$
U = Pf/2 = S_{v}^{2}V/(4Gk^{2})
$$

\n
$$
f = 64nr^{3}P/(d^{4}G) = 4\pi nr^{2}S_{v}/(dGk)
$$

For heavy closely coiled springs, $k = (4c - 1)/(4c - 4) + 0.615/c$, where $c = 2r/d$.

Fig. 8.2.116 Cylindrical helical spring: circular cross section.

Fig. 8.2.117 Wahl correction factor.

16. **Cylindrical helical spring of rectangular cross section** (Fig. 8.2.118).

 $P = 2b^2hS_v/(9rk)$ $K = b/h$
 $4S_v^2V(K^2 + 1)/(45Gk^2)$ max when $K = 1$ $U = Pf/2 = 4S_v^2V(K^2 + 1)/(45Gk^2)$ max when $K = 1$ $f = 7.2 \pi n r^3 P(b^2 + h^2)/(b^3 h^3 G) = 1.6 \pi n r^2 S_v(b^2 + h^2)/(b h^2 G k)$

For heavy closely coiled springs, $k = (4c - 1)/(4c - 4) + 0.615/c$, where $c = 2r/b$.

Fig. 8.2.118 Cylindrical helical spring: rectangular cross section.

17. **Conical helical spring of circular cross section** (Fig. 8.2.119*a*).

- $l =$ length of developed spring
- $d =$ diameter of wire
- $r =$ maximum mean radius of coil
- $P = \pi d^3 S_v/(16rk) = 0.1963d^3 S_v/(rk)$
- $U = Pf/2 = S_v^2 V/(8Gk^2)$
- $f = 16r^2lP/(\pi d^4G) = 16nr^3P/(d^4G)$
- $= r l S_v / (dGk) = \pi n r^2 S_v / (dGk)$

For heavy closely coiled springs, $k = (4c - 1)/(4c - 4) + 0.615/c$, where $c = 2r/d$.

Fig. 8.2.119*a* Conical helical **Fig. 8.2.119** Conical helical **Fig. 8.2.119***b* Conical helical spring: circular cross section.

spring: rectangular cross section.

18. **Conical helical spring of rectangular cross section** (Fig. 8.2.119*b*).

 $b =$ small dimension of section $d = \text{large dimension of section}$ $r =$ maximum mean radius of coil $K = b/h \leq 1$ $P = 2b^2hS_v/(9rk)$
= $2S_v^2V(K^2 + 1)/(45Gk^2)$ max when $K = 1$ $U = Pf/2 = 2S_v^2V(K^2 + 1)/(45Gk^2)$ max when $K = 1$ $f = 1.8r^{2}$ *lP*($b^{2} + h^{2}$)/($b^{3}h^{3}$ *G*) = 1.8 $\pi nr^{3}P(b^{2} + h^{2})$ /($b^{3}h^{3}$ *G*) $= 0.4rI S_v(b^2 + h^2)/(bh^2 Gk) = 0.4\pi n r^2 S_v(b^2 + h^2)/(bh^2 Gk)$

For heavy closed coiled springs, $k = (4c - 1)/(4c - 4) + 0.615c$, where $c = 2r/r_o - r_i$.

19. **Truncated conical springs** (17 and 18). The formulas under 17 and 18 apply for truncated springs. In calculating deflection *f*, however, it is necessary to substitute $r_1^2 + r_2^2$ for r^2 , and $\pi n(r_1 + r_2)$ for $\pi n r$, r_1 and r_2 being, respectively, the greatest and least mean radii of the coils.

NOTE. The preceding formulas for various forms of coiled springs are sufficiently accurate when the cross-section dimensions are small in comparison with the radius of the coil, and for small pitch. Springs 15 to 19 are for either tension or compression but formulas for springs 17 and 18 are good for compression only until the largest coil flattens out; then *r* becomes a variable, depending on the load.

Design of Helical Springs

When sizing a new spring, one must consider the spring's available working space and the loads and deflections the spring must experience. Refinements dictated by temperature, corrosion, reliability, cost, etc. may also enter design considerations. The two basic formulas of load

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and deflection (see item 15[, Fig. 8.2.116](#page-68-0)) contain eight variables (*f*, *P*, *d*, *S*, *r*, *k*, *n*, *G*) which prevent one from being able to use a one-step solution. For instance, if *f* and *P* are known and *S* and *G* are chosen, there still remain *d*, *r*, *k*, and *n* to be found.

A variety of solution approaches are available, including: (1) sliderule-like devices available from spring manufacturers, (2) nomographic methods (Chironis, "Spring Design and Application," McGraw-Hill; Tsai, Speedy Design of Helical Compression Springs by Nomography Method, *J. of Eng. for Industry,* Feb. 1975), (3) table methods (Carlson, ''Spring Designer's Handbook,'' Marcel Dekker), (4) formula method (ibid.), and (5) computer programs and subroutines.

Design by Tables

Safe working loads and deflections of cylindrical helical springs of round steel wire in tension or compression are given i[n Table 8.2.64.](#page-70-0) The table is based on the formulas given for spring 15. $d =$ diameter of steel wire, in; $D =$ pitch diameter (center to center of wire), in; $P =$ safe working load for given unit stress, lb; $f =$ deflection of 1 coil for safe working load, in.

The table is based on the values of unit stress indicated, and $G =$ 12,500,000. For any other value of unit stress, divide the tabular value by the unit stress used in the table and multiply by the unit stress to be used in the design. For any other value of *G*, multiply the value of *f* in the table by 12,500,000 and divide by the value of *G* chosen. For **square steel wire,** multiply values of *P* by 1.06, and values of *f* by 0.75. For **round brass wire,** take $S_s = 10,000$ to 20,000, and multiply values of *f* by 2 (Howe).

EXAMPLES OF USE OF TABLE 8.2.64. 1. Required the safe load (*P*) for a spring of 3⁄8-in round steel with a pitch diameter (*D*) of 31⁄2 in. In the line headed *D*, under $3\frac{1}{2}$, is given the value of *P*, or 678 lb. This is for a unit stress of 115,000 lb/in2. The load *P* for any other unit stress may be found by dividing the 678 by 115,000 and multiplying by the unit stress to be used in the design. To determine the number of coils this spring would need to compress (say) 6 in under a load of (say) 678 lb, take the value of *f* under 678, or 0.938, which is the deflection of one coil under the given load. Therefore, $6/0.938 = 6.4$, say 7, equals the number of coils required. The spring will therefore be 2% in long when closed (7 \times 3/8), counting the working coils only, and must be 85⁄8 in long when unloaded. Whether there is an extra coil at one end which does not deflect will depend upon the details of the particular design. The deflection in the above example is for a unit stress of 115,000 lb/in2. The rule is, divide the deflection by 115,000 and multiply by the unit stress to be used in the design.

2. A 7⁄16-in steel spring of 31⁄2-in OD has its coils in close contact. How much can it be extended without exceeding the limit of safety? The maximum safe load for this spring is found to be 1,074 lb, and the deflection of one coil under this load is 0.810 in. This is for a unit stress of 115,000 lb/in2. Therefore, 0.810 is the greatest admissible opening between any two coils. In this way, it is possible to ascertain whether or not a spring is overloaded, without knowledge of the load carried.

Design by Formula

A design formula can be constructed by equating calculated stress s_v (from load formula, [Fig. 8.2.117\)](#page-68-0) to an allowable working stress in torsion:

1:
\n
$$
s_{v} = \sigma_{\text{max}} = \frac{16rP}{\pi d^{3}} \left(\frac{4c - 1}{4c - 4} + \frac{0.615}{c} \right) = \frac{16rPk}{\pi d^{3}} = \frac{S_{v}}{K_{\text{sf}}}
$$

where $P =$ axial load on spring, lb; $r = D/2 =$ mean radius of coil, in; $D =$ mean diameter of coil, in (outside diameter minus wire diameter); *d* = wire diameter, in; σ_{max} = torsional stress, lb/in²; K_{sf} = safety factor and $c = D/d$. Note that the expression in parentheses $[(4c - 1)(4c - 1)]$ $4) + 0.615/c$ is the Wahl correction factor *k*, which accounts for the added stresses in the coils due to curvature and direct shear. See [Fig.](#page-68-0) [8.2.117.](#page-68-0) Values of S_v , yield point in shear from standard tests, are strongly dependent on d , hence the availability of S_v in the literature is limited. However, an empirical relationship between S_{uT} and *d* is available (see Shigley, ''Mechanical Engineering Design,'' McGraw-Hill, 4th ed., p. 452). Using also the approximate relations $S_y = 0.75 S_{ut}$

and $S_v = 0.577S_v$ results in the following relationship:

$$
S_v = \frac{0.43A}{d^m}
$$

where *A* and *m* are constants (se[e Table 8.2.65\)](#page-74-0).

Substituting S_v and rearranging yield the following useful formula:

$$
d^{3-m} = \frac{K_{\rm sf} 16rPk}{\pi 0.43A}
$$

EXAMPLE. A slow-speed follower is kept in contact with its cam by means of a helical compression spring, in which the minimum spring force desired is 20 lb to assure firm contact, while maximum spring force is not to exceed 60 lb to prevent excessive surface wear on the cam. The follower rod is 1/4 inch in diameter, and the rod enclosure where the spring is located is $\frac{7}{8}$ inch in diameter. Maximum displacement is 1.5 in.

Choose $r = 0.5 \times 0.75 = 0.375$. Fro[m Table 8.2.65](#page-74-0) choose $m = 0.167$ and $A =$ 169,000. Choose $K_{\text{sf}} = 2$. Assume $k = 1$ to start.

$$
d^{3-0.167} = \frac{(2)(0.375)(60)(16)}{(\pi)(0.43)(169,000)} = 0.00315
$$

$$
d = (0.00315)^{0.35298} = 0.131 \text{ in}
$$
ng constant
$$
= \frac{\Delta P}{\Delta f} = \frac{40}{1.5} = 26.667
$$

and from the deflection formula, the number of active turns

Spri

$$
n = \frac{(0.131)^{4}(11,500,000)}{(26.667)(64)(0.375)^{3}} = 37.6
$$

For squared and ground ends add two dead coils, so that

$$
n_{\text{total}} = 40
$$

\n
$$
H = \text{solid height} = (40)(0.131) = 5.24 \text{ in}
$$

\n
$$
f_0 = \text{displacement from zero to maximum load}
$$

\n
$$
= 60/26.667 = 2.249
$$

\n
$$
L_0 = \text{approximate free length} = 5.24 + 2.249 = 7.49 \text{ in}
$$

NOTE. Some clearance should be added between coils so that at maximum load the spring is not closed to its solid height. Also, the nearest commercial stock size should be selected, and recalculations made on this stock size for S_v , remembering to include *k* at this juncture. If recalculated S_v is satisfactory as compared to published values, the design is retained, otherwise enough iterations are performed to arrive at a satisfactory result[. Figure 8.2.120](#page-74-0) shows a plot of S_{uT} versus *d*. To convert S_{uT} to S_{v} , multiply S_{uT} by 0.43.

$$
c = 2(0.375/0.131) = 5.73
$$

\n
$$
k = \frac{4(5.73) - 1}{4(5.73) - 4} + \frac{0.615}{5.73} = 1.257
$$

\n
$$
S_v = \frac{(K_{\rm sf})(16)(0.375)(1.257)(60)}{\pi (0.131)^3} = (K_{\rm sf})(64,072)
$$

Now $S_{uT} = 235,000$ lb/in² (from [Fig. 8.2.120\)](#page-74-0) and S_v (tabulated) = $(0.43)(235,000) = 101,696$ lb/in² so that $K_{\text{sf}} = 101,696/64,072 = 1.59$, a satisfactory value.

NOTE. The original choice of a generous $K_{\text{sf}} = 2$ was made to hedge against the large statistical variations implied in the empirical formula $S_v = 0.43A/d^m$.

The basis for design of springs in parallel or in series is shown in [Fig.](#page-74-0) [8.2.121.](#page-74-0)

Belleville Springs Often called dished, or conical spring, washers, Belleville springs occupy a very small space. They are stressed in a very complex manner, and provide unusual spring rate curves [\(Fig.](#page-74-0) [8.2.122](#page-74-0)*a*). These springs are nonlinear, but for some proportions, they behave with approximately linear characteristics in a limited range. Likewise, for some proportions they can be used through a spectrum of spring rates, from positive to flat and then through a negative region. The snap-through action, shown at point *A* in [Fig. 8.2.122](#page-74-0)*b*, can be useful in particular applications requiring reversal of spring rates. These

| Allowable unit | | | Pitch diameter D , in | | | | | | | | | | | | | | | | | | | | |
|----------------------|-------------|-----------------------------------|-------------------------|----------------|---------------|----------------|---------------|----------------|---------------|--------------|--------------|---------------|--------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| stress, $1b/in^2$ | Diam, in | D | $\frac{5}{32}$ | $\frac{3}{16}$ | $\frac{1}{4}$ | $\frac{5}{16}$ | $\frac{3}{8}$ | $\frac{7}{16}$ | $\frac{1}{2}$ | $5/8$ | $^{3}/_{4}$ | $\frac{7}{8}$ | -1 | $1\frac{1}{8}$ | $1\frac{1}{4}$ | $1\frac{3}{8}$ | $1\frac{1}{2}$ | $1\frac{5}{8}$ | $1\frac{3}{4}$ | $1\frac{7}{8}$ | $\overline{2}$ | $2\frac{1}{4}$ | $2\frac{1}{2}$ |
| 150,000 | 0.035 | \boldsymbol{P} \mathcal{f} | 16.2 .026 | 13.4 .037 | 10.0 .067 | 8.10 .105 | 6.66 .149 | 5.75 .200 | 4.96 .276 | 4.05 .420 | 3.39 .608 | | | | | | | | | | | | |
| | 0.041 | \boldsymbol{P} | 26.2 .023 | 21.6 .032 | 16.2 .057 | 13.0 .089 | 10.8 .128 | 9.27 .175 | 8.10 .229 | 6.52 .362 | 5.35 .512 | 4.57 .697 | | | | | | | | | | | |
| | 0.047 | \boldsymbol{P} | 39.1 .019 | 32.6 .028 | 24.5 .049 | 19.6 .078 | 16.4 .112 | 13.9 .153 | 12.3 .200 | 9.80 .311 | 8.10 .449 | 6.92 .610 | 6.14 .800 | | | | | | | | | | |
| | 0.054 | \boldsymbol{P} \int | 59.4 .016 | 49.6 .024 | 37.2 .043 | 29.7 .067 | 24.6 .098 | 21.2 .133 | 18.5 .174 | 14.7 .273 | 12.4 .390 | 10.5 .532 | 9.25 .695 | 8.23 .878 | | | | | | | | | |
| | 0.062 | \boldsymbol{P} \mathcal{f} | | 74.9 .021 | 56.1 .037 | 44.9 .058 | 37.3 .084 | 32.0 .115 | 28.0 .151 | 22.4 .235 | 18.6 .340 | 16.1 .460 | 13.9 .605 | 12.5 .760 | 11.2 .947 | | | | | | | | |
| | 0.063 | \boldsymbol{P} | | 78.2 .020 | 58.7 .037 | 46.9 .057 | 39.2 .083 | 33.9 .113 | 29.4 .148 | 23.5 .233 | 19.6 .335 | 16.8 .445 | 14.7 .591 | 13.2 .748 | 11.9 .930 | 10.7 1.12 | | | | | | | |
| | 0.072 | \boldsymbol{P} \mathcal{f} | | 117. .018 | 80.7 .032 | 70.0 .050 | 58.7 .077 | 50.2 .100 | 43.6 .130 | 35.2 .203 | 29.0 .294 | 25.0 .405 | 21.9 .521 | 19.5 .652 | 17.5 .802 | 16.0 .986 | | | | | | | |
| | 0.080 | \boldsymbol{P} \mathcal{f} | | | 121 .029 | 96.6 .045 | 80.5 .065 | 69.1 .090 | 60.4 .117 | 48.2 .183 | 48.2 .262 | 34.6 .359 | 30.1 .470 | 26.7 .593 | 24.2 .735 | 22.1 .886 | 20.2 1.105 | | | | | | |
| 140,000 | 0.092 | \boldsymbol{P} $\sqrt{ }$ | | | 171 .023 | 136 .037 | 113 .053 | 97.6 .072 | 85.5 .098 | 68.9 .148 | 57.3 .214 | 48.8 .291 | 42.6 .388 | 37.8 .481 | 34.5 .596 | 31.3 .720 | 28.6 .854 | | | | | | |
| | 0.093 | \boldsymbol{P} | | | 178 .023 | 142 .036 | 118 .052 | 99.5 .071 | 89.0 .093 | 71.2 .146 | 59.1 .211 | 50.9 .286 | 44.3 .376 | 39.6 .473 | 35.7 .585 | 32.3 .707 | 29.6 .841 | 27.3 .986 | | | | | |
| | 0.105 | \boldsymbol{P} f | | | | 204 .032 | 170 .047 | 147 .064 | 127 .083 | 102 .122 | 85.4 .188 | 73.0 .256 | 63.4 .336 | 56.6 .425 | 51.1 .512 | 46.3 .632 | 42.6 .755 | 38.9 .880 | | | | | |
| | 0.120 | \boldsymbol{P} \mathcal{f} | | | | 303 .028 | 253 .041 | 217 .055 | 190 .073 | 152 .114 | 126 .174 | 108 .223 | 95.2 .296 | 84.2 .368 | 76.2 .449 | 69.2 .551 | 63.5 .657 | 58.5 .768 | 54.3 .893 | | | | |
| | 0.125 | \boldsymbol{P} f | | | | | 286 .039 | 245 .053 | 214 .069 | 171 .109 | 143 .169 | 121 .213 | 107 .278 | 95.5 .353 | 85.2 .437 | 78.0 .528 | 71.5 .626 | 65.8 .731 | 60.8 .855 | 57.2 .981 | | | |
| | 0.135 | \boldsymbol{P} f | | | | | 359 .036 | 309 .049 | 270 .064 | 217 .106 | 171 .145 | 154 .198 | 135 .260 | 120 .327 | 108 .399 | 98.7 .486 | 90.2 .581 | 82.7 .680 | 72.2 .791 | 71.8 .908 | 67.5 1.04 | | |
| | 0.148 | \boldsymbol{P} $\sqrt{ }$ | | | | | | 408 .045 | 356 .059 | 285 .092 | 237 .132 | 207 .180 | 178 .236 | 158 .293 | 142 .370 | 130 .448 | 118 .530 | 109 .620 | 102 .723 | 95.0 .828 | 89.0 .945 | | |

Table 8.2.64 Safe Working Loads P and Deflections *f* of Cylindrical Helical Steel Springs of Circular Cross Section
(For closely coiled springs, divide given load and deflection values by the curvature factor *k.*)

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| | | Table 8.2.64 Safe Working Loads P and Deflections f of Cylindrical Helical Steel Springs of Circular Cross Section (Continued) | |
|--|--|--|--|
| | | | |

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Table 8.2.64 Safe Working Loads P and Deflections f of Cylindrical Helical Steel Springs of Circular Cross Section (Continued)

Table 8.2.65 Constants for Use in $S_v = 0.43A/d^m$

* Surface is smooth, free from defects, and has a bright, lustrous finish.

† Has a slight heat-treating scale which must be removed before plating.

Surface is smooth and bright, with no visible marks.

§ Aircraft-quality tempered wire; can also be obtained annealed.

¶ Tempered to Rockwell C49 but may also be obtained untempered. SOURCE: Adapted from ''Mechanical Engineering Design,'' Shigley, McGraw-Hill, 1983 by permission.

Fig. 8.2.120 Minimum tensile strength for the most popular spring materials, spring-quality wire. *(Reproduced from Carlson, ''Spring Designer's Handbook,'' Marcel Dekker, by permission.)*

Fig. 8.2.121 Springs in parallel and in series.

Fig. 8.2.122*a* Sectional view of Belleville spring.

Fig. 8.2.122*b* Load deflection curves for a family of Belleville springs. *(Associated Spring Corp.)*

springs are used for very high and special spring rates. They are extremely sensitive to slight variations in their geometry. A wide range is available commercially.

WIRE ROPE

When power source and load are located at extreme distances from one another, or loads are very large, the use of wire rope is suggested. Design and use decisions pertaining to wire ropes rest with the user, but manufacturers generally will help users toward appropriate choices. The following material, based on the Committee of Wire Rope Producers, ''Wire Rope User's Manual,'' 2d ed., 1981, may be used as an initial guide in selecting a rope.

Wire rope is composed of (1) wires to form a strand, (2) strands wound helically around a core, and (3) a core. Classification of wire ropes is made by giving the number of strands, number of minor strands in a major strand (if any), and nominal number of wires per strand. For example 6×7 rope means 6 strands with a nominal 7 wires per strand (in this case no minor strands, hence no middle number). A nominal value simply represents a range. A nominal value of 7 can mean anywhere from 3 to 14, of which no more than 9 are outside wires. A full Copyright (C) 1999 by The McGraw-Hill Companies, Inc. All rights reserved. Use of this product is subject to the terms of its License Agreement. [Click here to view.](#page-0-0)

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Fig. 8.2.123 Cross sections of some commonly used wire rope construction. *(Reproduced from ''Wire Rope User's Manual,'' AISI, by permission.)*

rope description will also include length, size (diameter), whether wire is preformed or not prior to winding, direction of lay (right or left, indicating the direction in which strands are laid around the core), grade of rope (which reflects wire strength), and core. The most widely used classifications are: 6×7 , 6×19 , 6×37 , 6×61 , 6×91 , 6×127 , $8 \times$ 19, 18 \times 7, 19 \times 7. Some special constructions are: 3 \times 7 (guardrail rope); 3×19 (slusher), 6×12 (running rope); 6×24 and 6×30 (hawsers); 6×42 and $6 \times 6 \times 7$ (tiller rope); $6 \times 3 \times 19$ (spring lay); 5×19 and 6×19 (marlin clad); $6 \times 25B$, $6 \times 27H$, and $6 \times 30G$ (flattened strand). The diameter of a rope is the circle which just contains the rope. The right-regular lay (in which the wire is twisted in one direction to form the strands and the strands are twisted in the opposite direction to form the rope) is most common. Regular-lay ropes do not kink or untwist and handle easily. Lang-lay ropes (in which wires and strands are twisted in the same direction) are more resistant to abrasive wear and fatigue failure.

Cross sections of some commonly used wire rope are shown in [Fig.](#page-75-0) [8.2.123.](#page-75-0) Figure 8.2.124 shows rotation-resistant ropes, and Fig. 8.2.125 shows some special-purpose constructions.

The core provides support for the strands under normal bending and loading. Core materials include fibers (hard vegetable or synthetic) or steel (either a strand or an independent wire rope). Most common core designations are: fiber core (FC), independent wire-rope core (IWRC), and wire-strand core (WSC). Lubricated fiber cores can provide lubrication to the wire, but add no real strength and cannot be used in high temperature environments. Wire-strand or wire-rope cores add from 7 to 10 percent to strength, but under nonstationary usage tend to wear from interface friction with the outside strands. Great flexibility can be achieved when wire rope is used as strands. Such construction is very pliable and friction resistant. Some manufacturers will provide plastic coatings (nylon, Teflon, vinyl, etc.) upon request. Such coatings help provide resistance to abrasion, corrosion, and loss of lubricant. *Crushing* refers to rope damage caused by excessive pressures against drum or sheave, improper groove size, and multiple layers on drum or sheave. Consult wire rope manufacturers in doubtful situations.

Wire-rope materials and their strengths are reflected as grades. These are: traction steel (TS), mild plow steel (MPS), plow steel (PS), improved plow steel (IPS), and extra improved plow (EIP). The plow steel strength curve forms the basis for calculating the strength of all steel rope wires. American manufacturers use color coding on their ropes to identify particular grades.

The grades most commonly available and tabulated are IPS and EIP. Two specialized categories, where selection requires extraordinary attention, are elevator and rotation-resistant ropes.

Elevator rope can be obtained in four principal grades: iron, traction steel, high-strength steel, and extra-high-strength steel.

Bronze rope has limited use; iron rope is used mostly for older existing equipment.

Selection of Wire Rope

Appraisal of the following is the key to choosing the rope best suited to the job: resistance to breaking, resistance to bending fatigue, resistance to vibrational fatigue, resistance to abrasion, resistance to crushing, and reserve strength. Along with these must be an appropriate choice of safety factor, which in turn requires careful consideration of all loads, acceleration-deceleration, shocks, rope speed, rope attachments, sheave

Fig. 8.2.124 Cross section of some rotation-resistant wire ropes. *(Reproduced from ''Wire Rope User's Manual,'' AISI, by permission.)*

Fig. 8.2.125 Some special constructions. *(Reproduced from ''Wire Rope User's Manual,'' AISI, by permission.)*

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SOURCE: ''Wire Rope User's Manual,'' AISI, adapted by permission.

arrangements as well as their number and size, corrosive and/or abrasive environment, length of rope, etc. An approximate selection formula can be written as:

$$
DSL = \frac{(NS)K_b}{K_{sf}}
$$

where DSL (demanded static load) $=$ known or dead load **plus** additional loads caused by sudden starts or stops, shocks, bearing friction, etc., tons; NS (nominal strength) $=$ published test strengths, tons (see [Table 8.2.66\)](#page-77-0); $K_b = a$ factor to account for the reduction in nominal strength due to bending when a rope passes over a curved surface such as a stationary sheave or pin (see Fig. 8.2.126); $K_{\text{sf}} =$ safety factor. (For average operation use $K_{\text{sf}} = 5$. If there is danger to human life or other critical situations, use $8 \leq K_{\text{sf}} \leq 12$. For instance, for elevators moving at 50 ft/min, $K_{\text{sf}} = 8$, while for those moving at 1,500 ft/min, $K_{\text{sf}} = 12$.)

Having made a tentative selection of a rope based on the demanded static load, one considers next the wear life of the rope. A loaded rope

Fig. 8.2.126 Values of K_{bend} vs. *D/d* ratios (*D* = sheave diameter, d = rope diameter), based on standard test data for 6 3 9 and 6 3 17 class ropes. *(Compiled from ''Wire Rope User's Manual,'' AISI, by permission.)*

bent over a sheave stretches elastically and so rubs against the sheave, causing wear of both members. Drum or sheave size is of paramount importance at this point.

Sizing of Drums or Sheaves

Diameters of drums or sheaves in wire rope applications are controlled by two main considerations: (1) the radial pressure between rope and groove and (2) degree of curvature imposed on the rope by the drum or sheave size.

Radial pressures can be calculated from $p = 2T/(Dd)$, where $p = \text{unit}$ radial pressure, lb/in²; $T =$ rope load, lb; $D =$ tread diameter of drum or sheave, in; $d =$ nominal diameter of rope, in. Table 8.2.67 lists suggested allowable radial bearing pressures of ropes on various sheave materials.

All wire ropes operating over drums or sheaves are subjected to cyclical stresses, causing shortened rope life because of fatigue. Fatigue resistance or relative service life is a function of the ratio *D*/*d*. Adverse effects also arise out of relative motion between strands during passage around the drum or sheave. Additional adverse effects can be traced to poor match between rope and groove size, and to lack of rope lubrication. Table 8.2.68 lists suggested and minimum sheave and drum ratios for various rope construction[. Table 8.2.69](#page-79-0) lists relative bending life factors[; Figure 8.2.127](#page-79-0) shows a plot of relative rope service life versus *D*/*d*[. Table 8.2.70](#page-79-0) lists minimum drum (sheave) groove dimensions. Periodic groove inspection is recommended, and worn or corrugated grooves should be remachined or the drum replaced, depending on severity of damage.

Seizing and Cutting Wire Rope Before a wire rope is cut, seizings (bindings) must be applied on either side of the cut to prevent rope distortion and flattening or loosened strands. Normally, for preformed ropes, one seizing on each side of the cut is sufficient, but for ropes that

Table 8.2.68 Sheave and Drum Ratios

| Construction* | Suggested | Minimum |
|---|-----------|---------|
| 6×7 | 72 | 42 |
| 19×7 or 18×7 Rotation-resistant | 51 | 34 |
| 6×19 S | 51 | 34 |
| 6×25 B flattened strand | 45 | 30 |
| 6×27 H flattened strand | 45 | 30 |
| 6×30 G flattened strand | 45 | 30 |
| 6×21 FW | 45 | 30 |
| 6×26 WS | 45 | 30 |
| 6×25 FW | 39 | 26 |
| 6×31 WS | 39 | 26 |
| 6×37 SFW | 39 | 26 |
| 6×36 WS | 35 | 23 |
| 6×43 FWS | 35 | 23 |
| 6×41 WS | 32 | 21 |
| 6×41 SFW | 32 | 21 |
| 6×49 SWS | 32 | 21 |
| 6×46 SFW | 28 | 18 |
| 6×46 WS | 28 | 18 |
| $8 \times 19S$ | 41 | 27 |
| 8×25 FW | 32 | 21 |
| 6×42 Tiller | 21 | 14 |

* WS—Warrington Seale; FWS—Filler Wire Seale; SFW—Seale Filler Wire; SWS—Seale Warrington Seale; S—Seale; FW—Filler Wire.

 $\dagger D$ = tread diameter of sheave; d = nominal diameter of rope. To find any tread diameter from this table, the diameter for the rope construction to be used is multiplied by its nominal diameter *d*. For example, the minimum sheave tread diameter for a $\frac{1}{2}$ -in 6 \times 21 FW rope would be $\frac{1}{2}$ in (nominal diameter) \times 30 (minimum ratio), or 15 in.

NOTE: These values are for reasonable service. Other values are permitted by various standards such as ANSI, API, PCSA, HMI, CMAA, etc. Similar values affect rope life.

SOURCE: ''Wire Rope User's Manual,'' AISI, reproduced by permission.

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Table 8.2.69 Relative Bending Life Factors

| Rope construction | Factor | Rope construction | Factor | |
|----------------------------------|--------|-------------------------|--------|--|
| 6×7 | 0.61 | 6×36 WS | 1.16 | |
| 19×7 or 18×7 | 0.67 | 6×43 FWS | 1.16 | |
| Rotation-resistant | 0.81 | 6×41 WS | 1.30 | |
| 6×19 S | 0.90 | 6×41 SFW | 1.30 | |
| 6×25 B flattened strand | 0.90 | 6×49 SWS | 1.30 | |
| 6×27 H flattened strand | 0.90 | 6×43 FW (2 op) | 1.41 | |
| 6×30 G flattened strand | 0.89 | 6×46 SFW | 1.41 | |
| 6×21 FW | 0.89 | 6×46 WS | 1.41 | |
| 6×26 WS | 1.00 | $8 \times 19S$ | 1.00 | |
| 6×25 FW | 1.00 | 8×25 FW | 1.25 | |
| 6×31 WS | 1.00 | 6×42 Tiller | 2.00 | |
| 6×37 SFW | | | | |

SOURCE: ''Wire Rope User's Manual,'' AISI, reproduced by permission.

Table 8.2.70 Minimum Sheave- and Drum-Groove Dimensions*

| Nominal rope diameter | | Groove radius | | | | | | | |
|--------------------------|------|---------------|-------|-------|-------|--|--|--|--|
| | | | New | Worn | | | | | |
| in | nm | in | mm | in | mm | | | | |
| $\frac{1}{4}$ | 6.4 | 0.135 | 3.43 | .129 | 3.28 | | | | |
| $\frac{5}{16}$ | 8.0 | 0.167 | 4.24 | .160 | 4.06 | | | | |
| $\frac{3}{8}$ | 9.5 | 0.201 | 5.11 | .190 | 4.83 | | | | |
| $\frac{7}{16}$ | 11 | 0.234 | 5.94 | .220 | 5.59 | | | | |
| $\frac{1}{2}$ | 13 | 0.271 | 6.88 | .256 | 6.50 | | | | |
| $\frac{9}{16}$ | 14.5 | 0.303 | 7.70 | .288 | 7.32 | | | | |
| $\frac{5}{8}$ | 16 | 0.334 | 8.48 | .320 | 8.13 | | | | |
| $\frac{3}{4}$ | 19 | 0.401 | 10.19 | .380 | 9.65 | | | | |
| $\frac{7}{8}$ | 22 | 0.468 | 11.89 | .440 | 11.18 | | | | |
| 1 | 26 | 0.543 | 13.79 | .513 | 13.03 | | | | |
| $1\frac{1}{8}$ | 29 | 0.605 | 15.37 | .577 | 14.66 | | | | |
| $1\frac{1}{4}$ | 32 | 0.669 | 16.99 | .639 | 16.23 | | | | |
| $1\frac{3}{8}$ | 35 | 0.736 | 18.69 | .699 | 17.75 | | | | |
| $1\frac{1}{2}$ | 38 | 0.803 | 20.40 | .759 | 19.28 | | | | |
| $1\frac{5}{8}$ | 42 | 0.876 | 22.25 | .833 | 21.16 | | | | |
| $1\frac{3}{4}$ | 45 | 0.939 | 23.85 | .897 | 22.78 | | | | |
| 1% | 48 | 1.003 | 25.48 | .959 | 24.36 | | | | |
| \overline{c} | 52 | 1.085 | 27.56 | 1.025 | 26.04 | | | | |
| $2\frac{1}{8}$ | 54 | 1.137 | 28.88 | 1.079 | 27.41 | | | | |
| $2\frac{1}{4}$ | 58 | 1.210 | 30.73 | 1.153 | 29.29 | | | | |
| $2\frac{3}{8}$ | 60 | 1.271 | 32.28 | 1.199 | 30.45 | | | | |
| $2\frac{1}{2}$ | 64 | 1.338 | 33.99 | 1.279 | 32.49 | | | | |
| $2^{5/8}$ | 67 | 1.404 | 35.66 | 1.339 | 34.01 | | | | |
| $2^{3/4}$ | 71 | 1.481 | 37.62 | 1.409 | 35.79 | | | | |
| $2\frac{7}{8}$ | 74 | 1.544 | 39.22 | 1.473 | 37.41 | | | | |
| 3 | 77 | 1.607 | 40.82 | 1.538 | 39.07 | | | | |
| $3\frac{1}{8}$ | 80 | 1.664 | 42.27 | 1.598 | 40.59 | | | | |
| $3\frac{1}{4}$ | 83 | 1.731 | 43.97 | 1.658 | 42.11 | | | | |
| $3\frac{3}{8}$ | 87 | 1.807 | 45.90 | 1.730 | 43.94 | | | | |
| $3\frac{1}{2}$ | 90 | 1.869 | 47.47 | 1.794 | 45.57 | | | | |
| $3^{3}/_{4}$ | 96 | 1.997 | 50.72 | 1.918 | 48.72 | | | | |
| 4 | 103 | 2.139 | 54.33 | 2.050 | 52.07 | | | | |
| $4\frac{1}{4}$ | 109 | 2.264 | 57.51 | 2.178 | 55.32 | | | | |
| $4\frac{1}{2}$ | 115 | 2.396 | 60.86 | 2.298 | 58.37 | | | | |
| $4^{3}/_{4}$ | 122 | 2.534 | 64.36 | 2.434 | 61.82 | | | | |
| 5 | 128 | 2.663 | 67.64 | 2.557 | 64.95 | | | | |
| $5\frac{1}{4}$ | 135 | 2.804 | 71.22 | 2.691 | 68.35 | | | | |
| $5\frac{1}{2}$ | 141 | 2.929 | 74.40 | 2.817 | 71.55 | | | | |
| $5^{3}/_{4}$ | 148 | 3.074 | 78.08 | 2.947 | 74.85 | | | | |
| 6 | 154 | 3.198 | 81.23 | 3.075 | 78.11 | | | | |

* Values given are applicable to grooves in sheaves and drums; they are not generally suitable for pitch design since this may involve other factors. Further, the dimensions do not apply to traction-type elevators; in this circumstance, drum- and sheave-groove tolerances should conform to the elevator manufacturer's specifications. Modern drum design embraces extensive considerations beyond the scope of this publication. It should also be noted that drum grooves are now produced with a number of oversize dimensions and pitches applicable to certain service requirements.

SOURCE: ''Wire Rope User's Manual,'' AISI, reproduced by permission.

are not preformed a minimum of two seizings on each side is recommended, and these should be spaced six rope diameters apart (see Fig. 8.2.128). Seizings should be made of soft or annealed wire or strand, and the width of the seizing should never be less than the diameter of the rope being seized[. Table 8.2.71](#page-80-0) lists suggested seizing wire diameters.

Wire Rope Fittings or Terminations End terminations allow forces to be transferred from rope to machine, or load to rope, etc. [Figure](#page-80-0) [8.2.129](#page-80-0) illustrates the most commonly used end fittings or terminations. Not all terminations will develop full strength. In fact, if all of the rope elements are not held securely, the individual strands will sustain unequal loads causing unequal wear among them, thus shortening the effective rope service life. Socketing allows an end fitting which reduces the chances of unequal strand loading.

Fig. 8.2.127 Service life curves for various *D*/*d* ratios. Note that this curve takes into account only bending and tensile stresses. *(Reproduced from ''Wire Rope User's Manual,'' AISI, by permission.)*

Wire rope manufacturers have developed a recommended procedure for socketing. A tight wire serving band is placed where the socket base will be, and the wires are unlaid, straightened, and ''broomed'' out. Fiber core is cut close to the serving band and removed, wires are cleaned with a solvent such as SC-methyl chloroform, and brushed to remove dirt and grease. If additional cleaning is done with muriatic acid this must be followed by a neutralizing rinse (if possible, ultrasonic cleaning is preferred). The wires are dipped in flux, the socket is positioned, zinc (spelter) is poured and allowed to set, the serving band is removed, and the rope lubricated.

A somewhat similar procedure is used in thermoset resin socketing. Socketed terminations generally are able to develop 100 percent of nominal strength.

Fig. 8.2.128 Seizings. *(Reproduced from ''Wire Rope User's Manual,'' AISI, by permission.)*

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Fig. 8.2.129 End fittings, or terminations, showing the six most commonly used. *(Reproduced from ''Wire Rope User's Manual,'' AISI, by permission.)*

Table 8.2.72 Breaking Strength of Fiber Lines, Lb

Table 8.2.71 Seizing*

* Length of the seizing should not be less than the rope diameter. † The diameter of seizing wire for elevator ropes is usually somewhat smaller than that shown in this table. Consult the wire rope manufacturer for specific size recommendations. Soft annealed seizing strand may also be used.

SOURCE: ''Wire Rope User's Manual,'' AISI, reproduced by permission.

FIBER LINES

The breaking strength of various fiber lines is given in Table 8.2.72.

Knots, Hitches, and Bends

No two parts of a knot which would move in the same direction if the rope were to slip should lie alongside of and touching each other. The knots shown in [Fig. 8.2.130](#page-81-0) are known by the following

A, bight of a rope; *B*, simple or overhand knot; *C*, figure 8 knot; *D*, double knot; *E*, boat knot; *F*, bowline, first step; *G*, bowline, second step; *H*, bowline, completed; *I*, square or reef knot; *J*, sheet bend or weaver's knot; *K*, sheet bend with a toggle; *L*, carrick bend;

Breaking strength is the maximum load the line will hold at the time of breaking. The working load of a line is one-fourth to one-fifth of the breaking strength. SOURCE: Adapted, by permission of the U.S. Naval Institute, Annapolis, MD, and Wall Rope Works, Inc., New York, NY.

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Fig. 8.2.130 Knots, hitches, and bends.

M, ''stevedore'' knot completed; *N*, ''stevedore'' knot commenced; *O*, slip knot; *P*, Flemish loop; *Q*, chain knot with toggle; *R*, half hitch; *S*, timber hitch; *T*, clove hitch; *U*, rolling hitch; *V*, timber hitch and half hitch; *W*, blackwall hitch; *X*, fisherman's bend; *Y*, round

Table 8.2.73 Wire Nails for Special Purposes (Steel wire gage)

turn and half hitch; *Z*, wall knot commenced; *AA*, wall knot completed; *BB*, wall-knot crown commenced; *CC*, wall-knot crown completed.

The bowline *H*, one of the most useful knots, will not slip, and after being strained is easily untied. Knots *H*, *K*, and *M* are easily untied after being under strain. The knot *M* is useful when the rope passes through an eye and is held by the knot, as it will not slip, and is easily untied after being strained. The wall knot is made as follows: Form a bight with strand 1 and pass the strand 2 around the end of it, and the strand 3 around the end of 2, and then through the bight of 1, as shown at *Z* in the figure. Haul the ends taut when the appearance is as shown in *AA*. The end of the strand 1 is now laid over the center of the knot, strand 2 laid over 1, and 3 over 2, when the end of 3 is passed through the bight of 1, as shown at *BB*. Haul all the strands taut, as shown at *CC*. The ''stevedore'' knot (*M*, *N*) is used to hold the end of a rope from passing through a hole. When the rope is strained, the knot draws up tight, but it can be easily untied when the strain is removed. If a knot or hitch of any kind is tied in a rope, its failure under stress is sure to occur at that place. The shorter the bend in the standing rope, the weaker is the knot. The approximate strength of knots compared with the full strength of (dry) rope $(= 100)$, based on Miller's experiments (*Mach.,* 1900, p. 198), is as follows: eye splice over iron thimble, 90; short splice in rope, 80; *S* and *Y*, 65; *H*, *O*, and *T*, 60; *I* and *J*, 50; *B* and *P*, 45.

NAILS AND SPIKES

Nails are either **wire nails** of circular cross section and constant diameter or **cut nails** of rectangular cross section with taper from head to point. The larger sizes are called **spikes.** The length of the nail is expressed in the **''penny''** system, the equivalents in inches being given in Tables 8.2.73 to 8.2.75. The letter d is the accepted symbol for penny. A keg of nails weighs 100 lb. **Heavy hinge nails** or **track nails** with countersunk heads have chisel points unless diamond points are specified. **Plasterboard nails** are smooth with circumferential grooves and have diamond points. **Spikes** are made either with flat heads and diamond points or with oval heads and chisel points.

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Table 8.2.74 Wire Nails and Spikes

(Steel wire gage)

Table 8.2.75 Cut Steel Nails and Spikes (Sizes, lengths, and approximate number per lb)

WIRE AND SHEET-METAL GAGES

In the metal industries, the word *gage* has been used in various systems, or scales, for expressing the thickness or weight per unit area of thin plates, sheet, and strip, or the diameters of rods and wire. Specific diameters, thicknesses, or weights per square foot have been or are denoted in gage systems by certain numerals followed by the word *gage,* for example, no. 12 gage, or simply 12 gage. Gage numbers for flat rolled products have been used only in connection with thin materials (Table 8.2.76). Heavier and thicker, flat rolled materials are usually designated by thickness in English or metric units.

There is considerable danger of confusion in the use of gage number in both foreign and domestic trade, which can be avoided by specifying thickness or diameter in inches or millimeters.

DRILL SIZES

Se[e Table 8.2.77.](#page-85-0)

* Principal uses—BWG: strips, bands, hoops, and wire; AWG or B&S: nonferrous sheets, rod, and wire; U.S. Steel Wire: steel wire except music wire; manufacturers' standard: uncoated steel sheets.

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Table 8.2.77 Diameters of Small Drills

Number, letter, metric, and fractional drills in order of size (rounded to 4 decimal places)

| No. | Ltr | mm | in | Diam, in | No. | Ltr | $\rm mm$ | in | Diam, in | No. | Ltr | mm | in | Diam, in |
|-----|---------------|------|----------------|----------|-----|-------------|----------|----------------|----------|-----|-----|-------|---------------|----------|
| | | | 19/64 | 0.2968 | | | 9.70 | | 0.3819 | | | 17.00 | | 0.6693 |
| | | 7.60 | | 0.2992 | | | 9.75 | | 0.3838 | | | | 43/64 | 0.6718 |
| | ${\bf N}$ | | | 0.3020 | | | 9.80 | | 0.3858 | | | | 11/16 | 0.6875 |
| | | 7.70 | | 0.3031 | | W | | | 0.3860 | | | 17.50 | | 0.6890 |
| | | 7.75 | | 0.3051 | | | 9.90 | | 0.3898 | | | | 45/64 | 0.7031 |
| | | 7.80 | | 0.3071 | | | | 25/64 | 0.3906 | | | 18.00 | | 0.7087 |
| | | 7.90 | | 0.3110 | | | 10.00 | | 0.3937 | | | | 23/32 | 0.7187 |
| | | | $\frac{5}{16}$ | 0.3125 | | X | | | 0.3970 | | | 18.50 | | 0.7283 |
| | | 8.00 | | 0.3150 | | $\mathbf Y$ | | | 0.4040 | | | | 47/64 | 0.7374 |
| | $\mathbf O$ | | | 0.3160 | | | | 13/32 | 0.4062 | | | 19.00 | | 0.7480 |
| | | 8.10 | | 0.3189 | | Z | | | 0.4130 | | | | $\frac{3}{4}$ | 0.7500 |
| | | 8.20 | | 0.3228 | | | 10.50 | | 0.4134 | | | | 49/64 | 0.7656 |
| | $\, {\bf P}$ | | | 0.3230 | | | | 27/64 | 0.4218 | | | 19.50 | | 0.7677 |
| | | 8.25 | | 0.3248 | | | 11.00 | | 0.4331 | | | | 25/32 | 0.7812 |
| | | 8.30 | | 0.3268 | | | | $\frac{7}{16}$ | 0.4375 | | | 20.00 | | 0.7874 |
| | | | 21/64 | 0.3281 | | | 11.50 | | 0.4528 | | | | 51/64 | 0.7968 |
| | | 8.40 | | 0.3307 | | | | 29/64 | 0.4531 | | | 20.50 | | 0.8070 |
| | Q | | | 0.3320 | | | | 15/32 | 0.4687 | | | | 13/16 | 0.8125 |
| | | 8.50 | | 0.3346 | | | 12.00 | | 0.4724 | | | 21.00 | | 0.8267 |
| | | 8.60 | | 0.3386 | | | | 31/64 | 0.4843 | | | | 53/64 | 0.8281 |
| | ${\mathbb R}$ | | | 0.3390 | | | 12.50 | | 0.4921 | | | | 27/32 | 0.8437 |
| | | 8.70 | | 0.3425 | | | | $\frac{1}{2}$ | 0.5000 | | | 21.50 | | 0.8464 |
| | | | 11/32 | 0.3437 | | | 13.00 | | 0.5118 | | | | 55/64 | 0.8593 |
| | | 8.75 | | 0.3444 | | | | 33/64 | 0.5156 | | | 22.00 | | 0.8661 |
| | | 8.80 | | 0.3464 | | | | 17/32 | 0.5312 | | | | $\frac{7}{8}$ | 0.8750 |
| | $\mathbf S$ | | | 0.3480 | | | 13.50 | | 0.5315 | | | 22.50 | | 0.8858 |
| | | 8.90 | | 0.3504 | | | | 35/64 | 0.5468 | | | | 57/64 | 0.8906 |
| | | 9.00 | | 0.3543 | | | 14.00 | | 0.5512 | | | 23.00 | | 0.9055 |
| | $\mathbf T$ | | | 0.3580 | | | | $\frac{9}{16}$ | 0.5625 | | | | 29/32 | 0.9062 |
| | | 9.10 | | 0.3583 | | | 14.50 | | 0.5708 | | | | 59/64 | 0.9218 |
| | | | 23/64 | 0.3593 | | | | 37/64 | 0.5781 | | | 23.50 | | 0.9251 |
| | | 9.20 | | 0.3622 | | | 15.00 | | 0.5905 | | | | 15/16 | 0.9375 |
| | | 9.25 | | 0.3641 | | | | 19/32 | 0.5937 | | | 24.00 | | 0.9448 |
| | | 9.30 | | 0.3661 | | | | 39/64 | 0.6093 | | | | 61/64 | 0.9531 |
| | U | | | 0.3680 | | | 15.50 | | 0.6102 | | | 24.50 | | 0.9646 |
| | | 9.40 | | 0.3701 | | | | $5/8$ | 0.6250 | | | | 31/32 | 0.9687 |
| | | 9.50 | | 0.3740 | | | 16.00 | | 0.6299 | | | 25.00 | | 0.9842 |
| | | | $\frac{3}{8}$ | 0.3750 | | | | 41/64 | 0.6406 | | | | 63/64 | 0.9843 |
| | V | | | 0.3770 | | | 16.50 | | 0.6496 | | | | 1.0 | 1.0000 |
| | | 9.60 | | 0.3780 | | | | 21/32 | 0.6562 | | | 25.50 | | 1.0039 |

Table 8.2.77 Diameters of Small Drills (*Continued***)**

SOURCE: Adapted from Colvin and Stanley, ''American Machinists' Handbook,'' 8th ed., McGraw-Hill, New York, 1945.

8.3 GEARING

by George W. Michalec

REFERENCES: Buckingham, ''Manual of Gear Design,'' Industrial Press. Cunningham, Noncircular Gears, *Mach. Des.,* Feb. 19, 1957. Cunningham and Cunningham, Rediscovering the Noncircular Gear, *Mach. Des.,* Nov. 1, 1973. Dudley, ''Gear Handbook,'' McGraw-Hill. Dudley, ''Handbook of Practical Gear Design,'' McGraw-Hill. Michalec, ''Precision Gearing: Theory and Practice,'' Wiley. Shigely, ''Engineering Design,'' McGraw-Hill. AGMA Standards. ''Gleason Bevel and Hypoid Gear Design,'' Gleason Works, Rochester. ''Handbook of Gears: Inch and Metric'' and ''Elements of Metric Gear Technology,'' Designatronics, New Hyde Park, NY. Adams, ''Plastics Gearing: Selection and Application,'' Marcel Dekker.

Notation

- $a =$ addendum
- $b =$ dedendum
- $B =$ backlash, linear measure along pitch circle
- $c =$ clearance
- $C =$ center distance
- $d =$ pitch diam of pinion
- d_b = base circle diam of pinion
- d_{ρ} = outside diam of pinion
- d_r = root diam of pinion
- $D =$ pitch diameter of gear
- D_P = pitch diam of pinion
- D_G = pitch diam of gear
- D_o = outside diam of gear
- D_b = base circle diam of gear
- D_t = throat diam of wormgear
- $F =$ face width
- h_k = working depth
- $h_t =$ whole depth
- inv $\dot{\phi}$ = involute function (tan $\phi \phi$)

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- $l =$ lead (advance of worm or helical gear in 1 rev)
- $l_p(l_G)$ = lead of pinion (gear) in helical gears
	- $L =$ lead of worm in one revolution
	- $m =$ module
	- m_G = gear ratio ($m_G = N_G/N_P$)
	- m_p = contact ratio (of profiles)
	- \dot{M} = measurement of over pins
- $n_P(n_G)$ = speed of pinion (gear), r/min
- $N_P(N_G)$ = number of teeth in pinion (gear)
	- n_w = number of threads in worm
		- $p =$ circular pitch
		- p_b = base pitch
		- p_n = normal circular pitch of helical gear
		- P_d = diametral pitch
		- P_{dn} = normal diametral pitch
		- \ddot{R} = pitch radius
		- R_c = radial distance from center of gear to center of measuring pin
- $R_P(R_G)$ = pitch radius of pinion (gear)
	- R_T = testing radius when rolled on a variable-center-distance inspection fixture
	- $s =$ stress
	- $t =$ tooth thickness
	- t_n = normal circular tooth thickness
- $T_p(T_G)$ = formative number of teeth in pinion (gear) (in bevel gears)
	- $v =$ pitch line velocity
	- $X =$ correction factor for profile shift
	- α = addendum angle of bevel gear
	- γ = pitch angle of bevel pinion
	- γ_R = face angle at root of bevel pinion tooth
	- γ_o = face angle at tip of bevel pinion tooth Γ = pitch angle of bevel gear
	-
	- Γ_R = face angle at root of bevel gear tooth
	- Γg_o = face angle at tip of bevel gear tooth
	- δ = dedendum angle of bevel gear
	- $\overline{\Delta C}$ = relatively small change in center distance *C*
	- ϕ = pressure angle
	- ϕ_n = normal pressure angle
	- ψ = helix or spiral angle
- $\psi_P(\psi_G)$ = helix angle of teeth in pinion (gear)
	- Σ = shaft angle of meshed bevel pair

BASIC GEAR DATA

Gear Types Gears are grouped in accordance with tooth forms, shaft arrangement, pitch, and quality. Tooth forms and shaft arrangements are:

Pitch definitions (see Fig. 8.3.1). **Diametral pitch** P_d is the ratio of number of teeth in the gear to the diameter of the pitch circle *D* measured in inches, $P_d = N/D$. **Circular pitch** *p* is the linear measure in inches along the pitch circle between corresponding points of adjacent teeth. From these definitions, $P_d p = \pi$. The base pitch p_b is the distance along the line of action between successive involute tooth surfaces. The base and circular pitches are related as $p_b = p \cos \phi$, where $\phi =$ the pressure angle.

Pitch circle is the imaginary circle that rolls without slippage with a pitch circle of a mating gear. The pitch (circle) diameter equals $D = N/P_d = Np/\pi$. The basic relation between P_d and p is $P_d p = \pi$.

Tooth size is related to pitch. In terms of diametral pitch P_d , the relationship is inverse; i.e., large P_d implies a small tooth, and small P_d implies a large tooth. Conversely, there is a direct relationship between tooth size and circular pitch p . A small tooth has a small p , but a large tooth has a large p . (See Fig. 8.3.1*b*.) In terms of P_d , coarse teeth comprise P_d less than 20; fine teeth comprise P_d of 20 and higher. (See Fig. 8.3.1*b*.) **Quality** of gear teeth is classified as commercial, precision, and ultraprecision.

Fig. 8.3.1*a* Basic gear geometry and nomenclature.

| $P_{d} = 10$ | $P_{d} = 20$ |
|--------------|--------------|
| $p = 0.3142$ | $p = 0.1571$ |

Fig. 8.3.1*b* Comparison of pitch and tooth size.

Pressure angle ϕ for all gear types is the acute angle between the common normal to the profiles at the contact point and the common pitch plane. For spur gears it is simply the acute angle formed by the common tangent between base circles of mating gears and a normal to the line of centers. For standard gears, pressure angles of 141⁄2°, 20°, and 25° have been adopted by ANSI and the gear industry (see Fig. 8.3.1*a*). The 20° pressure angle is most widely used because of its versatility. The higher pressure angle 25° provides higher strength for highly loaded gears. Although 141⁄2° appears in standards, and in past decades was extensively used, it is used much less than 20°. The 141⁄2° standard is still used for replacement gears in old design equipment, in applications where backlash is critical, and where advantage can be taken of lower backlash with change in center distance.

The **base circle** (or **base cylinder**) is the circle from which the involute tooth profiles are generated. The relationship between the base-circle and pitch-circle diameter is $D_b = D \cos \phi$.

Tooth proportions are established by the addendum, dedendum, working depth, clearance, tooth circular thickness, and pressure angle (see Fig. 8.3.1). In addition, gear face width *F* establishes thickness of the gear measured parallel to the gear axis.

For involute teeth, proportions have been standardized by ANSI and AGMA into a limited number of systems using a basic rack for specification (see Fig. 8.3.2 and Table 8.3.1). Dimensions for the basic rack are normalized for diametral pitch $= 1$. Dimensions for a specific pitch are

Fig. 8.3.2 Basic rack for involute gear systems. $a =$ addendum; $b =$ dedendum; $c =$ clearance; $h_k =$ working depth; $h_t =$ whole depth; $p =$ circular pitch; r_f = fillet radius; *t* = tooth thickness; ϕ = pressure angle.

obtained by dividing by the pitch. Standards for basic involute spur, helical and face gear designs, and noninvolute bevel and wormgear designs are listed in Table 8.3.2.

Gear ratio (or **mesh ratio**) m_G is the ratio of number of teeth in a meshed pair, expressed as a number greater than 1 ; $m_G = N_G/N_P$, where the pinion is the member having the lesser number of teeth. For spur and parallel-shaft helical gears, the base circle ratio must be identical to the gear ratio. The speed ratio of gears is inversely proportionate to their numbers of teeth. Only for standard spur and parallel-shaft helical gears is the pitch diameter ratio equal to the gear ratio and inversely proportionate to the speed ratio.

Metric Gears—Tooth Proportions and Standards

Metric gearing not only is based upon different units of length measure but also involves its own unique design standard. This means that metric gears and American-standard-inch diametral-pitch gears are not interchangeable.

In the metric system the *module m* is analogous to pitch and is defined as

 $m = \frac{D}{N}$ = mm of pitch diameter per tooth

Note that, for the module to have proper units, the pitch diameter must be in millimeters.

The **metric module** was developed in a number of versions that differ in minor ways. The German DIN standard is widely used in Europe and other parts of the world. The Japanese have their own version defined in JS standards. Deviations among these and other national standards are minor, differing only as to dedendum size and root radii. The differences have been resolved by the new unified module standard promoted by the International Standards Organization (ISO). This unified version (Fig. 8.3.3) conforms to the new SI in all respects. All major industrial

Fig. 8.3.3 The ISO basic rack for metric module gears.

countries on the metric system have shifted to this ISO standard, which also is the basis for American metric gearing[. Table 8.3.3](#page-89-0) lists pertinent current ISO metric standards.

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Table 8.3.3 ISO Metric Gearing Standards

Tooth proportions for standard spur and helical gears are given in terms of the basic rack. Dimensions, in millimeters, are normalized for module $m = 1$. Corresponding values for other modules are obtained by multiplying each dimension by the value of the specific module *m*. Major tooth parameters are described by this standard:

Tooth form: Straight-sided and full-depth, forming the basis of a family of full-depth interchangeable gears.

Pressure angle: 20°, conforming to worldwide acceptance.

Addendum: Equal to module *m*, which corresponds to the American practice of $1/P_d =$ addendum.

Dedendum: Equal to 12.5*m*, which corresponds to the American practice of $1.25/P_d =$ dedendum.

Root radius: Slightly greater than American standards specifications. **Tip radius:** A maximum is specified, whereas American standards do not specify. In practice, U.S. manufacturers can specify a tip radius as near zero as possible.

Note that the basic racks for metric and American inch gears are essentially identical, but metric and American standard gears are not interchangeable.

The preferred standard gears of the metric system are not interchangeable with the preferred diametral-pitch sizes. Table 8.3.4 lists commonly used pitches and modules of both systems (preferred values are boldface).

Metric gear use in the United States, although expanding, is still a small percentage of total gearing. Continuing industry conversions and imported equipment replacement gearing are building an increasing demand for metric gearing. The reference list cites a domestic source of stock metric gears of relatively small size, in medium and fine pitches. Large diameter coarse pitch metric gears are made to order by many gear fabricators.

Table 8.3.4 Metric and American Gear Equivalents

FUNDAMENTAL RELATIONSHIPS OF SPUR AND HELICAL GEARS 8-91

Table 8.3.4 Metric and American Gear Equivalents (*Continued***)**

FUNDAMENTAL RELATIONSHIPS OF SPUR AND HELICAL GEARS

Center distance is the distance between axes of mating gears and is determined from $C = (n_G + N_P)/(2P_d)$, or $C = (D_G + D_P)/2$. Deviation from ideal center distance of involute gears is not detrimental to proper (conjugate) gear action which is one of the prime superiority features of the involute tooth form.

Contact Ratio Referring to the top part of Fig. 8.3.4 and assuming no tip relief, the pinion engages in the gear at *a*, where the outside circle of the gear tooth intersects the line of action *ac*. For the usual spur gear and pinion combinations there will be two pairs of teeth theoretically in contact at engagement (a gear tooth and its mating pinion tooth considered as a pair). This will continue until the pair ahead (bottom part of Fig. 8.3.4) disengages at *c*, where the outside circle of the pinion intersects the line of action *ac*, the movement along the line of action being

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ab. After disengagement the pair behind will be the only pair in contact until another pair engages, the movement along the line of action for single-pair contact being *bd*. Two pairs are theoretically in contact during the remaining intervals, $ab + dc$.

Fig. 8.3.4 Contact conditions at engagement and disengagement.

Contact ratio expresses the average number of pairs of teeth theoretically in contact and is obtained numerically by dividing the length of the line of action by the normal pitch. For full-depth teeth, without undercutting, the contact ratio is $m_p = (\sqrt{D_0^2 - D_b^2} + \sqrt{d_0^2 - d_b^2} - 2C \sin \phi)$ / ($2p \cos \phi$). The result will be a mixed number with the integer portion the number of pairs of teeth always in contact and carrying load, and the decimal portion the amount of time an additional pair of teeth are engaged and share load. As an example, for m_p between 1 and 2:

Load is carried by one pair, $(2 - m_p)/m_p$ of the time.

Load is carried by two pairs, $2(m_p - 1)/m_p$ of the time.

In Figs. 8.3.5 to 8.3.7, contact ratios are given for standard generated gears, the lower part of Figs. 8.3.5 and 8.3.6 representing the effect of undercutting.

These charts are applicable to both standard dimetral pitch gears made in accordance with American standards and also standard metric gears that have an addendum of one module.

Tooth Thickness For standard gears, the tooth thickness *t* of mating gears is equal, where $t = p/2 = \pi/(2P_d)$ measured linearly along the arc of the pitch circle. The tooth thickness t_1 at any radial point of the tooth (at diameter D_1) can be calculated from the known thickness *t* at the pitch radius *D*/2 by the relationship $t_1 = t(D_1/D) - D_1$ (inv ϕ_1 – inv ϕ), where inv $\phi = \tan \phi - \phi =$ involute function. Units for ϕ must be radians. Tables of values for inv ϕ from 0 to 45° can be found in the references (Buckingham and Dudley).

Over-plus measurements (spur gears) are another means of deriving tooth thickness. If cylindrical pins are inserted in tooth spaces diametrically opposite one another (or nearest space for an odd number of teeth) [\(Fig. 8.3.8\)](#page-92-0), the tooth thickness can be derived from the measurement *M* as follows:

$$
t = D(\pi/N + \text{inv }\phi_1 - \text{inv }\phi - d_w/D_b)
$$

\n
$$
\cos \phi_1 = (D \cos \phi)/2R_c
$$

\n
$$
R_c = (M - d_w)/2
$$
 for even number of teeth
\n
$$
R_c = (M - d_w)/[2 \cos (90/N)]
$$
 for odd number of teeth

where d_w = pin diameter, R_c = distance from gear center to center of pin, and $M =$ measurement over pins.

For the reverse situation, the over-pins measurement *M* can be found for a given tooth thickness t at diameter D and pressure angle ϕ by the following: inv $\phi_1 = t/D + \text{inv } \phi + d_w/(D \cos \phi) - \pi/N$, $M = D$ cos $\phi/\cos \phi_1 + d_w$ (for even number of teeth), $M =$ (*D* cos ϕ /cos ϕ_1) cos (90°/*N*) + d_w (for odd number of teeth).

Table values of over-pins measures (see Dudley and Van Keuren) facilitate measurements for all standard gears including those with slight departures from standard. (For correlation with tooth thickness and testing radius, see Michalec, *Product Eng.,* May 1957, and ''Precision Gearing: Theory and Practice,'' Wiley.)

Testing radius R_T is another means of determining tooth thickness and refers to the effective pitch radius of the gear when rolled intimately with a master gear of known size calibration. (See Michalec, *Product Eng.,* Nov. 1956, and ''Precision Gearing: Theory and Practice,'' op. cit.) For standard design gears the testing radius equals the pitch radius. The testing radius may be corrected for small departures Δt from ideal tooth thickness by the relationship, $R_T = R + \Delta t/2$ tan ϕ , where $\Delta t =$ $t_1 - t$ and is positive and negative respectively for thicker and thinner tooth thicknesses than standard value *t*.

Backlash *B* is the amount by which the width of a tooth space exceeds the thickness of the engaging tooth measured on the pitch circle. Backlash does not adversely affect proper gear function except for lost mo-

Fig. 8.3.5 Contact ratio, spur gear pairs—full depth, standard generated teeth, $14\frac{1}{2}$ ° pressure angle.

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Fig. 8.3.6 Contact ratio, spur gear pairs—full-depth standard generated teeth, 20° pressure angle.

Fig. 8.3.7 Contact ratio for large numbers of teeth—spur gear pairs, full-depth standard teeth, 20° pressure angle. *(Data by R. Feeney and T. Wall.)*

Fig. 8.3.8 Geometry of over-pins measurements (*a*) for an even number of teeth and (*b*) for an odd number of teeth.

tion upon reversal of gear rotation. Backlash inevitably occurs because of necessary fabrication tolerances on tooth thickness and center distance plus need for clearance to accommodate lubricant and thermal expansion. Proper backlash can be introduced by a specified amount of tooth thinning or slight increase in center distance. The relationship between small change in center distance ΔC and backlash is $B = 2 \overline{\Delta C}$ tan ϕ (see Michalec, "Precision Gearing: Theory and Practice").

Total composite error (tolerance) is a measure of gear quality in terms of the net sum of irregularity of its testing radius R_T due to pitch-circle runout and tooth-to-tooth variations (see Michalec, op. cit.).

Tooth-to-tooth composite error (tolerance) is the variation of testing radius R_T between adjacent teeth caused by tooth spacing, thickness, and profile deviations (see Michalec, op. cit.).

Profile shifted gears have tooth thicknesses that are significantly different from nominal standard value; excluded are deviations caused by normal allowances and tolerances. They are also known as **modified gears, long and short addendum gears,** and **enlarged gears.** They are produced by cutting the teeth with standard cutters at enlarged or reduced outside diameters. The result is a relative shift of the two families of involutes forming the tooth profiles, simultaneously with a shift of the tooth radially outward or inward (s[ee Fig. 8.3.9](#page-93-0)). Calculation of operating conditions and tooth parameters are

$$
C_1 = \frac{(C \cos \phi)}{\cos \phi_1}
$$

inv $\phi_1 = inv \phi + \frac{N_P(t'_G + t'_P) - \pi D_P}{D_P(N_P + N_G)}$
 $t'_G = t + 2X_G \tan \phi$
 $t'_P = t + 2X_P \tan \phi$
 $D'_G = (N_G/P_d) + 2X_G$
 $D'_P = (N_P/P_d) + 2X_P$
 $D'_P = D'_G + (2/P_d)$
 $d'_P = D'_P + (2/P_d)$

where ϕ = standard pressure angle, ϕ_1 = operating pressure angle, *C* = standard center distance = $(N_G + N_P)/2P_d$, *C*₁ = operating center distance, X_G = profile shift correction of gear, and X_P = profile shift correction of pinion. The quantity *X* is positive for enlarged gears and negative for thinned gears.

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* All linear dimensions in millimeters.

Fig. 8.3.9 Geometry of profile-shifted teeth. (*a*) Enlarged case; (*b*) thinned tooth thickness case.

Metric Module Gear Design Equations Basic design equations for spur gearing utilizing the metric module are listed in Table 8.3.5. (See Designatronics, ''Elements of Metric Gear Technology.'')

HELICAL GEARS

Helical gears divide into two general applications: for driving parallel shafts and for driving skew shafts (mostly at right angles), the latter often referred to as *crossed-axis* helical gears. The helical tooth form may be imagined as consisting of an infinite number of staggered laminar spur gears, resulting in the curved cylindrical helix.

Pitch of helical gears is definable in two planes. The diametral and circular pitches measured in the plane of rotation (transverse) are defined as for spur gears. However, pitches measured normal to the tooth are related by the cosine of the helix angle; thus normal diametral pitch = $P_{dn} = P_d/\cos \psi$, normal circular pitch = $p_n = p \cos \psi$, and $P_{dn} p_n = \pi$. Axial pitch is the distance between corresponding sides of adjacent teeth measured parallel to the gear axis and is calculated as $p_a = p \cot \psi$.

Pressure angle of helical gears is definable in the normal and trans-

verse planes by tan $\phi_n = \tan \phi \cos \psi$. The transverse pressure angle, which is effectively the real pressure angle, is always greater than the normal pressure angle.

Tooth thickness *t* of helical gears can be measured in the plane of rotation, as with spur gears, or normal to the tooth surface t_n . The relationship of the two thicknesses is $t_n = t \cos \psi$.

Over-Pins Measurement of Helical Gears Tooth thicknesses *t* at diameter *d* can be found from a known over-pins measurement *M* at known pressure angle ϕ , corresponding to diameter *D* as follows:

Parallel-shaft helical gears must conform to the same conditions and requirements as spur gears with parameters (pressure angle and pitch) consistently defined in the transverse plane. Since standard spur gear cutting tools are usually used, normal plane values are standard, resulting in nonstandard transverse pitches and nonstandard pitch diameters and center distances. For parallel shafts, helical gears must have identical helix angles, but must be of opposite hand (left and right helix directions). The commonly used helix angles range from 15 to 35°. To make most advantage of the helical form, the advance of a tooth should be greater than the circular pitch; recommended ratio is 1.5 to 2 with 1.1 minimum. This overlap provides two or more teeth in continual contact with resulting greater smoothness and quietness than spur gears. Because of the helix, the normal component of the tangential pressure on the teeth produces end thrust of the shafts. To remove this objection, gears are made with helixes of opposite hand on each half of the face and are then known as herringbone gears (see [Fig. 8.3.10\)](#page-94-0).

Crossed-axis helical gears, also called *spiral* or *screw gears* [\(Fig.](#page-94-0) [8.3.11\)](#page-94-0), are a simple type of involute gear used for connecting nonpar-

NONSPUR GEAR TYPES 8-95

allel, nonintersecting shafts. Contact is point and there is considerably more sliding than with parallel-axis helicals, which limits the load capacity. The individual gear of this mesh is identical in form and specification to a parallel-shaft helical gear. Crossed-axis helicals can connect

Fig. 8.3.10 Herringbone gears.

any shaft angle Σ , although 90° is prevalent. Usually, the helix angles will be of the same hand, although for some extreme cases it is possible to have opposite hands, particularly if the shaft angle is small.

Fig. 8.3.11 Crossed-axis helical gears.

Helical Gear Calculations For parallel shafts the center distance is a function of the helix angle as well as the number of teeth, that is, $C =$ $(N_G + N_P)/(2P_{dn} \cos \psi)$. This offers a powerful method of gearing shafts at any specified center distance to a specified velocity ratio. For crossed-axis helicals the problem of connecting a pair of shafts for any velocity ratio admits of a number of solutions, since both the pitch radii and the helix angles contribute to establishing the velocity ratio. The formulas given in Tables 8.3.6 and 8.3.7 are of assistance in calculations. The notation used in these tables is as follows:

 $N_P(N_G)$ = number of teeth in pinion (gear)

- $D_P(D_G)$ = pitch diam of pinion (gear)
- $p_P(p_G)$ = circular pitch of pinion (gear)
	- $p =$ circular pitch in plane of rotation for both gears
	- P_d = diametral pitch in plane of rotation for both gears
	- p_n = normal circular pitch for both gears
	- P_{dn} = normal diametral pitch for both gears
	- ψ_G = tooth helix angle of gear
	- ψ_p = tooth helix angle of pinion
- $l_P(l_G)$ = lead of pinion (gear)
- $=$ lead of tooth helix
- $n_P(n_G) = r/\text{min of }$ pinion (gear)
- Σ = angle between shafts in plan
	- $C =$ center distance

Table 8.3.7 Crossed Helical Gears on Skew Shafts

NONSPUR GEAR TYPES*

Bevel gears are used to connect two intersecting shafts in any given speed ratio. The tooth shapes may be designed in any of the shapes shown in Fig. 8.3.12. A special type of gear known as a **hypoid** was developed by Gleason Works for the automotive industry (see *Jour. SAE,* **18,** no. 6). Although similar in appearance to a spiral bevel, it is not a true bevel gear. The basic pitch rolling surfaces are hyperbolas of revolution. Because a ''spherical involute'' tooth form has a curved crown tooth (the basic tool for generating all bevel gears), Gleason used a straight-sided crown tooth which resulted in bevel gears differing slightly from involute form. Because of the figure 8 shape of the complete theoretical tooth contact path, the tooth form has been called ''octoid.'' Straight-sided bevel gears made by reciprocating cutters are of this type. Later, when curved teeth became widely used (spiral and Zerol), practical limitations of such cutters resulted in introduction of the ''spherical'' tooth form which is now the basis of all curved tooth bevel gears. (For details see Gleason's publication, ''Guide to Bevel Gears.'') Gleason Works also developed the generated tooth form

* In the following text relating to bevel gearing, all tables and figures have been extracted from Gleason Works publications, with permission.

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Revecycle and the nongenerated tooth forms Formate and Helixform, used principally for mass production of hypoid gears for the automotive industry.

Referring to Fig. 8.3.13, we see that the pitch surfaces of bevel gears are frustums of cones whose vertices are at the intersection of the axes; the essential elements and definitions follow.

Addendum angle α : The angle between elements of the face cone and pitch cone.

Back angle: The angle between an element of the back cone and a plane of rotation. It is equal to the pitch angle.

Back cone: The angle of a cone whose elements are tangent to a sphere containing a trace of the pitch circle.

Back-cone distance: The distance along an element of the back cone from the apex to the pitch circle.

Cone distance *Ao* : The distance from the end of the tooth (heel) to the pitch apex.

Crown: The sharp corner forming the outside diameter.

Crown-to-back: The distance from the outside diameter edge (crown) to the rear of the gear.

Dedendum angle δ **: The angle between elements of the root cone and** pitch cone.

Face angle γ _o: The angle between an element of the face cone and its axis.

Face width *F*: The length of teeth along the cone distance.

Front angle: The angle between an element of the front cone and a plane of rotation.

Generating mounting surface, GMS: The diameter and/or plane of rotation surface or shaft center which is used for locating the gear blank during fabrication of the gear teeth.

Heel: The portion of a bevel gear tooth near the outer end.

Mounting distance, MD: For assembled bevel gears, the distance from the crossing point of the axes to the registering surface, measured along the gear axis. Ideally, it should be identical to the pitch apex to back.

Mounting surface, MS: The diameter and/or plane of rotation surface which is used for locating the gear in the application assembly.

Octoid: The mathematical form of the bevel tooth profile. Closely resembles a spherical involute but is fundamentally different.

Pitch angle Γ : The angle formed between an element of the pitch cone and the bevel gear axis. It is the half angle of the pitch.

Pitch apex to back: The distance along the axis from apex of pitch cone to a locating registering surface on back.

Registering surface, RS: The surface in the plane of rotation which locates the gear blank axially in the generating machine and the gear in application. These are usually identical surfaces, but not necessarily so.

Root angle γ_R : The angle formed between a tooth root element and the axis of the bevel gear.

Shaft angle Σ : The angle between mating bevel-gear axes; also, the sum of the two pitch angles.

Spiral angle ψ **: The angle between the tooth trace and an element of** the pitch cone, corresponding to helix angle in helical gears. The spiral angle is understood to be at the mean cone distance.

Toe: The portion of a bevel tooth near the inner end.

Bevel gears are described by the parameter dimensions at the large end (heel) of the teeth. Pitch, pitch diameter, and tooth dimensions, such as addendum are measurements at this point. At the large end of the gear, the tooth profiles will approximate those generated on a spur gear pitch circle of radius equal to the back cone distance. The formative number of teeth is equal to that contained by a complete spur gear. For pinion and gear, respectively, this is $T_P = N_P/\cos \gamma$; $T_G = N_G/\cos \Gamma$, where T_P and T_G = formative number teeth and N_P and N_G = actual number teeth.

Although bevel gears can connect intersecting shafts at any angle, most applications are for right angles. When such bevels are in a 1 : 1 ratio, they are called **mitre gears.** Bevels connecting shafts other than 90° are called **angular bevel gears.** The speeds of the shafts of bevel gears are determined by $n_P/n_G = \sin \Gamma / \sin \gamma$, where $n_P(n_G) = r / \min$ of pinion (gear), and $\gamma(\Gamma)$ = pitch angle of pinion (gear).

All standard bevel gear designs in the United States are in accordance with the **Gleason bevel gear system.** This employs a basic pressure angle of 20° with long and short addendums for ratios other than 1 : 1 to avoid undercut pinions and to increase strength.

20° Straight Bevel Gears for 90° Shaft Angle Since straight bevel gears are the easiest to produce and offer maximum precision, they are frequently a first choice. Modern straight-bevel-gears generators produce a tooth with localized tooth bearing designated by the Gleason registered tradename Coniflex. These gears, produced with a circular cutter, have a slightly crowned tooth form (see [Fig. 8.3.12](#page-94-0)*b*). Because of the superiority of Coniflex bevel gears over the earlier reciprocating cutter produced straight bevels and because of their faster production, they are the standards for all bevel gears. The design parameters of Fig. 8.3.13 are calculated by the formulas o[f Table 8.3.8.](#page-96-0) Backlash data are given in [Table 8.3.9.](#page-96-0)

Fig. 8.3.13 Geometry of bevel gear nomenclature. (*a*) Section through axes; (*b*) view along axis *Z/Z*.

Table 8.3.8 Straight Bevel Gear Dimensions* (All linear dimensions in inches)

* Abstracted from "Gleason Straight Bevel Gear Design," Tables 8.3.8 and 8.3.9 an[d Fig. 8.3.4.](#page-90-0) Gleason Works, Inc.
† Numbers of teeth; ratios with 16 or more teeth in pinion: 15/17 and higher; 14/20 and higher; 13/31 and h without undercut.

[‡] The actual dedendum will be 0.002 in greater than calculated.

Table 8.3.9 Recommended Normal Backlash for Bevel Gear Meshes*

| P_d | Backlash range | P_d | Backlash range |
|---------------|-----------------|---------------|-----------------|
| $1.00 - 1.25$ | $0.020 - 0.030$ | $3.50 - 4.00$ | $0.007 - 0.009$ |
| $1.25 - 1.50$ | $0.018 - 0.026$ | $4 - 5$ | $0.006 - 0.008$ |
| $1.50 - 1.75$ | $0.016 - 0.022$ | $5 - 6$ | $0.005 - 0.007$ |
| $1.75 - 2.00$ | $0.014 - 0.018$ | $6 - 8$ | $0.004 - 0.006$ |
| $2.00 - 2.50$ | $0.012 - 0.016$ | $8 - 10$ | $0.003 - 0.005$ |
| $2.50 - 3.00$ | $0.010 - 0.013$ | $10 - 12$ | $0.002 - 0.004$ |
| $3.00 - 3.50$ | $0.008 - 0.011$ | Finer than 12 | $0.001 - 0.003$ |
| | | | |

* The table gives the recommended normal backlash for gears assembled ready to run. Because of manufacturing tolerances and changes resulting from heat treatment, it is frequently necessary to reduce the theoretical tooth

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Angular straight bevel gears connect shaft angles other than 90° (larger or smaller), and the formulas of [Table 8.3.8 a](#page-96-0)re not entirely applicable, as shown in the following:

Item 8, shaft angle, is the specified non-90° shaft angle.

Item 10, pitch angles. Shaft angle Σ less than 90°, tan γ = $\sin \Sigma/(N/n + \cos \Sigma)$; shaft angle Σ greater than 90°, tan γ = $\sin (180 - \Sigma)/[N/n - \cos (180^\circ - \Sigma)].$

For all shaft angles, sin γ /sin $\Gamma = n/N$; $\Gamma = \Sigma - \gamma$.

Item 13, addendum, requires calculation of the equivalent 90° bevel gear ratio m_{90} , $m_{90} = [N \cos \gamma/(n \cos \Gamma)]^{1/2}$. The value m_{90} is used as the ratio N/n when applying the formula for addendum. The quantity under the radical is always the absolute value and is therefore always positive.

Item 20, pitch apex to crown, $x_o = A_0 \cos \gamma - a_{op} \sin \gamma$, $X_o =$ A_0 cos $\Gamma - a_{oG}$ sin Γ .

Item 21, circular thickness, except for high ratios, *K* may be zero.

Spiral Bevel Gears for 90° Shaft Angle The spiral curved teeth produce additional overlapping tooth action which results in smoother gear action, lower noise, and higher load capacity. The spiral angle has been standardized by Gleason at 35°. Design parameters are calculated by formulas of Table 8.3.10.

Angular Spiral Bevel Gears Several items deviate from the formulas of Table 8.3.10 in the same manner as angular straight bevel gears. Therefore, the same formulas apply for the deviating items with only the following exception:

Item 21, circular thickness, the value of *K* in [Fig. 8.3.15](#page-98-0) must be determined from the equivalent 90° bevel ratio (m_{90}) and the equivalent 90° bevel pinion. The latter is computed as $n_{90} = n \sin \Gamma_{90}/\cos \gamma$, where $\tan\Gamma_{\infty} = m_{\infty}$.

Fig. 8.3.14 Circular thickness factor for straight bevel gears.

SOURCE: Gleason, ''Spiral Bevel Gear System.''

WORMGEARS AND WORMS 8-99

The zerol bevel gear is a special case of a spiral bevel gear and is limited to special applications. Design and fabrication details can be obtained from Gleason Works.

Hypoid gears are special and are essentially limited to automotive applications.

Fig. 8.3.15 Circular thickness factors for spiral bevel gears with 20° pressure angle and 35° spiral angle. Left-hand pinion driving clockwise or right-hand pinion driving counterclockwise.

WORMGEARS AND WORMS

Worm gearing is used for obtaining large speed reductions between nonintersecting shafts making an angle of 90° with each other. If a wormgear such as shown in Fig. 8.3.16 engages a straight worm, as shown in Fig. 8.3.17, the combination is known as **single enveloping worm gearing.** If a wormgear of the kind shown in Fig. 8.3.16 engages a worm as shown in Fig. 8.3.18, the combination is known as **double enveloping worm gearing.**

Fig. 8.3.16 Single enveloping worm gearing.

Fig. 8.3.17 Straight worm.

With worm gearing, the **velocity ratio** is the ratio between the number of teeth on the wormgear and the number of threads on the worm. Thus, a 30-tooth wormgear meshing with a single threaded worm will have a velocity ratio of 1 : 30; that is, the worm must make 30 rv in order to revolve the wormgear once. For a double threaded worm, there will be 15 rv of the worm to one of the wormgear, etc. High-velocity ratios are thus obtained with relatively small wormgears.

Fig. 8.3.18 Double enveloping worm gearing.

Tooth proportions of the worm in the central section (Fig. 8.3.17) follow standard rack designs, such as $14\frac{1}{2}$, 20, and 25° . The mating wormgear is cut conjugate for a unique worm size and center distance. The geometry and related design equations for a straight-sided cylindrical worm are best seen from a development of the pitch plane [\(Fig.](#page-99-0) [8.3.19\)](#page-99-0).

$$
D_w = \text{pitch diameter of worm} = \frac{n_w p_n}{\pi \sin \lambda}
$$

\n
$$
p_n = p \cos \lambda = \frac{\pi D_w}{n_w} \sin \lambda
$$

\n
$$
L = \text{lead of worm} = n_w p
$$

\n
$$
D_g = \text{pitch diameter of worm gear}
$$

\n
$$
= \frac{N_g}{P_d} = \frac{p N_g}{\pi} = \frac{P_n N_g}{\pi \cos \lambda}
$$

\n
$$
C = \text{center distance}
$$

\n
$$
= \frac{D_w + D_g}{2} = \frac{p_n}{2\pi} \left(\frac{N_g}{\cos \lambda} + \frac{n_w}{\sin \lambda} \right)
$$

where n_w = number of threads in worm; N_g = number of teeth in wormgear; $Z =$ velocity ratio $=N_e/n_w$.

The pitch diameter of the wormgear is established by the number of teeth, which in turn comes from the desired gear ratio. The pitch diameter of the worm is somewhat arbitrary. The lead must match the wormgear's circular pitch, which can be satisfied by an infinite number of worm diameters; but for a fixed lead value, each worm diameter has a unique lead angle. AGMA offers a design formula that provides near optimized geometry:

$$
D_w = \frac{C^{0.875}}{2.2}
$$

where $C =$ center distance. Wormgear face width is also somewhat arbitrary. Generally it will be $\frac{3}{5}$ to $\frac{2}{3}$ of the worm's outside diameter.

Worm mesh nonreversibility, a unique feature of some designs, occurs because of the large amount of sliding in this type of gearing. For a given coefficient of friction there is a critical value of lead angle below

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which the mesh is nonreversible. This is generally 10° and lower but is related to the materials and lubricant. Most single thread worm meshes are in this category. This locking feature can be a disadvantage or in some designs can be put to advantage.

Double enveloping worm gearing is special in both design and fabrication. Application is primarily where a high load capacity in small space is desired. Currently, there is only one source of manufacture in the United States: Cone Drive Division of Ex-Cello Corp. For design details and load ratings consult publications of Cone Drive and AGMA Standards.

Fig. 8.3.19 Cylindrical worm geometry and design parameters.

Other Gear Types

Gears for special purposes include the following (details are to be found in the references):

Spiroid (Illinois Tool Works) gears, used to connect skew shafts, resemble a hypoid-type bevel gear but in performance are more like worm meshes. They offer very high ratios and a large contact ratio resulting in high strength. The **Helicon** (Illinois Tool Works) gear is a variation in which the pinion is not tapered, and ratios under 10 : 1 are feasible.

Beveloid (Vinco Corp.) gears are tapered involute gears which can couple intersecting shafts, skew shafts, and parallel shafts.

Face gears have teeth cut on the rotating face plane of the gear and mate with standard involute spur gears. They can connect intersecting or nonparallel, nonintersecting shafts.

Noncircular gears or **function gears** are used for special motions or as elements of analog computers. They can be made with elliptical, logarithmic, spiral, and other functions. See Cunningham references; also, Cunningham Industries, Inc., Stamford, CT.

DESIGN STANDARDS

In addition to the ANSI and AGMA standards on basic tooth proportions, the AGMA sponsors a large number of national standards dealing with gear design, specification, and inspection. (Consult AGMA, 1500 King St., Arlington, VA 22314, for details.) Helpful general references are AGMA, ''Gear Handbook,'' 390.03 and ANSI/AGMA, ''Gear Classification and Inspection Handbook,'' 2000-A88, which establish a system of quality classes for all gear sizes and pitches, ranging from crude coarse commercial gears to the highest orders of fine and coarse ultra-precision gears.

There are 13 quality classes, numbered from 3 through 15 in ascending quality. Tolerances are given for key functional parameters: runout, pitch, profile, lead, total composite error, tooth-to-tooth composite error, and tooth thickness. Also, tooth thickness tolerances and recommended mesh backlash are included. These are related to diametral pitch and pitch diameter in recognition of fabrication achievability. Data are available for spur, helical, herringbone, bevel, and worm gearing; and spur and helical racks. Special sections cover gear applications and suggested quality number; gear materials and treatments; and standard procedure for identifying quality, material, and other pertinent parameters. These data are too extensive for inclusion in this handbook, and the reader is referred to the cited AGMA references.

STRENGTH AND DURABILITY

Gear teeth fail in two classical manners: tooth breakage and surface fatigue pitting. Instrument gears and other small, lightly loaded gears are designed primarily for tooth-bending beam strength since minimizing size is the priority. Power gears, usually larger, are designed for both strengths, with surface durability often more critical. Expressions for calculating the beam and surface stresses started with the Lewis-Buckingham formulas and now extend to the latest AGMA formulas.

The Lewis formula for analysis of beam strength, now relegated to historical reference, serves to illustrate the fundamentals that current formulas utilize. In the Lewis formula, a tooth layout shows the load assumed to be at the tip (Fig. 8.3.20). From this Lewis demonstrated that the beam strength $W_b = FSY/P_d$, where $F =$ face width; $S =$ allowable stress; $Y =$ Lewis form factor; P_d = diametral pitch. The form factor *Y* is derived from the layout as $Y = 2P_d/3$. The value of *Y* varies with tooth design (form and pressure angle) and number of teeth. In the case of a helical gear tooth, there is a thrust force W_{th} in the axial direction that arises and must be considered as a component of bearing load. Se[e Fig. 8.3.21](#page-100-0)*b*. Buckingham modified the Lewis formula to include dynamic effects on beam strength and developed equations for evaluating surface stresses. Further modifications were made by other investigators, and have resulted in the most recent AGMA rating formulas which are the basis of most gear designs in the United States.

Fig. 8.3.20 Layout for beam strength (Lewis formula).

AGMA Strength and Durability Rating Formulas

For many decades the AGMA Gear Rating Committee has developed and provided tooth beam strength and surface durability (pitting resistance) formulas suitable for modern gear design. Over the years, the formulas have gone through a continual evolution of revision and improvement. The intent is to provide a common basis for rating various gear types for differing applications and thus have a uniformity of practice within the gear industry. This has been accomplished via a series of standards, many of which have been adopted by ANSI.

The latest standards for rating bending beam strength and pitting resistance are ANSI/AGMA 2001-C95, ''Fundamental Rating Factors and Calculation Methods for Involute, Spur, and Helical Gear Teeth'' (available in English and metric units) and AGMA 908-B89, ''Geometry Factors for Determining the Pitting Resistance and Bending Strength of Spur, Helical, and Herringbone Gear Teeth.'' These standards have replaced AGMA 218.01 with improved formulas and details.

The rating formulas in [Tables 8.3.11](#page-100-0) and 8.3.12 are abstracted from ANSI/AGMA 2001-B88, ''Fundamental Rating Factors and Calculation Methods for Involute Spur and Helical Gear Teeth,'' with permission.

Overload factor K_a is intended to account for an occasional load in excess of the nominal design load W_t . It can be established from experience with the particular application. Otherwise use $K_o = 1$.

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Table 8.3.11 AGMA Pitting Resistance Formula for Spur and Helical Gears

(See Note 1 below.)

$$
s_c = C_p \sqrt{W_t K_o K_v K_s \frac{K_m}{dF} \frac{C_f}{I}}
$$

where s_c = contact stress number, $1b/in^2$

- C_p = elastic coefficient,* (lb/in²)^{0.5} (see text an[d Table 8.3.13\)](#page-101-0)
- W_t = transmitted tangential load, lb
- K_o = overload factor (see text)
- K_v = dynamic factor (see Fig. 8.3.22)
- K_s = size factor (see text)
- K_m = load distribution factor (see text an[d Table 8.3.14\)](#page-101-0)
- C_f = surface condition factor for pitting resistance (see text)
- \hat{F} = net face width of narrowest member, in
- $I =$ geometry factor for pitting resistance (see text an[d Figs. 8.3.23](#page-102-0) and 8.3.24)
- $d =$ operating pitch diameter of pinion, in

$$
= \frac{2C}{m_G + 1}
$$
 for external years

 $m_G - 1$ for internal gears

where $C =$ operating center distance, in

 m_G = gear ratio (never less than 1.0)

Allowable contact stress number *sac*

$$
s_c \le \frac{s_{ac} Z_N C_H}{S_H K_T K_R}
$$

- where s_{ac} = allowable contact stress number, lb/in² (se[e Tables 8.3.15](#page-106-0) and 8.3.16[; Fig. 8.3.34\)](#page-106-0)
	- Z_N = stress cycle factor for pitting resistance (se[e Fig. 8.3.35\)](#page-109-0)
	- C_H = hardness ratio factor for pitting resistance (see text an[d Figs. 8.3.36](#page-109-0))
	- and 8.3.37)
	- S_H = safety factor for pitting (see text)
	- K_T = temperature factor (see text)
	- K_R = reliability factor (se[e Table 8.3.19\)](#page-107-0)
- * **Elastic coefficient** C_p can be calculated from the following equation when the paired materials in the pinion-gear set are not listed in [Table 8.3.13:](#page-101-0)

$$
C_p = \sqrt{\frac{1}{\pi [(1 - \mu_P^2)/E_P + (1 - \mu_G^2)/E_G]}}
$$

where $\mu_p(\mu_G)$ = Poisson's ratio for pinion (gear)

 $E_P(E_G)$ = modulus of elasticity for pinion (gear), lb/in²

Note 1: If the rating is calculated on the basis of uniform load, the transmitted tangential load is

$$
W_t = \frac{33,000P}{v_t} = \frac{2T}{d} = \frac{126,000P}{n_p d}
$$

where $P =$ transmitted power, hp

 $T =$ transmitted pinion torque, lb \cdot in *v*_{*t*} = pitch line velocity at operating pitch diameter, ft/min = $\frac{\pi n_p d}{12}$

12

Table 8.3.12 AGMA Bending Strength Fundamental Formula for Spur and Helical Gears (See Note 1 in Table 8.3.11.)

$$
s_t = W_t K_o K_v K_s \frac{P_d}{F} \frac{K_m K_B}{J}
$$

where s_t = bending stress number, lb/in²

- K_B = rim thickness factor (se[e Fig. 8.3.38\)](#page-110-0) $J =$ geometry factor for bending strength (see text an[d Figs. 8.3.25](#page-103-0) to 8.3.31)
- P_d = transverse diametral pitch, in^{-1*}; P_{dn} for helical gears

$$
f_{\rm{max}}
$$

 $P_d = \frac{\pi}{p_x \tan \psi_s} = P_{dn} \cos \psi_s$ for helical gears

where P_{dn} = normal diametral pitch, in⁻¹

- p_x = axial pitch, in ψ_s = helix angle at standard pitch diameter
	- $\psi_s = \arcsin \frac{\pi}{p_x P_{dn}}$

Allowable bending stress numbers *s at*

$$
s_t \le \frac{s_{at}Y_N}{S_F K_T K_R}
$$

where s_{at} = allowable bending stress number, lb/in² (se[e Tables 8.3.17](#page-107-0) and 8.3.18 an[d Figs. 8.3.39](#page-107-0) to 8.3.41)

 Y_N = stress cycle factor for bending strength (se[e Fig. 8.3.42\)](#page-112-0)

 S_F = safety factor for bending strength (see text)

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Poisson's ratio $= 0.30$.

SOURCE: ANSI/AGMA 2001-B88; with permission.

Size factor K_s is intended to factor in material nonuniformity due to tooth size, diameter, face width, etc. AGMA has not established factors for general gearing; use $K_s = 1$ unless there is information to warrant using a larger value.

Load distribution factor K_m **reflects the nonuniform loading along the** lines of contact due to gear errors, installation errors, and deflections. Analytical and empirical methods for evaluating this factor are presented in ANSI/AGMA 2001-C95 but are too extensive to include here. Alternately, if appropriate for the application, K_m can be extrapolated from values given in Table 8.3.14.

Surface condition factor C_f is affected by the manufacturing method (cutting, shaving, grinding, shotpeening, etc.). Standard factors have not been established by AGMA. Use $C_f = 1$ unless experience can establish confidence for a larger value.

Geometry factors *I* **and** *J* relate to the shape of the tooth at the point of contact, the most heavily loaded point. AGMA 908-B89 (Information Sheet, Geometry Factors for Determining the Pitting Resistance and Bending Strength for Spur, Helical and Herringbone Gear Teeth) presents detailed procedures for calculating these factors. The standard also includes a collection of tabular values for a wide range of gear tooth designs, but they are too voluminous to be reproduced here in their entirety. Earlier compact graphs of *I* and *J* values in AGMA 218.01 are still valid. They are presented here along with several curves from AGMA 610-E88, which are based upon 218.01. Se[e Figs. 8.3.23](#page-102-0) to 8.3.31.

Allowable contact stress s_{ac} and allowable bending stress s_{at} are obtainable fro[m Tables 8.3.15](#page-106-0) to 8.3.18. Contact stress hardness specification applies to the start of active profile at the center of the face width, and for bending stress at the root diameter in the center of the tooth space and face width. The lower stress values are for general design purposes; upper values are for high-quality materials and high-quality control. (See ANSI/AGMA 2001-C95, tables 7 through 10, regarding detailed metallurgical specifications; stress grades 1, 2, and 3; and type A and B hardness patterns.)

For **reversing loads**, allowable bending stress values, s_{at} are to be reduced to 70 percent. If the rim thickness cannot adequately support the load, an additional derating factor K_B is to be applied. Se[e Fig. 8.3.38.](#page-110-0)

Hardness ratio factor C_H applies when the pinion is substantially harder than the gear, and it results in work hardening of the gear and increasing its capacity. Factor C_H applies to only the gear, not the pinion. Se[e Figs. 8.3.36](#page-109-0) and 8.3.37.

Safety factors S_H and S_F are defined by AGMA as factors beyond K_O and K_R ; they are used in connection with extraordinary risks, human or economic. The values of these factors are left to the designer's judgment as she or he assesses all design inputs and the consequences of possible failure.

Temperature factor $K_T = 1$ when gears operate with oil temperature not exceeding 250°F.

Reliability factor K_R accounts for statistical distribution of material failures. Typically, material strength ratings (Tables 8.3.13, and 8.3.15 to 8.3.18; [Fig. 8.3.34](#page-106-0) and 8.3.42) are based on probability of one failure in 100 at 107 cycle[s. Table 8.3.19](#page-107-0) lists reliability factors that may be used to modify the allowable stresses and the probability of failure.

Strength and Durability of Bevel, Worm, and Other Gear Types

For bevel gears, consult the referenced Gleason publications; for worm gearing refer to AGMA standards; for other special types, refer to Dudley, ''Gear Handbook.''

Table 8.3.14 Load-Distribution Factor *Km* **for Spur Gears***

* An approximate guide only. See ANSI/AGMA 2001-C95 for derivation of more exact values.

SOURCE: Darle W. Dudley, ''Gear Handbook,'' McGraw-Hill, New York, 1962.

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Fig. 8.3.23 Geometry factor *I* for 20° full-depth standard spur gears. (*Source: ANSI/AGMA 2018-01, with permission.*)

Fig. 8.3.24 Geometry factor *I* for 25° full-depth standard spur gears. (*Source: ANSI/AGMA 2018-01, with permission.*)

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Fig. 8.3.25 Geometry factor *J* for 20° standard addendum spur gears. (*Source: ANSI/AGMA 2018-01, with permission.*)

Fig. 8.3.26 Geometry factor *J* for 25° standard addendum spur gears. (*Source: ANSI/AGMA 2018-01, with permission.*)

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Fig. 8.3.27 Geometry factor *J* for 20° normal pressure angle helical gears. (Standard addendum, finishing hob.) (*Source: ANSI/AGMA 2018-01, with permission.*)

Fig. 8.3.28 Geometry factor *J* for 20° normal pressure angle helical gears. (Standard addendum, full fillet hob.) (*Source: ANSI/AGMA 2018-01, with permission.*)

Fig. 8.3.29 Geometry factor *J* for 25° normal pressure angle helical gears. (Standard addendum, full fillet hob.) (*Source: ANSI/AGMA 2018-01, with permission.*)

Fig. 8.3.30 Factor *J* multipliers for 20° normal pressure angle helical gears. The modifying factor can be applied to the *J* factor when other than 75 teeth are used in the mating element. (*Source: ANSI/AGMA 2018-01, with permission.*)

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Fig. 8.3.31 Factor *J* multipliers for 25° normal pressure angle helical gears. The modifying factor can be applied to the *J* factor when other than 75 teeth are used in the mating element. (*Source: ANSI/AGMA 6010-E88, with permission.*)

Note 1: Table 9 and Tables 7, 8, and 10 cited in Tables 8.3.16 to 8.3.18 are in ANSI/AGMA 2001-95.
* The allowable-stress numbers indicated may be used with the case depths shown [in Figs. 8.3.32](#page-108-0) and 8.3.33.
SOURCE: Abstrac

* See ANSI/AGMA 2004–B89, ''Gear Materials and Heat Treatment Manual.'' SOURCE: Abstracted from ANSI/AGMA 2001-C95, with permission.

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Note 1: See Table 8 in ANSI/AGMA 2001-C95.

Note 2: See Table 9 in ANSI/AGMA 2001-C95.

* The allowable-stress numbers indicated may be used with the case depths shown [in Figs. 8.3.32](#page-108-0) and 8.3.33. † If bainite and microcracks are limited to grade 3 levels, 70,000 lb/in2 may be used.

‡ The overload capacity of nitrided gears is low. Since the shape of the effective *S–N* curve is flat, the sensitivity to shock should be investigated before one proceeds with the design. § The tabular material is too extensive to record here. Refer to ANSI/AGMA 2001-C95, tables 7 to 10.

SOURCE: Abstracted from ANSI/AGMA 2001-C95, with permission.

Table 8.3.18 Allowable Bending Stress Number *s at* **for Iron and Bronze Gears**

* See ANSI/AGMA 2004-B89, ''Gear Materials and Heat Treatment Manual.''

SOURCE: Abstracted from ANSI/AGMA 2001-C95, with permission.

Table 8.3.19 Reliability Factors K_R

* Tooth breakage is sometimes considered a greater hazard than pitting. In such cases a greater value of K_R is selected for bending.

† At this value, plastic flow might occur rather than pitting. ‡ From test data extrapolation.

SOURCE: Abstracted from ANSI/AGMA 2001-C95, with permission.

GEAR MATERIALS

(Se[e Tables 8.3.15](#page-106-0) to 8.3.18.)

Metals

Plain carbon steels are most widely used as the most economical; similarly, cast iron is used for large units or intricate body shapes. Heattreated carbon and alloy steels are used for the more severe load- and wear-resistant applications. Pinions are usually made harder to equalize wear. Strongest and most wear-resistant gears are a combination of heat-treated high-alloy steel cores with case-hardened teeth. (See Dudley, ''Gear Handbook,'' chap. 10.) Bronze is particularly recommended for wormgears and crossed helical gears. Stainless steels are limited to special corrosion-resistant environment applications. Aluminum alloys are used for light-duty instrument gears and airborne lightweight requirements.

Sintered powdered metals technology offers commercial high-quality gearing of high strength at very economical production costs. Die-cast gears for light-duty special applications are suitable for many products.

Fig. 8.3.32 Minimum effective case depth for carburized gears h_{emin} . Effective case depth is defined as depth of case with minimun hardness of 50 RC. Total case depth to core carbon is approximately 1.5 times the effe (*Source: ANSI/AGMA 2001-C95, with permission.*)

Fig. 8.3.33 Minimum total case depth for nitrided gears h_{cmin} . (*Source: ANSI/AGMA 2001-C95, with permission.*)

Fig. 8.3.34 Allowable contact stress number for through-hardened steel gears *sac* . (*Source: ANSI/AGMA 2001-C95, with permission.*)

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Fig. 8.3.35 Pitting resistance stress cycle factor Z_N . (*Source: ANSI/AGMA 2001-C95, with permission.*)

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Fig. 8.3.37 Hardness ratio factor *CH* (surface-hardened pinions). (*Source: ANSI/AGMA 2001-C95, with permission.*)

For power gear applications, heat treatment is an important part of complete and proper design and specification. Heat treatment descriptions and specification tolerances are given in the reference cited below.

Precision gears of the small device and instrument types often require protective coatings, particularly for aircraft, marine, space, and military applications. There is a wide choice of chemical and electroplate coatings offering a variety of properties and protection.

For pertinent properties and details of the above special materials and protective coatings see Michalec, "Precision Gearing," chap. 9, Wiley.

Plastics

In recent decades, various forms of nonmetallic gears have displaced metal gears in particular applications. Most plastics can be hobbed or shaped by the same methods used for metallic gears. However, highstrength composite plastics suitable for good-quality gear molding have become available, along with the development of economical highspeed injection molding machines and improved methods for producing accurate gear molds.

Fig. 8.3.38 Rim thickness factor *K_B*. (*Source: ANSI/AGMA 2001-C95, with permission.)*

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Fig. 8.3.39 Allowable bending stress numbers for through-hardened steel gears *sat* . (*Source: ANSI/AGMA 2001-C95, with permission.*)

Fig. 8.3.40 Allowable bending stress numbers *sat* for nitrided through-hardened steel gears (i.e., AISI 4140 and 4340). (*Source: ANSI/AGMA 2001-C95, with permission.*)

Fig. 8.3.41 Allowable bending stress numbers for nitrided steel gears *sat* . (*Source: ANSI/AGMA 2001-C95, with permission.*) **8-112**

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Fig. 8.3.42 Bending strength stress cycle factor *Y_N*. (*Source: ANSI/AGMA 2001-C95, with permission.)*

The most significant features and advantages of plastic gear materials are:

Cost-effectiveness of injection molding process

Wide choice of characteristics: mechanical strength, density, friction, corrosion resistance, etc.

One-step production; no preliminary or secondary operations

Uniformity of parts

Ability to integrate special shapes, etc., into gear body

Elimination of machining operations

Capability to mold with metallic insert hubs, if required, for more precise bore diameter or body stability

Capability to mold with internal solid lubricants

Ability to operate without lubrication

Quietness of operation

Consistent with trend toward greater use of plastic housings and components

Plastic gears do have limitations relative to metal gears. The most significant are:

Less load-carrying capacity

Cannot be molded to as high accuracy as machined metal gears Much larger coefficient of expansion compared to metals

Less environmentally stable with regard to temperature and water absorption

Can be negatively affected by some chemicals and lubricants

Initial high cost in mold manufacture to achieve proper tooth geometry accuracies

Narrower range of temperature operation, generally less than 250°F and not lower than 0°F

For further information about plastic gear materials and achievable precision, consult the cited reference: Michalec, ''Precision Gearing: Theory and Practice.''

For a comprehensive presentation of gear molding practices, design, plastic materials, and strength and durability of plastic gears, consult the cited reference: Designatronics, ''Handbook of Gears: Inch and Metric,'' pp. T131–T158.

GEAR LUBRICATION

Proper lubrication is important to prevention of premature wear of tooth surfaces. In the basic action of involute tooth profiles there is a significant sliding component along with rolling action. In worm gearing sliding is the predominant consideration. Thus, a lubricant is essential for all gearing subject to measurable loadings, and even for lightly or negligibly loaded instrument gearing it is needed to reduce friction. Excellent oils and greases are available for high unit load, high speed gearing. See Secs. 6.11 and 8.4; also consult lubricant suppliers for recommendations and latest available high-quality lubricants with special-purpose additives.

General and specific information for lubrication of gearing is found in ANSI/AGMA 9005-D94, ''Industrial Gear Lubrication,'' which covers open and enclosed gearing of all types. AGMA lists a family of lubricants in accordance with viscosities, numbered 1 through 13, with a cross-reference to equivalent ISO grades. See [Table 8.3.20.](#page-113-0) For AGMA's lubrication recommendations for open and closed gearing related to pitch line speed and various types of lubrication systems, refer t[o Tables 8.3.21](#page-113-0) to 8.3.23. For worm gearing and other information, see ANSI/AGMA 9005-D94.

Information in [Table 8.3.24 m](#page-114-0)ay be used as a quick guide to gear lubricants and their sources for general-purpose instrument and medium-size gearing. Lubricant suppliers should be consulted for specific high-demand applications.

Often gear performance can be enhanced by special additives to the oil. For this purpose, colloidal additives of graphite, molybdenum disulfide $(MoS₂)$, and Teflon are very effective. These additives are particularly helpful to reduce friction and prevent wear; they are also very beneficial to reduce the rate of wear once it has begun, and thus they prolong gear life. The colloidal additive combines chemically with the metal surface material, resulting in a tenacious layer of combined material interposed between the base metals of the meshing teeth. The size of the colloidal additives is on the order of $2 \mu m$, sufficiently fine not to interfere with the proper operation of the lubricant system filters. [Table](#page-115-0) [8.3.25 l](#page-115-0)ists some commercial colloidal additives and their sources of supply.

Plastic gears are often operated without any external lubrication, and

Table 8.3.20 Viscosity Ranges for AGMA Lubricants

e Per ISO 3448, "Industrial Liquid Lubricants—ISO Viscosity Classification," also ASTM D2422 and British Standards Institution B.S. 4231.
P Extreme-pressure lubricants should be used only when recommended by the gear manuf

^c Synthetic gear oils 9S to 13S are available but not yet in wide use.

d Oils marked *Comp* are compounded with 3% to 10% fatty or synthetic fatty oils.
* Viscosities of AGMA lubricant no. 13 and above are specified at 100°C (210°F) since measurement of viscosities of these heavy lubricants a

thick film of lubricant on the gear teeth. Viscosities listed are for the base compound without diluent.
CAUTION: These lubricants may require special handling and storage procedures. Diluent can be toxic or irritating to lubricant supplier's instructions.

SOURCE: Abstracted from ANSI/AGMA 9005-D94, with permission.

a AGMA lubricant numbers listed above refer to gear lubricants shown in Table 8.3.20. Physical and performance specifications are shown in Tables 1 and 2 of ANSI/ASMA 9005-D94.
Although both R & O and EP oils are listed, t *b* Does not apply to worm gearing.

Temperature in vicinity of the operating gears.
4 When ambient temperatures approach the lower end of the given range, lubrication systems must be equipped with suitable heating units for proper circulation of lubricant an prevention of channeling. Check with lubricant and pump suppliers.
^e When ambient temperature remains between 30°C (90°F) and 50°C (125°F) at all times, use 10 or 10 EP.
When ambient temperature remains between 30°C (90°

SOURCE: Abstracted from ANSI/AGMA 9005-D94, with permission.

Table 8.3.22 AGMA Lubricant Number Guidelines for Open Gearing Intermittent Applications*a*,*b*,*^c*

Gear pitch line velocity does not exceed 7.5 m/s (1,500 ft/min)

^a AGMA viscosity number guidelines listed above refer to gear oils shown in Table 8.3.20.

^b Does not apply to worm gearing. *^c* Feeder must be capable of handling lubricant selected.

^d Ambient temperature is temperature in vicinity of gears.

^e Special compounds and certain greases are sometimes used in mechanical spray systems to lubricate open gearing.

Consult gear manufacturer and spray system manufacturer before proceeding. *^f* Diluents must be used to facilitate flow through applicators.

^g EP oils are preferred, but may not be available in some grades. SOURCE: Abstracted from ANSI/AGMA 9005-D94, with permission.

Table 8.3.23 AGMA Lubricant Number Guidelines for Enclosed Helical, Herringbone, Straight Bevel, Spiral Bevel, and Spur Gear Drives*^a*

^a AGMA lubricant numbers listed above refer to R&O and synthetic gear oil shown i[n Table 8.3.20.](#page-113-0) Physical and performance specifications are shown in Tables 1 and 3 of ANSI/AGMA 9005-D94. EP or synthetic gear lubricants in the corresponding viscosity

grades may be substituted where deemed acceptable by the gear drive manufacturer.
^{*b*} Special considerations may be necessary at speeds above 40 m/s (8,000 ft/min). Consult gear drive manufacturer for specific recommendations.

^c Pitch line velocity replaces previous standards' center distance as the gear drive parameter for lubricant selection.

^d Variations in operating conditions such as surface roughness, temperature rise, loading, speed, etc., may necessitate use of a lubricant of one grade higher or lower. Contact gear drive manufacturer for specific recomm

^e Drives incorporating wet clutches or overrunning clutches as backstopping devices should be referred to the gear manufacturer, as certain types of lubricants may adversely affect clutch performance.

For ambient temperatures outside the ranges shown, consult the gear manufacturer.
⁸ Pour point of lubricant selected should be at least 5°C (9°F) lower than the expected minimum ambient starting temperature. If the ambient starting temperature approaches lubricant pour point, oil sump heaters may be required to facilitate starting and ensure proper lubrication (see 5.1.6 in ANSI/AGMA 9005-D94).

h At the extreme upper and lower pitch line velocity ranges, special consideration should be given to all drive components, including bearing and seals, to ensure their proper performance. SOURCE: Abstracted from ANSI/AGMA 9005-D94, with permission.

Table 8.3.24 Typical Gear Lubricants

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| | Temperature | | | |
|----------------------------|-----------------------|----------------------|-----------------------|---|
| Lubricant type | range, ^o F | Source | Identification | Remarks |
| Colloidal graphite | Up to $1,000$ | Acheson Colloids Co. | SLA 1275 | Good load capacity, excellent temperature resistance |
| Colloidal MoS ₂ | Up to 750 | Acheson Colloids Co. | SLA 1286 | Good antiwear |
| Colloidal Teflon | Up to 575 | Acheson Colloids Co. | SLA 1612 | Low coefficient of friction |

Table 8.3.25 Solid Oil Additives

they will provide long service life if the plastic chosen is correct for the application. Plastics manufacturers and their publications can be consulted for guidance. Alternatively, many plastic gear materials can be molded with internal solid lubricants, such as $MoS₂$, Teflon, and graphite.

GEAR INSPECTION AND QUALITY CONTROL

Gear performance is not only related to the design, but also depends upon obtaining the specified quality. Details of gear inspection and control of subtle problems relating to quality are given in Michalec, ''Precision Gearing,'' Chap. 11.

COMPUTER MODELING AND CALCULATIONS

A feature of the latest AGMA rating standards is that the graphs, including those presented here, are accompanied by equations which allow application of computer-aided design. Gear design equations and strength and durability rating equations have been computer modeled by many gear manufacturers, users, and university researchers. Numerous software programs, including integrated CAD/CAM, are available from these places, and from computer system suppliers and specialty software houses. It is not necessary for gear designers, purchasers, and fabricators to create their own computer programs.

With regard to gear tooth strength and durability ratings, many custom gear house designers and fabricators offer their own computer modeling which incorporates modifications of AGMA formulas based upon experiences from a wide range of applications.

The following organizations offer software programs for design and gear ratings according to methods outlined in AGMA publications: Fairfield Manufacturing Company Gear Software; Geartech Software, Inc.; PC Gears; Universal Technical Systems, Inc. For details and current listings, refer to AGMA's latest ''Catalog of Technical Publications.''

8.4 FLUID FILM BEARINGS by Vittorio (Rino) Castelli

REFERENCES: ''General Conference on Lubrication and Lubricants,'' ASME. Fuller, ''Theory and Practice of Lubrication for Engineers,'' 2d ed., Wiley. Booser, ''Handbook of Lubrication, Theory and Design,'' vol. 2, CRC Press. Barwell, ''Bearing Systems, Principles and Practice,'' Oxford Univ. Press. Cam-eron, ''Principles of Lubrication,'' Longmans Greene. ''Proceedings,'' Second International Symposium on Gas Lubrication, ASME. Gross, ''Fluid-Film Lubrication,'' Wiley. Gunter, ''Dynamic Stability of Rotor-Bearing Systems,'' NASA SP-113, Government Printing Office.

Plain bearings, according to their function, may be

Journal bearings, cylindrical, carrying a rotating shaft and a radial load

Thrust bearings, the function of which is to prevent axial motion of a rotating shaft

Guide bearings, to guide a machine element in its translational motion, usually without rotation of the element

In exceptional cases of design, or with a complete **failure of lubrication,** a bearing may run dry. The coefficient of friction is then between 0.25 and 0.40, depending on the materials of the rubbing surfaces. With the **bearing barely greasy,** or when the bearing is well lubricated but the speed of rotation is very slow, boundary lubrication takes place. The coefficient of friction may vary from 0.08 to 0.14. This condition occurs also in any bearing when the shaft is starting from rest if the bearing is not equipped with an oil lift.

Semifluid, or **mixed,** lubrication exists between the journal and bearing when the conditions are not such as to form a load-carrying fluid film and thus separate the surfaces. Semifluid lubrication takes place at comparatively low speed, with intermittent or oscillating motion, heavy load, insufficient oil supply to the bearing (wick or waste-lubrication, drop-feed lubrication). Semifluid lubrication may also exist in thrust bearings with fixed parallel-thrust collars, in guide bearings of machine tools, in bearings with copious lubrication where the shaft is bent or the bearing is misaligned, or where the bearing surface is interrupted by improperly arranged oil grooves. The coefficient of friction in such bearings may range from 0.02 to 0.08 (Fuller, Mixed Friction Conditions in Lubrication, *Lubrication Eng.,* 1954).

Fluid or **complete lubrication,** when the rubbing surfaces are completely separated by a fluid film, provides the lowest friction losses and prevents wear. A certain amount of oil must be fed to the oil film in order to compensate for end leakage and maintain its carrying capacity. Such lubrication can be provided under pressure from a pump or gravity tank, by automatic lubricating devices in self-contained bearings (oil rings or oil disks), or by submersion in an oil bath (thrust bearings for vertical shafts).

Notation

- $R =$ radius of bearing, length
- $r =$ radius of journal, length
- $c = mr = R r$ = radial clearance, length
- $W =$ bearing load, force
- μ = viscosity = force \times time/length²
- *Z* = viscosity, centipoise (cP); 1 cP = 1.45×10^{-7} lb \cdot s/in² $(0.001 \text{ N} \cdot \text{s/m}^2)$
- β = angle between load and entering edge of oil film
- η = coefficient for side leakage of oil
- ν = kinematic viscosity = μ/ρ , length²/time
- R_e = Reynolds number = umr/v
- P_a = absolute ambient pressure, force/area
- $\overline{P} = W/(ld) = \text{unit pressure}, \text{lb/in}^2$
- $N =$ speed of journal, r/min
- $m =$ clearance ratio (diametral clearance/diameter)
- $F =$ friction force, force
- $A =$ operating characteristic of plain cylindrical bearing
- P' = alternate operating characteristic of plain cylindrical bearing
- $h₀$ = minimum film thickness, length
- ε = eccentricity ratio, or ratio of eccentricity to radial clearance
- e = eccentricity = distance between journal and bearing centers, length
- f = coefficient of friction
- $f' =$ friction factor = $F/(\pi r l \rho u^2)$
- $l =$ length of bearing, length
- $d = 2r =$ diameter of journal, length
- K_f = friction factor of plain cylindrical bearing
- t_w = temperature of bearing wall
- t_0 = temperature of air
- t_1 = temperature of oil film
- $u =$ surface speed, length/time
- ω = angular velocity, rad/time
- ρ = mass density, mass/length³
- $\Lambda =$ bearing compressibility parameter = $6 \mu \omega r^2/(P_a c^2)$

INCOMPRESSIBLE AND COMPRESSIBLE LUBRICATION

Depending on the fluid employed and the pressure regime, the fluid density may or may not vary appreciably from the ambient value in the load-carrying film. Typically, oils, water, and liquid metals can be considered incompressible, while gases exhibit compressibility effects even at modest loads. The difference comes from the fact that, in incompressible lubricants, fluid flow rates are linearly proportional to pressure differences, whereas for compressible lubricants the mass flow rates are proportional to the difference of some power of the pressure. This is because the pressure affects the fluid density. The bearing behavior is somewhat dissimilar. In incompressible lubrication, gage pressures can be used and the value of the ambient pressure has no effect on the load-carrying capacity, which is linearly related to viscosity and speed. This is not true in compressible lubrication, where the value of ambient pressure has a direct effect on the load-carrying capacity which, in turn, increases with viscosity and speed, but only up to a limit dependent on the bearing geometry. In what follows, incompressible lubrication is treated first and compressible lubrication second.

Incompressible (Plain Cylindrical Journal Bearings)

Fluid lubrication in plain cylindrical bearings depends on the viscosity of the lubricant, the speed of the bearing components, the geometry of the film, and possible external sources of pressurized lubricant. The oil is entrained by the journal into the film by the action of the viscosity which, if the passage is convergent, causes the creation of a pressure field, resulting in a force sufficient to float the journal and carry the load applied to it.

The **minimum film thickness** h_0 determines the closest approach of the journal and bearing surfaces (Fig. 8.4.1). The allowable closest approach depends on the finish of these surfaces and on the rigidity of the journal and bearing structures. In practice, $h_0 = 0.00075$ in (0.019 mm) is common in electric motors and generators of medium speed, with

Fig. 8.4.1 Journal bearing with perfect lubrication.

steel shafts in babbitted bearings; $h_0 = 0.003$ in (0.076 mm) to 0.005 in (0.127 mm) for large steel shafts running at high speed in babbitted bearings (turbogenerators, fans), with pressure oil-supply for lubrication; $h_0 = 0.0001$ in (0.0025 mm) to 0.0002 in (0.005 mm) in automotive and aviation engines, with very fine finish of the surfaces.

Figure 8.4.2 gives the relationship between ε and the load-carrying coefficient *A* for a plain cylindrical journal. The operating characteristic

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of the bearing is

$$
A = (132/\eta)(1,000m)^{2}[P/(ZN)]
$$

In Fig. 8.4.1, β is the angle between the direction of the load *W* and the entering edge of the load-carrying oil film, in degrees. The entering edge is at the place where the hydrodynamic pressure is equal or nearly equal to the atmospheric pressure and may be at the location of the

Fig. 8.4.2 Eccentricity ratio for a plain cylindrical journal.

oil-distributing groove *B*, or at the end of the machined recess pocket as at *AA*. For **complete bearings,** i.e., when the inner surface of the bearing is not interrupted by grooves, β may be taken as 90°. The reason for this assumption is the fact that, where the film diverges, the bearing pumping action tends to generate negative pressure, which liquids cannot sustain. The film **cavitates;** i.e., it breaks up in regions of fluid intermixed with either air or fluid vapor, while the pressure does not deviate substantially from ambient. For a 120 $^{\circ}$ bearing with a central load, β may be taken as 60°.

The coefficient η corrects for side leakage. There is a loss of loadcarrying capacity caused by the drop in the hydrodynamic pressure *p* in the oil film from the midsection of the bearing toward its ends; $p = 0$ at the ends. The value of η depends on the length-diameter ratio l/d and ε , the eccentricity ratio. Values of η are given in Fig. 8.4.3.

EXAMPLE 1. A generator bearing, 6 in diam by 9 in long, carries a vertical downward load of 8,650 lb; $N = 720$ r/min. The diametral clearance of the bearing is 0.012 in; the bearing is split on its horizontal diameter, and the lower half is relieved 40° down on each side, for oil distribution along journal; the bearing arc is therefore 100°; with the load vertical, $\beta = 50^{\circ}$; bearing temperature 160°F. The absolute viscosity of the oil in the film is 12 centipoises (medium turbine oil). $P = W/d = 160$ lb/in²; $\mu = 12 \times 1.45 \times 10^{-7} = 17.4 \times$ 10^{-7} lb \cdot s/in². The solution is one of trial and error. By using Fig. 8.4.3 in conjunction with Fig. 8.4.2, only a few trials are necessary to obtain the answer. As a first trial assume $\varepsilon = 0.85$. For an *l*/*d* ratio of 1.5 in Fig. 8.4.3, η , the end-leakage factor, will be 0.77. Compute *A* using this value of η . $m = 0.012/6 = 0.002$.

$$
A = \frac{132}{0.77} (2)^2 \frac{160}{12 \times 720} = 12.7
$$

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Enter [Fig. 8.4.2 w](#page-116-0)ith this value of *a* and at $\beta = 50^{\circ}$, and find that $\varepsilon = 0.9$. This value is larger than the initial assumption for ε . As a second trial, $\varepsilon = 0.88$. Then $\eta = 0.8$, $A = 12.2$, and $\varepsilon = 0.89$. This is a sufficiently close check. The minimum film thickness is $h_0 = mr(1 - \varepsilon) = 0.002 \times 3 \times 0.12 = 0.0007$ in (0.01778 mm).

For severe operating conditions the value of *A* may exceed 18, the limit o[f Fig. 8.4.2.](#page-116-0) For complete journal bearings under extreme operating conditions, Fig. 8.4.4 should be used. The ordinate is P' , defined as shown. The curves are drawn for various values of *l*/*d* instead of values of β as i[n Fig. 8.4.2](#page-116-0). Values of ε may thus be obtained directly (Dennison, Film-Lubrication Theory and Engine-Bearing Design, *Trans. ASME,* **58,** 1936).

Fig. 8.4.4 Load-carrying parameter in terms of eccentricity.

EXAMPLE 2. A 360 $^{\circ}$ journal bearing 2¹/₂ in diam and 3⁷/₈ in long carries a steady load of 3,875 lb. Speed $N = 500$ r/min; diametral clearance, 0.0064 in; average viscosity of the oil in the film, 23.4 centipoises (SAE 20 light motor oil at 105°F). $P = 3,875/(2.5 \times 3.875) = 400$ lb/in². Value of $m = 0.0064/2.5 =$ 0.00256. Value of $l/d = 1.55$. First, attempt to us[e Figs. 8.4.2](#page-116-0) and 8.4.3 in this solution. Assume eccentricity ratio ε is 0.9. Then, i[n Fig. 8.4.3,](#page-116-0) with $l/d = 1.55$, value of η is determined as 0.8. *A* is calculated as 37. This is completely off scale i[n Fig. 8.4.2.](#page-116-0) Consider instead Fig. 8.4.4. Value of P' is computed as

$$
P' = 6.9(2.56)^2 \frac{400}{23.4 \times 500} = 1.54
$$

In Fig. 8.4.4, enter the curves with $P' = 1.54$, and move left to intersect the curve for $l/d = 1.5$. Drop downward to read a value for $1/(1 - \varepsilon)$ of 16. Then $\frac{1}{16}$ $1 - \varepsilon$, or the eccentricity ratio $\varepsilon = \frac{15}{16}$, or 0.94. The minimum film thickness, as in Example $1 = h_0 = mr(1 - \varepsilon)$, or

$$
h_0 = 0.00256 \times 1.25(1 - 0.94) = 0.0002
$$
 in (0.0051 mm)

Allowable mean bearing pressures in bearings with fluid film lubrication are given in Table 8.4.1. If the load maintains the same magnitude and direction when the journal is at rest (heavily loaded shafts, heavy gears), the mean bearing pressure should be somewhat less than when bearings are loaded only when running.

For internal-combustion-engine bearing design, Etchells and Underwood (*Mach. Des.,* Sept. 1942) list the following maximum design pressures for bearing alloys, pounds per square inch of projected area: lead-base babbitt (75 to 85 percent lead, 4 to 10 percent tin, 9 to 15 percent antimony) 600 to 800; tin-base babbitt (0.35 to 0.6 percent lead, 86 to 90 percent tin, 4 to 9 percent antimony, 4 to 6 percent copper) 800 to 1,000; cadmium-base alloy (0.4 to 0.75 percent copper, 97 percent cadmium, 1 to 1.5 percent nickel, 0.5 to 1.0 percent silver) 1,200 to 1,500; copper-lead alloy (45 percent lead, 55 percent copper) 2,000 to 3,000; copper-lead (25 percent lead, 3 percent tin, 72 percent copper) 3,000 to 4,000; silver (0.5 to 1.0 percent lead on surface, 99 percent silver) 5,000 up. The above pressures are based on fatigue life of 500 h at 300°F bearing temperature, and a bearing metal thickness 0.01 to 0.015 in for lead-, tin-, and cadmium-base metals and 0.25 in for copper, lead, and silver. At lower temperatures the life will be greatly extended.

Much higher pressures are encountered in rolling element bearings, such as ball and roller bearings, and gears. In these situations, the formation of fluid films capable of preventing contact between surface asperities is aided by the increase of viscosity with pressure, as exhibited by most lubricating oils. The relation is typically exponential, $\mu =$ $\mu_0e^{\alpha p}$, where α is the so-called pressure coefficient of viscosity.

Length-diameter ratios are usually chosen between $l/d = 1$ and $l/d = 1$ 2, although many engine bearings are designed with $l/d = 0.5$, or even less. In shorter bearings, the carrying capacity of the oil film is greatly impaired by the effect of side leakage. Longer bearings are used to restrain the shaft from vibration, as in line shafts, or to position the shaft accurately, as in machine tools. In power machines, the tendency is toward shorter bearings. Typical values are as follows: turbogenerators, 0.8 to 1.5; gasoline and diesel engines for main and crankpin bearings, 0.4 to 1.0, with most values between 0.5 and 0.8; generators and motors, 1.5 to 2.0; ordinary shafting, heavy, with fixed bearings, 2 to 3; light, with self-aligning bearings, 3 to 4; machine-tool bearings, 2 to 4; railroad journal bearings, 1.2 to 1.8.

For the **clearance between journal and bearing** see Fits in Sec. 8. Medium fits may be used for journals running at speeds under 600 r/min, and free fits for speeds over 600 r/min. Kingsbury suggests for these journals a diametral clearance = $0.002 + 0.001d$ in. In journals running at high speed, diametral clearance $= 0.002d$ should be used in order to lower the friction losses in the bearing. All units are in inches. The most satisfactory clearance should, of course, be based on a complete bearing analysis which includes both load-carrying capacity and heat generation due to friction. For example, a bearing designed to run at the extremely high speed of 50,000 r/min uses a diametral clearance of 0.0025 in for a journal with 0.8-in diameter, giving a clearance ratio, clearance/ diameter, of 0.00316.

For high-speed internal-combustion-engine bearings using forcedfeed lubrication, medium fits are used. Federal-Mogul recommends the following diametral clearances in inches per inch of shaft diameter for insert-type bearings: tin-base and high-lead babbitts, 0.0005; cadmiumsilver-copper, 0.0008; copper-lead, 0.001.

The dependence of the **coefficient of friction** for journal bearings on the bearing clearance, lubricant viscosity, rotational speed, and loading pressure, as reported by McKee and others, is shown in Sec. 3. A plot of the coefficient of friction against the parameter *ZN*/*P* is a convenient method for showing this relationship. *ZN*/*P* is a parameter based on mixed units. *Z* is the viscosity in centipoise, *N* is r/min, *P* is the mean pressure on the bearing due to the load, pounds per square inch of projected area, and *m* is the clearance ratio. Values of *ZN*/*P* greater than about 30 indicate fluid film conditions in the bearings. If the viscosity of the lubricant becomes lower or if there is a reduction in rotational speed or an increase in load, the value of *ZN*/*P* will become smaller until the coefficient of friction reaches a minimum value. Any further reduction in *ZN*/*P* will produce breakdown of the oil film, marking the transition from fluid film lubrication with complete separation of the moving surfaces to semifluid or mixed lubrication, where there is partial contact. As soon as semifluid conditions are initiated, there will be a sharp increase in the coefficient of friction. The critical value of *ZN*/*P*, where this transition takes place, will be lowest for a rigid bearing and shaft with finely finished surfaces.

Figure 8.4.5 shows a generalization of the relationship between the coefficient of friction for a journal bearing and the parameter *ZN*/*P*,

Fig. 8.4.5 Various zones of possible lubrication for a journal bearing.

indicating the various possible lubrication regimes that may be expected. For optimum design, a value of *ZN*/*P* somewhere between 30 and 300 would be recommended, but, in any case, the determination of minimum film thickness h_0 should be the deciding parameter. For extremely large values of *ZN*/*P*, resulting from high speeds and low loads,

Fig. 8.4.6 Variation of the friction factor of a bearing with eccentricity ratio.

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whirl instability may be developed. (See material on gas-lubricated bearings in this section.) With large values of *ZN*/*P* and a lubricant having a low kinematic viscosity, turbulent conditions may develop in the bearing clearance.

The friction force in plain journal bearings may be estimated by the use of the expression $F = K_f \mu N r l/m$, where μ is in lb·s/in² units. The value of K_f depends upon the magnitude of ε and the type of bearing. Figure 8.4.6 shows values of K_f for a complete bearing, a 150° partial bearing, and a 120° partial bearing, assuming that the clearance space is at all times filled with lubricant. Note that *F* is the friction force at the surface of the bearing. Consequently, the friction torque is obtained by multiplying *F* by the bearing radius.

EXAMPLE 3. As an illustration of the use of Fig. 8.4.6, determine the friction force in the bearing of Example 2. This is a complete journal bearing 21⁄2-in diam by 3% in. The value of ε was determined as 0.94. From Fig. 8.4.6, $K_f = 2.8$. Then

$$
F = \frac{2.8 \times 23.4 \times 1.45 \times 10^{-7} \times 500 \times 1.25 \times 3.875}{0.00256}
$$

= 8.97 lb (4.08 kg)

The coefficient of friction $F/W = 8.97/3875 = 0.00231$. The mechanical loss in the bearing is *FV*/33,000 hp, where *V* is the peripheral velocity of the journal, ft/min.

Friction hp =
$$
(8.97 \times 500 \times \pi \times 2.5)/(33,000 \times 12)
$$

= 0.089 hp (66.37 W)

Departure from laminarity in the fluid film of a journal bearing will increase the friction loss. Figure 8.4.7 (Smith and Fuller, Journal Bearing Operation at Super-laminar Speeds, *Trans. ASME,* **78**, 1956) shows test results for such bearings, expressed in terms of a Reynolds number for the fluid film, $R_e = u m r/v$. Laminar conditions hold up to an R_e of about 1,000. Friction may be calculated for laminar flow by using Fig. 8.4.6 or the left branch of the curve in Fig. 8.4.7, where $f' = 2/R_e$, and which applies to low values of the eccentricity ratio ($K_f = 0.66$). The values from Fig. 8.4.7 may be converted to friction torque *T* by the use of the expression $T = f' \pi \rho u^2 r^2 l$, where ρ is the mass density of the lubricant. In Fig. 8.4.7, a transition region spans values of the Reynolds number from 1,000 to 1,600. Here, two types of flow instability can occur. Usually, the first is due to **Taylor vortices** which are wrapped in

Fig. 8.4.7 Friction f' as a function of the Reynolds number for an unloaded journal bearing with $l/d = 1$. *(Smith and Fuller.)*

regular circumferential structures, each of which occupies the entire clearance. The onset of this phenomenon takes place at a value of the Reynolds number exceeding the threshold $R_e = 41.1(r/c)^{1/2}$. The second instability is due to turbulence, occurring at $R_e > 2,000$.

EXAMPLE 4. A journal bearing is 4.5 in diameter by 4.5 in long. Speed 22,000 r/min. $mr = 0.002$ in. Viscosity μ , 1 cP (water) = 1.45 \times 10⁻⁷ lb·s/in²; mass density $\rho = 62.4/1,728 \times 386 = 9.35 \times 10^{-5} \text{ lb} \cdot \text{s}^2/\text{in}^4$; $v = \mu/\rho = 1.45 \times$ $10^{-7}/9.35 \times 10^{-5} = 0.155 \times 10^{-2}$ in²/s; $u = 22,000 \times 2\pi \times 2.25/60 = 5,180$ in/s; $R_e = 5{,}180 \times 0.002/0.155 \times 10^{-2} = 6{,}680$. This would indicate turbulence in the film. Value of *f'* is then $0.078/6,680^{0.43} = 0.078/44.2 = 1.765 \times 10^{-3}$. Friction torque $T = 1.765 \times 10^{-3} \times \pi \times 9.35 \times 10^{-5} \times 5,180^{2} \times 2.25^{2} \times 4.5$, $T = 317.5$ in \cdot lb. Friction horsepower = $2\pi T N/12 \times 33,000 = 2\pi \times 317.5 \times$ $22,000/12 \times 33,000$, FHP = 111 (82.77 kW).

8-120 FLUID FILM BEARINGS

In self-contained bearings (electric motor, line shaft, etc.) without external oil or water cooling, the **heat dissipation** is equal to the heat generated by friction in the bearing.

The heat dissipated from the outside bearing wall to the surrounding air is governed by the laws of heat transfer $Q = hS(t_w - t_0)$, where *S* is the surface area from which the heat is convected, *Q* is the rate of energy flow; t_w and t_0 are the temperatures of the wall and ambient air, respectively; and *h* is the heat convection coefficient, which has values from 2.2 Btu/(h \cdot ft² \cdot °F) for still air to 6.5 Btu/(h \cdot ft² \cdot °F) for air moving at 500 ft/min. Calculations of heat loss are extremely important due to the strong temperature dependence of the viscosity of most oils.

The temperature of the oil film will be higher than the temperature of the bearing wall. Typical ranges of values according to Karelitz (*Trans. ASME,* **64**, 1942), Pearce (*Trans. ASME,* **62**, 1940), and Needs (*Trans. ASME,* **68**, 1948) for self-contained bearings with oil bath, oil ring, and waste-packed lubrication are shown in Fig. 8.4.8.

Fig. 8.4.8 Temperature rise of the film.

EXAMPLE 5. The frictional loss for the generator bearing of Example 1, computed by the method outlined in Example 3, is 0.925 hp with $\varepsilon = 0.88$, $K_f = 1.6$, and $F = 27$ lb. Operating in moving air the heat dissipated by the bearing housing will be $L = 6.5S(t_w - t_0)$. Since this is a self-contained bearing, the heat dissipated is also equal to the heat generated by friction in the oil film, or $L = 0.925 \times$ 2,545 = 2,355 Btu/h. With $S = 25 \times 6 \times 9/144 = 9.4$ ft², $t_w = t_0 = 2,355/6.5 \times$ $9.4 = 38.5$ °F. This is the temperature rise of the bearing wall above the ambient room temperature. For an 80°F room, the wall temperature of the bearing would be about 118°F. In Fig. 8.4.8 an oil-ring bearing in moving air with a temperature rise of wall over ambient of 38°F should have a film temperature 50°F higher than that of the wall. The film temperature on the basis of Fig. 8.4.8 will then be $80 +$ $38 + 50$, or 168°F. This is close enough to the value of the film temperature of 160°F from Example 1, with which the friction loss in the bearing was computed, to indicate that this bearing can operate without the need for external cooling.

To predict the operating temperature of a self-contained bearing, the cut-and-try method shown above may be used. First, an oil-film temperature is assumed. Viscosity and friction losses are calculated. Then the temperature rise of the wall over ambient is computed so as to dissipate to the atmosphere an amount of heat equal to the friction loss. Lastly from Fig. 8.4.8 the corresponding oil-film temperature is estimated and compared to the value that was originally assumed. A few adjustments of the assumed film temperature will produce satisfactory agreement and indicate the leveling-off temperature of the bearing. Self-contained bearings have been built with diameters of 3, 8, and 24 in (7.62, 20.32, and 60.96 cm) to operate at shaft speeds of 3,600, 1,000, and 200 r/min, respectively. These designs indicate a rough limit for bearings with no external cooling. The highest bearing temperature permissible with normal lubricants is about 210°F (100°C).

The temperature of automotive-type bearings is held within safe limits by using a **pressure-feed oil supply.** Sufficient lubricant is forced through the bearing to act as a coolant and prevent overheating. One widely used practice is to place a circumferential groove at the center of the bearing to which the oil supply is fed. This is effective as far as cooling is concerned but has the disadvantage of interrupting the active length of the bearing and lowering its *l*/*d* ratio (see Fig. 8.4.9). The axial

flow through each side of the bearing is given by
\n
$$
Q_1 = \frac{\Delta P m^3 r^4 \pi}{6 \mu b} \left(1 + \frac{3}{2} \epsilon^2 \right)
$$

where *b* is the effective axial length of the half bearing and ΔP is the difference between the oil pressure in the circumferential groove and

Fig. 8.4.9 Bearing with central circumferential groove.

the pressure at the ends of the bearing. The value of the last term in this equation will vary from 1.0 for a concentric shaft and bearing indicated by $\varepsilon = 0$ to a value of 2.5 for the extreme case of the shaft touching the bearing wall, indicated when $\varepsilon = 1$. Most of the heat caused by friction in the bearing is carried away by the circulating oil. Permissible temperature rises for this type of bearing may range from 15 to 50°F (8 to 28°C). In extreme cases a rise of $100^{\circ}F$ (55°C) can be tolerated for high-strength bearing materials. The lower values of temperature rise usually indicate needlessly large oil flow. Such a condition will result in an excessive friction loss in the bearing.

EXAMPLE 6. The bearing of Examples 2 and 3 is lubricated by a circumferential groove with an oil supply pressure of 30 lb/in² and, as before, $\varepsilon = 0.94$, $m = 0.0026$, and $\mu = 23.4 \times 1.45 \times 10^{-7}$ lb·s/in². Length *b* is about 1.93 in.

$$
Q_1 \text{ flow out one side} = \frac{30 \times 0.0026^3 \times 1.25^4 \times \pi}{6 \times 23.4 \times 1.45 \times 10^{-7} \times 1.93} \times [1 + 3/2(0.94)^2] = 0.240 \text{ in}^3\text{/s} (3.93 \text{ cm}^3\text{/s})
$$

Total flow (two sides) = 0.48 in³/s = 53 lb/h for sp gr = 0.85. The friction loss from Example 3 = 0.089 hp = 226 Btu/h. With a specific heat of 0.5 Btu/(lb·°F) and assuming that all the friction energy is given up to the oil in the form of heat, the temperature rise $\Delta t = 226/0.5 \times 53 = 8.5^{\circ}F (4.72^{\circ}C)$.

A definite **minimum rate of oil feed** is required to maintain a fluid film in journal bearings. This makes no allowance for the additional flow that may be needed to cool the bearings. However, many industrial bearings run at relatively low speeds with light loads and, as a consequence, additional oil flow to provide cooling is not necessary. But if a fluid film is desired, a definite minimum amount of lubricant is required. If the volume of lubricant fed to the bearing is less than this minimum requirement, there will not be a complete fluid film in the bearing. Friction will rise, wear will become greater, and the satisfactory service life of such a bearing will be reduced. This minimum lubricant supply can be evaluated by using the equation

$$
Q_M = K_M \text{urml}
$$

where Q_M is the flow rate and K_M is approximately 0.006.

Rotating shaft

Fig. 8.4.10 Siphon wick. **Fig. 8.4.11** Bottom wick.

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EXAMPLE 7. The minimum feed rate for a journal bearing 21⁄8-in diam by 21⁄8 in long will be determined. Diametral clearance is 0.0045 in; speed, 1,230 r/min; load, 40 lb/in² based on projected area. $u = 1,230 \times \pi \times 2.125 =$ 10,220 in/min, $r = 1.062$ in, $m = 0.0045/2.125 = 0.00212$, $l = 2.125$ in. Substituting,

$$
Q_M = 0.006 \times 10,220 \times 1.062 \times 0.00212 \times 2.125
$$

= 0.28 in³/min

(Fuller and Sternlicht, Preliminary Investigation of Minimum Lubricant Requirements of Journal Bearings, *Trans. ASME,* **78**, 1956.)

Many bearings are supplied with oil at low rates of feed by **felts, wicks,** and **drop-feed oilers.** Wicks can supply substantial rates of feed if they are properly designed. The two basic types of wick feed are siphon wicks, as shown i[n Fig. 8.4.10,](#page-119-0) and bottom wicks, as shown in Fig.

Fig. 8.4.12 Oil delivery with siphon wic[k \(Fig. 8.4.10\)](#page-119-0).

8.4.11. Data on oil delivery for these wicks are shown in Figs. 8.4.12 and 8.4.13. The data, from the American Felt Co., are for SAE Fl felts, based on a cross-sectional area of 0.1 in2. The flow rate is indicated in drops per minute. One drop equals 0.0026 in³ or 0.043 cm³.

EXAMPLE 8. If it is desired to deliver 12.5 drops/min to a journal bearing, and if the viscosity of the oil is 212 s Saybolt Universal at 70°F, and if *L*[, Fig. 8.4.10,](#page-119-0) is 5 in, what size of round wick would be required? From Fig. 8.4.12, for the stated conditions the delivery rate would be 0.9 drop/min for an area of 0.1 in². If 12.5 drops/min is needed, this would mean an area of 12.5 divided by 0.9 and multiplied by 0.1, or 1.4 in². For a round wick this would mean a diameter of 1³/₈ in (3.49 cm).

If a **bottom wick** is considered with $L = 4$ in[, Fig. 8.4.11](#page-119-0), then in Fig. 8.4.13 the delivery rate using the same oil would be 1.6 drops/min; and if 12.5 drops/min is required, the area would be 12.5 divided by 1.6 and multiplied by 0.1, or 0.78 in2. This would mean a bottom wick of 1 in diam if it is round (2.54 cm).

When journal **bearings** are **started, stopped,** or **reversed,** or whenever conditions are such that the operating value of *ZN*/*P* falls below the critical value for that bearing, the oil film will be ruptured and metal-tometal contact will increase friction and cause wear. This condition can be eliminated by using a **hydrostatic oil lift.** High-pressure oil is introduced to the area between the bottom of the journal and the bearing (Fig. 8.4.14). If the pressure and quantity of flow are great enough, the shaft, whether it is rotating or not, will be raised and supported by an oil film. Neglecting axial flow, which is small, the flow up one side is

$$
Q_1 = \frac{Wrm^3}{A\mu} \quad \text{in}^{2}/\text{s}
$$

and the inlet pressure required, $P_{o} = \mu Q_1 B/(b r^2 m^3)$, where *b* is the axial length of the high-pressure recess. Values of *A* and *B* are dimensionless factors which represent geometric effects and are given in the following table as a function of ε :

Fig. 8.4.13 Oil delivery with bottom wic[k \(Fig. 8.4.11\)](#page-119-0).

Current practice is to make the total area of the high-pressure recess in a bearing 21⁄2 to 5 percent of the projected area *ld* of the bearing. It is generally desirable to use a check valve in the supply line to the oil lift so that, when the journal builds up a hydrodynamic oil-film pressure, reverse flow of oil in the supply line will be prevented.

EXAMPLE 9. A 4,000-in-diam journal rests in a bearing of 4.012-in-diam. SAE 30 oil at 100°F (105 cP) is supplied under pressure to a groove at the lowest point in the bearing. Length of bearing, 6 in, length of groove, 3 in, load on bearing, 3,600 lb. What inlet pressure and oil flow are needed to raise the journal 0.004 in?

$$
h_0 = mr(1 - \varepsilon)
$$

0.004 = 0.006(1 - \varepsilon)

$$
\varepsilon = 0.333
$$

From the table, $A = 44.5$, $B = 42$.

$$
Q_1 = \frac{3,600 \times 2}{44.5 \times 105 \times 1.45 \times 10^{-7}} (0.003)^3
$$

= 0.287 in³/s, one side (4.70 cm³/s)

Flow from both sides = $(0.287 \times 2) \times 60/231 = 0.149$ gal/min (0.564 l/min). Oil supply pressure is

$$
P_o = \frac{105 \times 1.45 \times 10^{-7} \times 0.287 \times 42}{3 \times 4} \times \frac{1}{0.003^3} = 566 \text{ lb/in}^2
$$

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Fig. 8.4.15 Load-carrying capacity and flow for journal bearings *(Loeb).* Lengths in inches.

An adjustable constant-volume pump or a spur-gear pump with a capacity of about 1,000 lb/in2 (6.894 kN/m2) should be used to allow for pressure that may be built up in the line before the journal begins to rise.

Other configurations for hydrostatically lubricated journal bearings are shown in Fig. 8.4.15. These were obtained by means of electric analog solutions (Loeb, Determination of Flow, Film Thickness and Load-Carrying Capacity of Hydrostatic Bearings through the Use of the Electric Analog Field Plotter, *Trans. ASLE,* **1**, 1958). The data from Fig. 8.4.15 are exact for a uniform film thickness corresponding to $\varepsilon = 0$ but may be used with discretion for other values of ε .

Multiple recesses are used in externally pressurized bearings in order to provide local **stiffness**. This term indicates that the bearing resists shaft motions in any direction, and it is achieved by properly arranging the feeding network according to a strategy called **compensation**. Three main types are employed: orifice (and its variant, inherent), capillary, and fixed flow rates. In the first two, the idea is to insert a hydraulic resistance in each of the recess feeding lines and to use a single pump to feed all recesses. The flow rate *q* through orifices varies with the square root of the pressure drop Δp

$$
q \propto \sqrt{\Delta p}
$$

while for capillary tubes the relation is linear:

$$
q = \frac{\pi \, \Delta p \, d^4}{64 \, l_1 \, \mu}
$$

The general rule of thumb in designing orifices or capillary restrictors is to generate a pressure drop approximately equal to that taking place through the bearing, i.e., from the recesses to the ambient. The recess geometry and distribution, on the other hand, are designed so that $W =$ $0.5p_{\text{recess}}$ *DL*. Thus, the pump supply pressure is 4 times the average bearing pressure. The bearing stiffness is usually equal to $K =$ 0.5*p*recess *DL*/*c*.

The third method of compensation consists of forcing the same amount of flow to reach each recess regardless of clearance distribution. This can be achieved either by using separate pumps for each recess or by using a hydraulic device called a *flow divider.* With recess distributions as indicated above, the pump pressure need only be double the average bearing pressure; thus, this method of compensation leads to half the power dissipation of the other two. It is commonly used in large machinery, where power consumption must be limited. The polar axis bearings of the 200-in Hale telescope on Mount Palomar were the first large-scale demonstration of this technique. The azimuth axis thrust bearing of the 270-ft-diameter Goldstone radio telescope is probably the largest example of this type of bearing.

ELEMENTS OF JOURNAL BEARINGS

Typical dimensions of solid and split **bronze bushings** are given in Table 8.4.2.

Bronze bushings made from hard-drawn sheets and rolled into cylindrical shape are made with a wall thickness of only 1⁄32 in for bearings up to $\frac{1}{2}$ in diam and with a wall thickness of $\frac{1}{16}$ in for bearings from 1 in diam up. The wall thickness of these bearings depends chiefly upon the strength of the material which supports them. Bushings of this type are pressed into place, and the bearing surface is finished by burnishing with a slightly tapered bar to a mirror finish. The allowable bearing pressures may exceed those of cast bronze shown i[n Table 8.4.1](#page-117-0) by 10 to 20 percent.

Babbitt linings in larger bearings are generally employed in thickness of 1⁄8 in or over and must be provided with sufficient anchorage in the

Table 8.4.2 Wall Thickness of Bronze Bushings, in

| | Diam of journal, in | | | | | | | |
|-----------------------|---------------------|-----------------------------|-------------------|--------------------|-------------------------------|--------------------|--------------------|--|
| | $\frac{1}{4}$ | $\frac{1}{4} - \frac{1}{2}$ | $\frac{1}{2}$ - 1 | $1 - 1\frac{1}{2}$ | $1\frac{1}{2} - 2\frac{1}{2}$ | $2\frac{1}{2}$ – 4 | $4 - 5\frac{1}{2}$ | |
| Solid bushing, normal | $\frac{1}{16}$ | $\frac{3}{32}$ | ⅓ | $\frac{3}{16}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{1}{2}$ | |
| Split bushing, normal | $\frac{3}{32}$ | $\frac{1}{8}$ | $\frac{5}{32}$ | $\frac{7}{32}$ | $\frac{5}{16}$ | 15/32 | $\frac{5}{8}$ | |
| Solid bushing, thin | $\frac{1}{16}$ | $\frac{3}{32}$ | $\frac{3}{32}$ | $\frac{1}{8}$ | $\frac{3}{16}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | |
| Split bushing, thin | $\frac{1}{16}$ | $\frac{3}{32}$ | $\frac{1}{8}$ | $\frac{3}{16}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{1}{2}$ | |

supporting shell. The anchors take the form of dovetailed grooves or holes drilled in the shell and counterbored from the outside.

Improved conditions are obtained by sweating or bonding the babbitt to the shell by tinning the latter, using potassium chlorate as flux. Tinbase babbitts and other low-strength materials evidence some yielding when subjected to heavy pressures. This tendency may be alleviated by the use of a thinner layer of the bearing material, fused either to a bronze or to a steel shell. This improves the fatigue life of the bearing material. Standard bearing inserts of this type are available in tin-base babbitts, high-lead babbitts, cadmium alloys, and copper-lead mixtures in diameters up to about 6 in (15.24 cm) (Fig. 8.4.16). A few materials can be obtained in sizes up to 8 in (20.32 cm). Some types are available with flanges or with other special features. The bearing lining may vary from about 0.001 in (0.025 mm) to 0.1 in (2.5 mm) in thickness depending upon the size of the bearing.

Fig. 8.4.16 Bearing insert.

Figure 8.4.17 shows the principal types of bonded babbitt linings. Figure 8.4.17*a* is for normal operating conditions. Figure 8.4.17*b* is for more severe operating conditions.

General practice for the **thickness of babbitt lining and shells** is as follows: Fig. 8.4.18, $b = \frac{1}{32}d + \frac{1}{8}$ in, $S = 0.18d$ for bronze or steel = 0.2*d* for cast iron; Fig. 8.4.18*a*, $t = b/2 + \frac{1}{16}$ in, $W = 1.8t$, $W_1 = 2.2t$.

Solid bronze or steel bushings, when pressed into the bearing housing, must be finished after pressing in. Light press fits and securing by

setscrews or keys are preferable to heavy press fits and no keying, since heavy pressure, especially in thin-walled bushings, will set up stresses which will release themselves if bearings should run hot in service and will result in closing in on the journal and scoring when cooling.

Uniform Load Distribution Misalignment between journal and bearing should never be so great as to cause metallic contact. The maximum allowable inclination α of the shaft to the bearing is given by $\tan \alpha = md/l$.

Whenever the deflection angle of the bearing installation is greater than α , either the bearing length should be reduced or, if that is not feasible, the bearing should be mounted on a spherical seat to permit self-alignment.

Oil grooves are of two kinds, axial and circumferential; the former distribute the oil lengthwise in the bearing; the latter distribute it around the shaft at the oil hole, and also collect and return oil which would

otherwise be forced out at the ends of the bearing. Grooves have often been put into bearings indiscriminatingly, with the result that they scrape off the oil and interrupt the film.

In Fig. 8.4.19, *W* is the resultant force or load, pounds, on the bearing or journal. The radial ordinates P_1 , to the dotted curve, show the pressures, lb/in2, of the journal on the oil film due to the load when there is no axial groove, while the

ordinates P_2 , to the solid curve, show the pressures with an incorrectly located groove. Since there is no oil pressure near the groove, the permissible load *W* must be reduced or the film will be ruptured.

Groove dimensions (Fig. 8.4.20) are given by the following relations: $a = \frac{1}{3}$ wall thickness; $W_o = 2.5a$; $W_d = 3a$; $c = 0.5W_d$; $f = \frac{1}{16}$ in to $0.5W_{d}$.

In order to maintain the oil film, **the axial distributing groove should be placed in the unloaded sector** of the bearing. The location of grooves in a variety of cases is shown in Figs. 8.4.21 to 8.4.30.

Fig. 8.4.20 Lubrication and drainage grooves.

Horizontal Bearings, Rotational Motion

DIRECTION OF LOAD KNOWN AND CONSTANT

Load downward or inside the lower 60° segment as in the case of ring-oiling bearings (Fig. 8.4.21).

Load at an angle more than 45° to the vertical centerline [\(Fig. 8.4.22\)](#page-123-0). In force- or drop-feed oiling, the oil inlet may be anywhere within the no-load sector [\(Fig. 8.4.23\)](#page-123-0).

Oil can be introduced through the center of the revolving shaft [\(Fig.](#page-123-0) [8.4.24\)](#page-123-0).

Fig. 8.4.21

8-124 FLUID FILM BEARINGS

Where oil-ring electric-motor bearings will be subjected by the purchaser to belt loads varying from vertical downward to horizontal, a continuous type of oil groove developed by General Electric Co. has proved very successful (Fig. 8.4.25). There are no critical spots with this groove because only a small percentage of the babbitt surface is removed along any axial line.

Fig. 8.4.22

Fig. 8.4.24

ROTATING LOAD

For rotating shafts, a circumferential groove at the middle of the bearing and an axial groove on the no-load side (Fig. 8.4.26).

For stationary shafts and rotating bearings, a circumferential groove in the bearing and an axial groove on the no-load side. The oil hole is in the shaft at the midlength of the bearing (Fig. 8.4.27).

LOAD DIRECTION UNCERTAIN

Oil-ring bearings [\(Figs. 8.4.21](#page-122-0) and 8.4.22) may be used, although they have defects under certain load directions. With forced or drop feed, the oil hole enters a circumferential groove at the middle of the bearing and the axial groove is omitted (Fig. 8.4.28). Arrangements for introducing oil through the rotating shaft can be made.

Bearings with Oscillatory Motion

DIRECTION OF LOAD CONSTANT

No oil film can be built up owing to the small sliding velocity, and boundary lubrication will exist. Axial grooves in the loaded sector distribute the lubricant to all parts of the bearing and avoid dry spots (Fig. 8.4.29).

Fig. 8.4.29 Fig. 8.4.30

LOAD DIRECTION REVERSED DURING **OSCILLATION**

Fluid film lubrication is possible, at least during part of the motion, owing to the vacuum caused by shaft moving back and forth. Figure 8.4.30 shows grooving which may be modified to suit local conditions. This arrangement is also advisable for bearings under a load which reverses in direction periodically without any rotation of the bearing. The lubrication may then provide an oil cushion to soften shocks.

Bearing seals are used to prevent oil leakage from the bearing housing and to protect the bearing from outside dust, water, vapors, etc. A drainage groove at the end of the bearing is effective to divert the oil passing through the bearing back into the oil well (Fig. 8.4.31*a*). The drain holes at the bottom of the groove must be ample for passage of the oil flow.

Fig. 8.4.31 Sealing end grooves.

An oil thrower mounted on the shaft is shown in Fig. 8.4.31*b*. The bearing housing may be provided with a single (Fig. 8.4.31*c*) or double collecting groove, or with brass or aluminum strip scrapers (Fig. 8.4.31*d*), to collect the oil creeping along the shaft.

For protection from dust, etc., felt packing rings are often used (Fig. 8.4.31*e*). The felt ring is soaked in oil to prevent charring by friction heat. In severe cases, additional protection by a labyrinth runner is very effective (Fig. 8.4.31*f*).

Standard seals are available for oil and grease retention as shown in

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Fig. 8.4.32*a*, *b*, and *c*. The seal material that is pressed against the rotating shaft is typically made of synthetic rubber, which is satisfactory for temperatures as high as about 250°F (121°C). Figure 8.4.32*a* shows the seal material pressed against the shaft by a series of flexible fingers

Fig. 8.4.32 Seals for oil and grease retention.

or leaf springs. In Fig. 8.4.32*b* a helical garter spring provides the gripping force. In Fig. 8.4.32*c* the rubber acts as its own spring.

Types of bearings are shown in Figs. 8.4.33 to 8.4.38. They include the principal methods of lubrication and types of construction.

Oiless bearings is the accepted term for self-lubricating bearings containing lubricants in solid or liquid form in their material. Graphite, molybdenum disulfide, and Teflon are used as solid lubricants in one group, and another group consists of porous structures (wood, metal), containing oil, grease, or wax.

Full and dotted lines for indeterminate load

Fig. 8.4.34 Rigid ring-oiling pillow block. *(Link Belt Co.)*

Fig. 8.4.35 Split bearing with one chain. Main crankshaft bearing; vertical oil engine.

Graphite-lubricated bearings (bridge bearings, sheaves, trolley wheels, high-temperature applications) consist generally of cast bearing bronze as a supporting structure containing various overlapping designs of grooves which are filled with graphite. The graphite is mixed with a binder, and the plastic mass is pressed into the cavities to the hardness of a lead pencil; 45 percent of the bearing area may be graphite.

Porous-metal bearings, compressed from metal powders and sintered, contain up to 35 percent of liquid lubricant. See ASTM B202-45T for sintered bronze and iron bearings, and also Army and Navy Specification AN-B-7G. The porous metal generally consists of a 90-10 copper-

Fig. 8.4.36 Crankshaft main bearing. Horizontal engine with drop-feed lubrication.

tin bronze with $1\frac{1}{2}$ percent graphite. These bearings do not require oil grooves since capillarity distributes the oil and maintains an oil film. If additional lubrication from an oil well should be provided, oil will be absorbed through the porous wall as required. For high temperatures where oil will carburize, a higher percentage of graphite (6 to 15 percent) is used.

Porous-metal bearings are used where plain metal bearings are impractical because of lack of space, cost, or inaccessibility for lubrication, as in automotive generators and motors, hand power tools, vacuum cleaner motors, and the like.

THRUST BEARINGS

At low speeds, shaft shoulders or collars bear against flat bearing rings. The lubrication may be semifluid, and the friction is comparatively high.

For hardened-steel collars on bronze rings, with intermittent service, pressures up to 2,000 lb/in2 (13,790 kN/m2) are permissible; for continuous low-speed operation, 1,500 lb/in2 (10,341 kN/m2); for steel collars on babbitted rings, 200 lb/in2 (1,378.8 kN/m2). In multicollar thrust bearings, the values are reduced considerably because of the difficulty in distributing the load evenly between the several collars.

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The performance of the bearing thrust rings is much improved by the introduction of **grooves** with tapered lands as shown in Fig. 8.4.39. The lands extend on either side of the groove. The taper angle of the lands is very slight, so that a pressure oil film is formed between the bearing ring

Fig. 8.4.39 Thrust collar with grooves fitted with tapered lands.

and the collar of the shaft. It is generally known that slightly tapered radial grooves will develop a hydrodynamic load-carrying film, when formed in the manner of Fig. 8.4.39. The taper angle should be on the order of 0.5°. Alternatively, a shallow recessed area that is a couple of

film thicknesses deep can be used in place of the taper.

For high speeds or where low friction losses and a low wear rate are essential, **pivoted segmental thrust bearings** are used (Kingsbury thrust bearing, or Michell bearing in Europe). The bearing members in this type are tiltable shoes which rest on hard steel buttons mounted on the bearing housing. The shoes are free to form automatically a wedge-shaped oil film between the shoe surface and the collar of the shaft (Figs. 8.4.40 to 8.4.42).

Fig. 8.4.40 Kingsbury thrust bearing with six shoes.

The **minimum oil-film thickness** h_0 , in, between the shoe and the collar, at the trailing edge of the shoe, is approximately

$$
h_0 = 0.26 \sqrt{\mu u l / P_{\text{avg}}}
$$

where μ is the absolute viscosity; μ is the velocity of the collar, on the mean diam; *l* is the length of a shoe, at the mean diam of the collar, in the direction of sliding motion; P_{avg} is the average load on the shoes. As indicated in Fig. 8.4.40, $b = l$, approximately. The standard thrust bearings have six shoes. Load-carrying capacities of Kingsbury thrust bearings are given in [Table 8.4.3.](#page-126-0)

Fig. 8.4.41 Left half of six-shoe self-aligning equalizing horizontal thrust bearing for load in either axial direction.

The coefficient of friction in Kingsbury thrust bearings, referred to the mean diameter of the shoes, is approximately $f = 11.7h₀/l$, where $h₀$ is computed as shown above. Figures 8.4.41 and 8.4.42 show typical pivoted segmental thrust bearings. They usually embody a system of

Fig. 8.4.42 Half section of mounting for vertical thrust bearing.

rocking levers which are used for alignment and equalization of load on the several shoes (Fig. 8.4.43).

Thrust may be carried on a hydrostatic step bearing as shown schematically in Fig. 8.4.44, where high-pressure oil at P_o is supplied at the

Fig. 8.4.43 Kingsbury thrust bearings. (Developed cylindrical sections.)

center of the bearing from an external pump. The lubricant flows radially outward through the annulus of depth h_0 and escapes at the periphery of the shaft at some pressure P_1 which is usually at atmospheric pressure. An oil film will be present whether the shaft rotates or not. Friction in these bearings can be made to approach zero, depending

Fig. 8.4.44 Hydrostatic step bearing.

Table 8.4.3 Capacities of Six-Shoe Standard-Duty Horizontal and Vertical Thrust Bearings (Based on viscosity of 150 s Saybolt at operating temperatures. Capacities given may be increased from 10 to 25% if viscosity is increased in same proportion)

| | | | | | Speed, r/min | | | | | Speed, r/min | | | | | |
|-----------------------------|-------|---------------------|------|------|--------------|-------|----------|-----------------|---------------------|--------------|-------|-------|-------|-------|-------|
| Bearing | Area, | 100 | 200 | 400 | 800 | 1,800 | 3,600 | Bearing | Area, | 100 | 150 | 200 | 300 | 500 | 700 |
| in ² size, in | | Safe load, 103 lb | | | | | size, in | in ² | Safe load, 103 lb | | | | | | |
| 5 | 12.5 | 1.44 | 1.7 | 2.0 | 2.4 | 2.9 | 3.5 | 19 | 180 | 40.00 | 44.0 | 48.0 | 53.0 | 60.0 | 65.0 |
| 6 | 18.0 | 2.30 | 2.7 | 3.2 | 3.8 | 4.6 | 5.5 | 21 | 220 | 51.00 | 57.0 | 61.0 | 68.0 | 77.0 | 84.0 |
| 7 | 24.5 | 3.30 | 3.9 | 4.7 | 5.6 | 6.8 | 8.0 | 23 | 264 | 65.00 | 72.0 | 77.0 | 85.0 | 97.0 | 105.0 |
| 8 | 32.0 | 4.60 | 5.5 | 6.6 | 7.8 | 9.6 | 11.4 | 25 | 312 | 80.00 | 88.0 | 95.0 | 105.0 | 119.0 | 123.0 |
| 9 | 40.5 | 6.20 | 7.4 | 8.8 | 10.4 | 13.0 | 15.0 | 27 | 364 | 97.00 | 107.0 | 115.0 | 127.0 | 144.0 | 146.0 |
| $10\frac{1}{2}$ | 55.1 | 9.20 | 10.8 | 13.0 | 15.4 | 19.0 | 22.0 | 29 | 420 | 116.00 | 128.0 | 137.0 | 152.0 | 168.0 | 168.0 |
| 12 | 72.0 | 12.80 | 15.2 | 18.0 | 21.0 | 26.0 | 29.0 | 31 | 480 | 137.00 | 151.0 | 162.0 | 180.0 | 192.0 | 192.0 |
| $13\frac{1}{2}$ | 91.1 | 17.20 | 20.0 | 24.0 | 29.0 | 35.0 | 36.0 | 33 | 544 | 160.00 | 177.0 | 189.0 | 210.0 | 220.0 | 220.0 |
| 15 | 112.5 | 22.00 | 26.0 | 32.0 | 37.0 | 45.0 | | 37 | 684 | 215.00 | 235.0 | 250.0 | 275.0 | 275.0 | |
| 17 | 144.5 | 30.00 | 36.0 | 43.0 | 51.0 | 58.0 | | 41 | 840 | 275.00 | 305.0 | 325.0 | 335.0 | 335.0 | |
| | | | | | | | | 45 | 1012 | 345.00 | 385.0 | 405.0 | 405.0 | | |

upon the rotational velocity and the viscosity of the lubricant film. Figure 8.4.45 shows the step bearing of a vertical turbogenerator. The load-carrying capacity is

$$
W = \frac{P_o \pi}{2} \frac{R^2 - R_o^2}{\ln (R/R_o)}
$$

This equation is valid even when the recess is eliminated, in which case R_a becomes the radius of the inlet oil supply pipe. The volume flow rate of lubricant and the clearance are related thus:

$$
Q = P_o \pi h_0^3 [6\mu \ln(R/R_o)]
$$

The friction power loss in the bearing is

$$
H_f = \frac{\pi \mu \omega^2 (R^4 - R_o^4)}{2h_0}
$$

The pumping power loss in forcing the lubricant through the bearing is $H_p = Q(P_p - P_1)/\eta$, where η is the efficiency of the pump.

EXAMPLE 10. A typical 5,000-kW vertical turbogenerator has a thrust load of about 101,000 lb; outside diameter of bearing, 16 in; diam of recess, 10 in; pump

$$
\text{efficiency, 0.5; speed, 750 r/min. Substituting these values,}
$$
\n
$$
101,000 = \frac{P_o \pi}{2} \left[\frac{8^2 - 5^2}{\ln(8/5)} \right]
$$
\nor

\n
$$
P_o = 774 \, \text{lb/in}^2
$$

In practice, about 825 lb/in² is used on this step bearing to provide some margin of safety. Film thickness in the bearing should be from 0.001 to 0.01 in to protect the surfaces from metal-to-metal contact and allow passage of harmful grit that may

Fig. 8.4.45 Step bearing of a vertical turbogenerator.

find its way into the system. The film thickness determines the oil flow for a given viscosity and pressure. With $h_0 = 0.006$ in (0.1524 mm) and SAE 20 oil at 130°F (29 centipoises), $Q = 8.25 \times \pi \times (0.006)^3/6 \times 29 \times 1.45 \times 10^{-7} \times 0.470 =$ 46.8 in³/s (766.91 cm³/s). Flow = $46.8 \times 60/231 = 12.15$ gal/min (45.99 *L*/min). The horsepower lost due to friction, $H_f = 750^2 \times 29 \times 1.45(8^4 - 5^4)/383{,}000 \times$ $0.006 = 3.58$ hp (2.669 kW). The horsepower lost due to pumping with pump efficiency of 0.5, $H_p = 46.8 \times 825/6{,}600 \times 0.5 = 11.7$ hp (8.725 kW). The total energy lost = $11.7 + 3.58 = 15.28$ hp (11.39 kW).

Evaluation of these equations for other film thicknesses will show that the minimum lost energy will occur between $h_0 = 0.004$ and $h_0 =$ 0.006 in (0.1016 and 0.1524 mm). The coefficient of friction corresponding to an energy loss of 15.28 hp in the above example is 0.002.

Other configurations for hydrostatically lubricated thrust bearings are shown i[n Fig. 8.4.46 f](#page-127-0)rom Loeb. They may be used directly to obtain the value of load-carrying capacity *W* and flow rate *Q*.

LINEAR SLIDING BEARINGS

All sliding bearings [\(Fig. 8.4.47\)](#page-127-0), to wear true, must have the sliding parts of nearly equal lengths. Bearings made in this way will be found not to wear out of true. Oiling is accomplished in several ways, an acceptable method being that shown i[n Fig. 8.4.48.](#page-127-0) Short slides in many machine tools are lubricated by oil pads or direct oil application. The weight of the table and work and thrust of the tool cause wear on the bottom and sides of the guides. To compensate for the wear in both directions, bearings are sometimes made V-shaped, as shown i[n Fig.](#page-127-0) [8.4.49.](#page-127-0)

Simpler sliding bearings in machine tools are made with provision for adjustment (as shown in [Fig. 8.4.50\)](#page-127-0) of which there are many modifications. Recent applications involving hydrostatic lubrication on machine-tool ways have been very successful.

GAS-LUBRICATED BEARINGS

The fluid-film calculations included in Examples 1 through 10 have assumed that oil (or, in one case, water) was the lubricant. Actually, almost any **process fluid** may be used if proper recognition is given to the viscosity, corrosive action, change in state (where a liquid is close to its boiling point), toxicity, and in the case of a gas, its compressibility. Fluid-film journal and thrust bearings have run successfully, for example, on water, kerosene, gasoline, acid, liquid refrigerants, mercury, molten metals, and a wide variety of gases.

The previous equations for load-carrying capacity, film thickness, friction, and flow may be used for process liquids, but for gases, proper recognition must be made of the compressibility effects.

Because of the great value of gas-lubricated bearings for special applications, and to demonstrate the methods for handling the compressibility action, an introduction to the **design** of **gas-lubricated bearings** follows.

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Fig. 8.4.46 Load-carrying capacity and flow for several flat thrust bearings *(Loeb).* Lengths in inches.

Naturally, if the change in pressure within the bearing clearance is small compared to ambient pressure, the compressibility effect will be likewise small, and lubrication equations based on liquids may be used. A **compressibility parameter** Λ indicates the extent of this action. For hydrodynamic journal bearings it has the form $\Lambda = 6\mu \omega/(P_a m^2)$. For

Fig. 8.4.47

Fig. 8.4.48

Fig. 8.4.49

values of Λ less than one, the previous equations of this section for journal bearings may be used. For values of Λ greater than one, compressibility effects are included through the use of [Figs. 8.4.51](#page-128-0) to 8.4.54. (Data from Elrod and Burgdorfer, Proceedings First International Symposium on Gas-lubricated Bearings, 1959, and Raimondi, *Trans. ASLE,* vol. IV, 1961.)

Fig. 8.4.50

EXAMPLE 11. Determine the minimum film thickness for a journal bearing 0.5 in (1.27 cm) diameter by 0.5 in long. Ambient pressure 14.7 lb/in2 abs (101.34 kN/m2 abs). Speed 12,000 r/min. Load 0.4 lb (0.88 kg). Diametral clearance 0.0005 in (0.0127 mm). Lubricant, air at 100°F and 14.7 lb/in² abs (2.68 \times 10^{-9} lb·s/in² from [Fig. 8.4.55\)](#page-128-0). $m = 0.0005/0.5 = 0.001$ in/in. $\omega = 12,000 \times$ $2\pi/60 = 1,256$ rad/s, $\Lambda = (6 \times 2.68 \times 10^{-9} \times 1,256)/14.7 \times 0.001^2 = 1.37$, and $W((dIP_a) = 0.4/0.5 \times 0.5 \times 14.7 = 0.109$. Then, in [Fig. 8.4.53](#page-128-0) (*l*/*d* = 1), we find that $\varepsilon = 0.22$, and the minimum film thickness $h_0 = 0.00025(1 - 0.22) =$ 0.000195 in (0.00495 mm).

Gas-lubricated journal bearings should be checked for **whirl stability.** [Figure 8.4.56 i](#page-129-0)s applicable with sufficient accuracy to bearings where *l*/*d* is equal to or greater than one. It is used in conjunction with [Fig.](#page-128-0) [8.4.51](#page-128-0) for $\ell/d = \infty$. The stability parameter is ω^* which, for a bearing having only gravity loading, has the value $\omega_1^* = \omega \sqrt{mr/g}$.

EXAMPLE 12. To determine whether the bearing of Example 11 is stable at the running speed of 12,000 r/min, we compute ω_1^* as $1,256\sqrt{0.00025/386}$ = 1.015. The value of eccentricity ratio ε_0 for $l/d = \infty$ is computed from [Fig. 8.4.51](#page-128-0)

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Fig. 8.4.53 Fig. 8.4.54

Figs. 8.4.51–8.4.54 Theoretical load-carrying parameter vs. compressibility parameter for a full journal bearing: $l/d = \infty$. (Fig. 8.4.51), $l/d = 2$ (Fig. 8.4.52), $l/d = 1$ (Fig. 8.4.53), and $l/d = 0.5$ (Fig. 8.4.54). *(Elrod and Raimondi.)*

on the basis of *W* being the load per inch of bearing length. Thus $W(lb/in) =$ $0.4/0.5 = 0.8$ lb/in. For Fig. 8.4.51, $W(dIP_a) = 0.218$ and in Fig. 8.4.51, we determine $\varepsilon_0 = 0.18$. Then (in [Fig. 8.4.56\)](#page-129-0), for $\omega_1^* = 1.015$ and $\Lambda = 1.37$, we find the intersection at about where a curve for $\varepsilon_0 = 0.18$ would be found. The bearing should just be stable. An intersection point on the ε_0 line or to the left should represent a stable condition. An intersection point to the right of the appropriate ε_0 line would predict an unstable condition.

The plain cylindrical journal bearing (360°) is the least stable of possible bearing designs. Control of ''half-frequency'' whirl has been achieved and the threshold of instability has been raised through modification of the geometry of the plain bearing. The simplest modification is the insertion of axial grooves. Bearings with three or four such grooves have been successful, but lose much stiffness.

A typical three-groove (three-sector) bearing is shown i[n Fig. 8.4.57.](#page-129-0) Half-frequency whirl indicates a dynamic instability in which the journal orbits at approximately one-half of the shaft rotational speed, which coincides with the average speed of the lubricant in the film. If one looked at the bearing geometry from a coordinate system rotating at this whirl speed, one would see the journal attempting to pump lubricant

Fig. 8.4.55 Absolute viscosity of air. *(Iwaski, Sci. Rpts., Research Inst., Tohuku Univ., Ser. A; Kestin and Pliarczyk, Trans. ASME, 56, 1954.)* Reyns = 1.45×10^{-7} cP.

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in one direction and the bearing attempting to do the opposite. The capacity of the film to sustain any load is thus greatly diminished, and failure often occurs. Half-frequency whirl can occur when the dynamic system in which the bearing operates has a natural frequency at approximately one-half the speed of rotation. If the energy dissipation rate is

Fig. 8.4.56 Half-frequency translatory whirl threshold for infinite length, 360° journal bearing. *(Castelli and Elrod, Solution for the Stability Problem for 360°, Self Acting Gas Lubricated Bearings, Trans. ASME, 87, Mar. 1965.)*

not sufficiently large, instability occurs. In the dynamic system mentioned above, the stiffness and damping characteristics of the bearing, or bearings, play a major role. Damping arises from squeezing the lubricant in and out of the bearing by the action of the journal vibrations

> against the viscous resistance. When the journal moves, gas can compress and act as a capacitance rather than flow and act as a damper. Therefore, gas bearings are much more prone to instability than are liquid-lubricated ones.

> Aside from avoiding resonance conditions, two often successful techniques for whirl prevention are shown in Figs. 8.4.58 and 8.4.59. The first depicts a complete journal bearing with a rotating geometric artifact causing a synchronous disturbance. This artifact can be a variation in the clearance or an asymmetric mass leading to dynamic unbalance. The

Fig. 8.4.57 Sector sleeve bearing.

second depicts a bearing geometry with shallow, inward-pumping spiral grooves. The depth of the grooves is approximately twice the radial clearance, their angle is from 25° to 30° to the axis, the land-to-groove ratio is 0.5, and the axial extent of the grooved area is one-half the length of the bearing. The grooves can be on either the stator or the rotor, depending on manufacturing convenience. Etching is a common method for production of the grooves. Design data for this excellent type of self-acting gas bearing can be found in Sec. 4 of Gross's book. (See References.)

The tilting-pad journal bearing i[n Fig. 8.4.60](#page-130-0) is considered to be one of the most stable of all possible designs. The shoes, or pads, are supported on rounded pins and are free to pitch and roll through very small angles. Analysis shows that this freedom to move achieves the stability characteristics of these bearings, and also, of course, permits them to be self-aligning. Three-, four-, and five-shoe configurations are often used. [Figure 8.4.60](#page-130-0) shows an early design used for machine tool grinding spindles.

When applied to gas lubrication, pressurized gas may be supplied

through a drilled pivot (hydrostatic lubrication), as an aid in starting and to provide a reserve of load-carrying capacity [\(Fig. 8.4.61\)](#page-130-0). See Gunter, Hinkle, and Fuller, Design Guide for Gas-Lubricated, Tilting-Pad Journal and Thrust Bearings, NYO-2512-1, U.S. AEC, I-A 2392-3-1, Nov. 1964, Contract AT 30-1-2512.

Fig. 8.4.58 Stabilizing rotating geometry. (Clearance greatly exaggerated.)

Fig. 8.4.59 Spiral groove bearing shown as outward-pumping. (Clearance is greatly exaggerated.)

A bearing design development that is simple, inexpensive, and very stable is the foil bearing. It is also very tolerant of thermal distortions and possible loss of clearance resulting from elevated temperatures. Probably the most widely used of several designs is shown in [Fig.](#page-130-0) [8.4.62.](#page-130-0) It consists of overlapping metal shims, anchored at the base end like a cantilever beam. The ''free'' ends deflect and are able to automatically form their own operating clearance. These bearings are widely used in aircraft cabin cooling and for auxiliary power supply systems (Suriano, Dayton, and Woessner, Test Experience with Turbine-end Foil Bearing Equipped Gas Turbine Engines, ASME Paper 83-GT-73, 1983).

Thrust bearings of the tilting-pad variety are less susceptible to compressibility effects and may be considered as liquid-lubricated for values of Λ (suitable for thrust bearings) less than about 30. Λ = $6u\mu l/(h_0^2 P_a)$ where *l* is the length of the shoe in the direction of sliding and *U* is the linear velocity at the mean radius. However, the shoes

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Fig. 8.4.60 Filmatic bearing. *(Courtesy Cincinnati Milacron Corp.)*

should not be made flat for gas operation but should have a crowned contour (see Fig. 8.4.63). (Gross, ''Gas Film Lubrication,'' Wiley.) An approximate value for the crown is to make $\delta = \frac{3}{4}h_0$. The tilting-pad bearing design is probably the most common gas bearing presently in existence. Every hard-disk computer memory since the early 1960s has had its read-write heads supported by self-acting tilting-pad sliders. Hundreds of millions of such units, called *flying heads,* have been manufactured to date. Some designs employ the crown geometry while,

Fig. 8.4.61 Cross-sectional view, spring-mounted pivot assembly. *(Courtesy of The Franklin Institute Research Labs.)*

most commonly, heads with flat multiple sliders with straight ramps in their forward sections are used. The reason for the multiple thin sliders is the achievement of maximum damping possible. The typical minimum film heights have decreased steadily through the years from 1 μ m

Fig. 8.4.62 Bending-dominated segments foil bearing.

(40 millionths of an inch) 25 years ago to less than $0.2 \mu m$ (8 millionths of an inch) currently (1995). This trend is driven by the achievement of the higher and higher recording densities possible at lower flying heights. Design of these devices is done rather precisely from first principles by means of special simulation programs. At these low clearances, allowance must be made for the finiteness of the **molecular mean free path,** which represents the mean distance that a gas molecule must travel between collisions. This effect manifests itself in a lowering of viscosity and wall shear resistance.

Fig. 8.4.63 Schematic of tilting-pad shoe, showing crown height δ .

Gas-lubricated hydrostatic bearings, unlike liquid-lubricated bearings, cannot be designed on the basis of fixed flow rate. They are designed instead to have a pressure loss produced by an **orifice restrictor** in the supply line. Such throttling enables the bearing to have load-carrying capacity and stiffness. For maximum stiffness the pressure drop in the orifice may be about one-half of the manifold supply pressure. For a circular thrust bearing with a single circular orifice, the load-carrying capacity is given with sufficient accuracy by the equation previously used for liquids (se[e Fig. 8.4.44\)](#page-125-0). $W = (P_R - P_a/2)[R^2 - R_0^2/\ln(R/R_0)],$ where P_R is the recess pressure, lb/in² abs. The flow volume, however, is given by $Q_0 = \pi h_0^3 / [6\mu \ln (R/R_0)](P_0^2 - P_1^2)/2P_0$. Q_0 and P_0 refer to recess conditions, and Q_1 and P_1 refer to ambient conditions. Pressures are absolute.

EXAMPLE 13. A circular thrust bearing 6 in (15.24 cm) diameter with a recess 2 in (5.08 cm) diameter has a film thickness of $h_0 = 0.0015$ in (0.0381 mm). $P_0 =$ 30 lb/in² gage or 44.7 lb/in² abs (308.16 kN/m²). P_1 is room pressure, 14.7 lb/in² abs (101.34 kN/m² abs). Depth of recess is 0.02 in. Applied load is 375 lb. Q_0 = $(\pi \times 0.0015^3)/(6 \times 2.68 \times 10^{-9} \ln 3)(44.7^2 - 14.7^2)/(2 \times 44.7), Q_0 = 12.3 \text{ in}^3/\text{s}$ (201.6 cm³/s) at recess pressure. Converted to free air, $Q_1 = Q_0(P_0/P_1)$ with isothermal expansion, $Q_1 = 12.3(44.7/14.7) = 37.4$ in³/s (612.87 cm³/s), or Q_1 $37.4 \times 60 = 2,244$ in³/min (36.77 L/min). Actual measured flow = 2,440 in³/min (39.98 L/min).

Externally pressurized gas bearings are not as easily designed as liquid-lubricated ones. Whenever a volume larger than approximately that of the film is present between the restrictor and the film, a phenomenon known as **air hammer** or **pneumatic instability** can take place. Therefore, in practical terms, recesses cannot be used and orifice restrictors must be obtained by the smallest flow cross-section at the very entrance to the film; this area is equal to the perimeter of the inlet holes multiplied by the local height of the film. This technique is called **inherent compensation.** Unfortunately, as one can readily see, the area of the restrictors is smaller where the film is smaller; thus, the stiffness is lower than that obtainable by incompressible lubrication. Design data are available in Sec. 5 of Gross's book (see References).

8.5 BEARINGS WITH ROLLING CONTACT by Michael W. Washo

REFERENCES: Anti-Friction Bearing Manufacturers Association, Inc. (AFBMA), Method of Evaluating Load Ratings. American National Standards Institute (ANSI), Load Ratings for Ball and Roller Bearings. AFBMA, ''Mounting Ball and Roller Bearings.'' Tedric A. Harris, ''Rolling Bearing Analysis.''

COMPONENTS AND SPECIFICATIONS

Rolling-contact bearings are designed to support and locate rotating shafts or parts in machines. They transfer loads between rotating and stationary members and permit relatively free rotation with a minimum of friction. They consist of **rolling elements (balls or rollers)** between an **outer** and **inner ring. Cages** are used to space the rolling elements from each other. Figure 8.5.1 illustrates the common terminology used in describing rolling-contact bearings.

Fig. 8.5.1 Radial contact bearing terminology.

Rings The inner and outer rings of a rolling-contact bearing are normally made of SAE 52100 steel, hardened to Rockwell C 60 to 67. The rolling-element raceways are accurately ground in the rings to a very fine finish (16 μ in or less).

Rings are available for special purposes in such materials as stainless steel, ceramics, and plastic. These materials are used in applications where corrosion is a problem.

Rolling Elements Normally the rolling elements, balls or rollers, are made of the same material and finished like the rings. Other rolling-element materials, such as stainless steel, ceramics, Monel, and plastics, are used in conjunction with various ring materials where corrosion is a factor.

Cages Cages, sometimes called separators or retainers, are used to space the rolling elements from each other. Cages are furnished in a wide variety of materials and construction. Pressed-steel cages, riveted or clinched and filled nylon, are most common. Solid machined cages are used where greater strength or higher speeds are required. They are fabricated from bronze or phenolic-type materials. At high speeds, the phenolic type operates more quietly with a minimum amount of friction. Bearings without cages are referred to as full-complement.

A wide variety of rolling-contact bearings are normally manufactured to standard boundary dimensions (bore, outside diameter, width) and tolerances which have been standardized by the AFBMA. All bearing manufacturers conform to these standards, thereby permitting interchangeability. ANSI has for the most part adopted these and published them jointly as AFBMA/ANSI standards as follows:

The Annular Bearing Engineers Committee (ABEC) of the AFBMA has established progressive levels of precision for ball bearings. Designated as ABEC-1, ABEC-5, ABEC-7, and ABEC-9, these standards specify tolerances for bore, outside diameter, width, and radial runout. Similarly, roller bearings have established precision levels as RBEC-1 and RBEC-5.

PRINCIPAL STANDARD BEARING TYPES

The selection of the type of rolling-contact bearing depends upon many considerations, as evidenced by the numerous types available. Furthermore, each basic type of bearing is furnished in several **standard ''series''** as illustrated in Fig. 8.5.2. Although the bore is the same, the outside diameter, width, and ball size are progressively larger. The result is that a wide range of load-carrying capacity is available for a given size shaft, thus giving designers considerable flexibility in selecting standard-size interchangeable bearings. Some of the more common bearings are illustrated below and their characteristics described briefly.

Fig. 8.5.2 Bearing standard series.

Ball Bearings

Single-Row Radial [\(Fig. 8.5.3](#page-132-0)) This bearing is often referred to as the **deep groove** or conrad bearing. Available in many variations single or double shields or seals. Normally used for radial and thrust loads (maximum two-thirds of radial).

Maximum Capacity [\(Fig. 8.5.4](#page-132-0)) The geometry is similar to that of a deep-groove bearing except for a **filling slot.** This slot allows more balls in the complement and thus will carry heavier radial loads. However, because of the filling slot, the thrust capacity in both directions is reduced drastically.

Double-Row [\(Fig. 8.5.5\)](#page-132-0) This bearing provides for heavy radial and light thrust loads without increasing the OD of the bearing. It is approximately 60 to 80 percent wider than a comparable single-row bearing. Because of the filling slot, thrust loads must be light.

Internal Self-Aligning Double-Row [\(Fig. 8.5.6\)](#page-132-0) This bearing may be used for primarily radial loads where **self-alignment** $(\pm 4^{\circ})$ is required. The self-aligning feature should not be abused, as excessive misalignment or thrust load (10 percent of radial) causes early failure.

Angular-Contact Bearings [\(Fig. 8.5.7](#page-132-0)) These bearings are designed to support **combined radial and thrust** loads or heavy thrust loads depending on the contact-angle magnitude. Bearings having large contact angles can support heavier thrust loads. They may be mounted in pairs [\(Fig. 8.5.8](#page-132-0)) which are referred to as **duplex bearings:** back-toback, tandem, or face-to-face. These bearings (ABEC-7 or ABEC-9) may be preloaded to minimize axial movement and deflection of the shaft.

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ROLLING-CONTACT BEARINGS' LIFE, LOAD, AND SPEED RELATIONSHIPS 8-133

Ball Bushings (Fig. 8.5.9) This type of bearing is used for linear motions on hardened shafts (Rockwell C 58 to 64). Some types can be used for linear and rotary motion.

Split-Type Ball Bearing (Fig. 8.5.10) This type of ball or roller bearing has split inner ring, outer ring, and cage. They are assembled by screws. This feature is expensive but useful where it is difficult to install or remove a solid bearing.

Roller Bearings

Cylindrical Roller (Fig. 8.5.11) These bearings utilize cylinders with approximate length/diameter ratio ranging from 1:1 to 1:3 as rolling elements. Normally used for heavy radial loads. Especially useful for free axial movement of the shaft. Highest speed limits for roller bearings.

Needle Bearings (Fig. 8.5.12) These bearings have rollers whose length is at least 4 times their diameter. They are most useful where space is a factor and are available with or without inner race. If shaft is used as inner race, it must be hardened and ground. Full-complement type is used for high loads, oscillating, or slow speeds. Cage type should be used for rotational motion. They cannot support thrust loads.

Tapered-Roller (Fig. 8.5.13) These bearings are used for heavy radial and thrust loads. The bearing is designed so that all elements in the rolling surface and the raceways intersect at a common point on the axis: thus **true rolling** is obtained. Where maximum system rigidity is required, the bearings can be adjusted for a preload. They are available in double row.

Spherical-Roller (Fig. 8.5.14) These bearings are excellent for heavy radial loads and moderate thrust. Their internal self-aligning feature is useful in many applications such as HVAC fans.

Thrust Bearings

Ball Thrust Bearing (Fig. 8.5.15) It may be used for low-speed applications where other bearings carry the radial load. These bearings are made with shields, as well as the open type.

Straight-Roller Thrust Bearing (Fig. 8.5.16) These bearings are made of a series of short rollers to minimize the skidding, which causes twisting, of the rollers. They may be used for moderate speeds and loads.

Tapered-Roller Thrust (Fig. 8.5.17) It eliminates the skidding that takes place with straight rollers but causes a thrust load between the ends of the rollers and the shoulder on the race. Thus speeds are limited because the roller end and race flange are in sliding contact.

Selection of Ball or Roller Bearing

Selection of the type of rolling-element bearing is a function of many factors, such as load, speed, misalignment sensitivity, space limitations, and desire for precise shaft positioning. However, to determine if a ball or roller bearing should be selected, the following **general rules** apply:

1. Ball bearings function on theoretical point contact. Thus they are suited for higher speeds and lighter loads than roller bearings.

2. Roller bearings are generally more expensive except in larger sizes. Since they function theoretically on line contact, they will carry heavy loads, including shock, more satisfactorily, but are limited in speed.

Us[e Fig. 8.5.18](#page-133-0) as a general guide to determine if a ball or roller bearing should be selected. This figure is based on a rated life of 30,000 h.

ROLLING-CONTACT BEARINGS' LIFE, LOAD, AND SPEED RELATIONSHIPS

An accurate knowledge of the load-carrying capacity and expected life is essential in the proper selection of ball and roller bearings. Bearings that are subject to millions of different stress applications fail owing to

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Fig. 8.5.18 Guide to selection of ball or roller bearings.

fatigue. In fact, **fatigue** is the only cause of **failure** if the bearing is properly lubricated, mounted, and sealed against the entrance of dust or dirt and is maintained in this condition. For this reason, the **life** of an individual bearing is defined as the total number of revolutions or hours at a given constant speed at which a bearing runs before the first evidence of fatigue develops.

Definitions

Rated Life L_{10} The number of revolutions or hours at a given constant speed that 90 percent of an apparently identical group of bearings will complete or exceed before the first evidence of fatigue develops; i.e., 10 out of 100 bearings will fail before rated life. The names **Minimum life** and L_{10} **life** are also used to mean rated life.

Basic Load Rating *C* The radial load that a ball bearing can withstand for one million revolutions of the inner ring. Its value depends on bearing type, bearing geometry, accuracy of fabrication, and bearing material. The basic load rating is also called the **specific dynamic capacity,** the **basic dynamic capacity,** or the **dynamic load rating**.

Equivalent Radial Load *P* Constant stationary radial load which, if applied to a bearing with rotating inner ring and stationary outer ring, would give the same life as that which the bearing will attain under the actual conditions of load and rotation.

Static Load Rating C_0 Static radial load which produces a maximum contact stress of 580,000 lb/in2 (4,000 MPa).

Static Equivalent Load *P***⁰** Static radial load, if applied, which produces a maximum contact stress equal in magnitude to the maximum contact stress in the actual condition of loading.

Bearing Rated Life

Standard formulas have been developed to predict the statistical rated life of a bearing under any given set of conditions. These formulas are based on an exponential relationship of load to life which has been

established from extensive research and testing.
\n
$$
L_{10} = \left(\frac{C}{P}\right)^K \times 10^6
$$
\n(8.5.1)

where L_{10} = rated life, r; $C =$ basic load rating, lb; $P =$ equivalent radial load, lb; $K =$ constant, 3 for ball bearings, 10/3 for roller bearings.

To convert to hours of life
$$
L_{10}
$$
, this formula becomes
\n
$$
L_{10} = \frac{16,700}{N} \left(\frac{C}{P}\right)^K
$$
\n(8.5.2)

where $N =$ rotational speed, r/min. Table 8.5.1 lists some common design lives vs. the type of application. These may be altered to suit unusual circumstances.

Load Rating

The **load rating** is a function of many parameters, such as number of balls, ball diameter, and contact angle. Two load ratings are associated with a rolling-contact bearing: **basic** and **static** load rating.

Basic Load Rating *C* This rating is *always* used in determining bearing life for all speeds and load conditions [see Eqs. (8.5.1) and (8.5.2)].

Static Load Rating C_0 This rating is used only as a check to determine if the maximum allowable stress of the rolling elements will be exceeded. It is *never* used to calculate bearing life.

Values for C and C_0 are readily attainable in any bearing manufacturer's catalog as a function of size and bearing type[. Table 8.5.2](#page-134-0) lists the basic and static load ratings for some common sizes and types of bearings.

Equivalent Load

There are two **equivalent-load** formulas. Bearings operating with some finite speed use the equivalent radial load *P* in conjunction with *C* [Eq. (8.5.1)] to calculate bearing life. The static equivalent load is used in comparison with C_0 in applications when a bearing is highly loaded in a static mode.

Equivalent Radial Load *P* All bearing loads are converted to an equivalent radial load. Equation (8.5.3) is the general formula used for both ball and roller bearings.

$$
P = XR +YT \tag{8.5.3}
$$

where $P =$ equivalent radial loads, lb; $R =$ radial load, lb; $T =$ thrust (axial) load, lb; *X* and *Y* = radial and thrust factors [\(Table 8.5.3\).](#page-134-0) The empirical *X* and *Y* factors in Eq. (8.5.3) depend upon the geometry, loads, and bearing type. Average *X* and *Y* factors can be obtained from [Table 8.5.3](#page-134-0). Two values of *X* and *Y* are listed. The set X_1 Y_1 or X_2 Y_2 giving the largest equivalent load should always be used.

Static Equivalent Load P_0 The static equivalent load may be compared directly to the static load rating C_0 . If P_0 is greater than the C_0

rating, permanent deformation of the rolling element will occur. Calculate P_0 as follows:

$$
P_0 = X_0 R = Y_0 T \tag{8.5.4}
$$

where P_0 = static equivalent load, lb; X_0 = radial factor (see Table 8.5.4); Y_0 = thrust factor (see Table 8.5.4); R = radial load, lb; T = thrust (axial) load, lb. If a load higher than the basic static load rating is

Table 8.5.3 Radial and Thrust Factors

| Bearing type | X, | | Χ, | Υ, |
|--------------------|-----|------|------|------|
| Single-row ball | 1.0 | 0.0 | 0.56 | 1.40 |
| Double-row ball | 1.0 | 0.75 | 0.63 | 1.25 |
| Cylindrical roller | 1.0 | 0.0 | 1.0 | 0.0 |
| Spherical roller | 1.0 | 2.5 | 0.67 | 3.7 |

imposed while rotating, the deformation is distributed evenly and no practical impairment occurs until the deformation becomes quite large. Some equipment operates with loads greatly exceeding the static capacity, such as bearings supporting artillery (twice static capacity), or aircraft control pulleys (four times static capacity). The load which will fracture a bearing is approximately eight times the static load rating.

Oscillating loads, where the motion is such that the rolling element rotates less than half a revolution, approach static load conditions. This type of load is conducive to rapid **false brinelling** and requires special lubrication techniques.

Required Capacity

The basic load rating *C* is very useful in the selection of the type and size of bearing. By calculating the required capacity needed for a bearing in a certain application and comparing this with known capacities, a bearing can be selected. To calculate the required capacity, the following formula can be used:

$$
C_r = \frac{P(L_{10}N)^{1/K}}{Z}
$$
 (8.5.5)

where $C =$ required capacity, lb; $L_{10} =$ rated life, h; $P =$ equivalent radial load, lb; $K =$ constant, 3 for ball bearings, 10/3 for roller bearings; $Z =$ constant, 25.6 for ball bearings, 18.5 for roller bearings; $N =$ rotation speed, r/min.

LIFE ADJUSTMENT FACTORS

Modifications to Eq. (8.5.2) can be made, based on a better understanding of causes of fatigue. Influencing factors include

1. Reliability factors for survival rates greater than 90 percent

2. Improved raw materials and manufacturing processes for ball bearing rings and balls.

3. The beneficial effects of elastrohydrodynamic lubricant films

Equation (8.5.2) can be rewritten to reflect these influencing factors:
\n
$$
L_{10} \text{ modified} = A_1 A_2 A_3 \frac{16,700}{N} \left(\frac{C}{P}\right)^K \qquad (8.5.6)
$$

where A_1 = statistical life reliability factor for a chosen survival rate, A_2 = life-modifying factor reflecting bearing material type and condition, and A_3 = elastohydrodynamic lubricant film factor.

Factor A_1

Reliability factors listed i[n Table 8.5.5](#page-135-0) represent rates from 90 to 99 percent. Using rates other than 90 percent will yield larger bearings for equivalent loads and, therefore, will increase costs. Rates higher than 90 percent should be used only when absolutely necessary.

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Table 8.5.5 Reliability Factor *A***¹ for Various Survival Rates**

| Survival rate, % | Bearing life notation | Reliability factor A_1 |
|------------------|--------------------------|-----------------------------|
| 90 | L_{10} | 1.00 |
| 95 | L_{5} | 0.62 |
| 96 | L_{4} | 0.53 |
| 97 | L_3 | 0.44 |
| 98 | L_{2} | 0.33 |
| 99 | L, | 0.21 |

Factor A_2

While not formally recognized by AFBMA, estimated A_2 factors are commonly used as represented by the values in Table 8.5.6. The main considerations in establishing A_2 values are the material type, melting procedure, mechanical working and grain orientation, and hardness.

Factor A_3

This factor is based on elastohydrodynamic lubricant film calculations which relate film thickness and surface finish to fatigue life. A factor of 1 to 3 indicates adequate lubrication, with 1 being the minimum value for which the fatigue formula can still be applied. As A_3 goes from 1 to 3, the life expectancy will increase proportionately, with 3 being the largest value for A_3 that is meaningful. If A_3 is less than 1, poor lubrication conditions are presumed. Calculations for A_3 are beyond the scope of this section.

Speed Limits

Many factors combine to determine the limiting speeds of ball and roller bearings. It depends on several factors, like bearing size, inner- or outer-ring rotation, contacting seals, radial clearance and tolerances, operating loads, type of cage and cage material, temperature, and type of lubrication. A convenient check on speed limits can be made from a *dn* value. The *dn* value is a direct function of size and speed and is dependent on type of lubrication. It is calculated by multiplying the bore in millimeters (mm) by the speed in r/min.

$$
dn = \text{bore (mm)} \times \text{speed (r/min)} \tag{8.5.7}
$$

A guide for *dn* values is listed in Table 8.5.7. When these values are exceeded, bearing life is shortened. The values are only a guide for approaching difficulties and can be exceeded by special bearings, lubrication, and application.

Table 8.5.7 *dn* **Values vs. Bearing Types**

Friction

One of the assets of rolling-contact bearings is their low friction. The **coefficient of friction** varies appreciably with the type of bearing, load, speed, lubrication, and sealing element. For rough calculations the following coefficients can be used for normal operating conditions and favorable lubrication:

Excess grease, contact seals, etc., will increase these values, and allowances should be made.

PROCEDURE FOR DETERMINING SIZE, LIFE, AND BEARING TYPE

Basically, three common situations may be encountered in the analysis of a bearing system; bearing-size selection, bearing-type selection, and bearing-life determination. Each of these problems requires the following conditions to be known; radial load, thrust load, and speed. The static load capacity is not considered in the following procedures but should be analyzed if the bearing rotational speed is slow or if the bearing is idle for a period of time.

Bearing Size Selection

Known type and series:

- 1. Select desired design life [\(Table 8.5.1\)](#page-133-0).
- 2. Calculate equivalent radial load *P* [Eq. (8.5.3)].
- 3. Calculate required capacity C_r [Eq. (8.5.5)].
- 4. Compare *Cr* with capacities *C* i[n Table 8.5.2.](#page-134-0) Select first bore size having a capacity *C* greater than *Cr*.
	- 5. Check bearing speed limit [Eq. (8.5.7)].

Bearing-Type Selection

Known bore size and life:

1. Select ball or roller bearing [\(Fig. 8.5.18\)](#page-133-0).

2. Calculate equivalent load *P* [Eq. (8.5.3)] for various bearing types (conrad, spherical, etc.).

3. Calculate *Cr* [(Eq. (8.5.5)].

4. Compare C_r with capacities C i[n Table 8.5.3,](#page-134-0) and select the type that has a capacity equal to or greater than C_r .

5. Check bearing speed limit [Eq. (8.5.7)].

Bearing-Life Determination

Known bearing size:

- 1. Select ball or roller bearing [\(Fig. 8.5.18\)](#page-133-0).
- 2. Calculate equivalent radial load *P* [Eq. (8.5.3)].
- 3. Select basic load rating *C* fro[m Table 8.5.3.](#page-134-0)
- 4. Calculate rated life *L*¹⁰ [Eq. (8.5.1) or (8.5.2)].
- 5. Check calculated life with design life.

BEARING CLOSURES

Rolling-element bearings are made with a wide variety of **closures**. Basically, they are open, shielded, or sealed (Figs. 8.5.19 and 8.5.20). **Shielded bearings** have a small clearance between the stationary shield and rotating ring. This provides reasonable exclusion of dirt without an

Fig. 8.5.19 Fig. 8.5.20

increase in friction. **Sealed bearings** have a flexible lip (usually synthetic rubber) in contact with the inner ring. Friction is increased, but more effective retention of lubricant and exclusion of dirt is obtained. Seals should not be used to seal a fluid head or at high speeds.

BEARING MOUNTING

Correct **mounting** of a rolling-contact bearing is essential to obtain its rated life. Many types of mounting methods are available. The selection of the proper method is a function of the accuracy, speed, load, and cost of the application. The most common and best method of bearing retention is a press fit against a shaft shoulder secured with a locknut. End caps are used to secure the bearing against the housing shoulder (Fig. 8.5.21). Retaining rings are also used to fix a bearing on a shaft or in a housing (Fig. 8.5.22). Each shaft assembly normally must provide for expansion by allowing one end to float. This can be accomplished by

Fig. 8.5.21

Fig. 8.5.22

allowing the bearing to expand linearly in the housing or by using a straight roller bearing on one end. Care must be exercised when designing a **floating installation** because it requires a slip fit. An excessively loose fit will cause the bearing to spin on the shaft or in the housing.

Table 8.5.8 lists shaft and housing tolerances for press fits with ABEC 1 precision applications (pumps, gear reducers, electric motors, etc.) and ABEC 7 precision applications (grinding spindles, etc.).

Table 8.5.8 Shaft and Housing Tolerances for Press Fit

| Bearing bore, mm | Shaft tolerances, in, ABEC 1 precision | Bearing bore, mm | Shaft tolerances, in, ABEC 7 precision |
|---------------------|---|---------------------|---|
| $4 - 6$ | $+0.0000$ -0.0002 | $4 - 30$ | $+0.00000$ -0.00015 |
| $7 - 17$ | $+0.0000$ -0.0003 | $35 - 50$ | $+0.0000$ -0.0002 |
| $20 - 50$ | $+0.0000$ -0.0004 | $55 - 80$ | $+0.0000$ -0.0003 |
| $55 - 80$ | $+0.0000$ -0.0005 | $85 - 120$ | $+0.00000$ -0.00035 |
| $85 - 120$ | $+0.0000$ -0.0006 | | |
| Bearing OD, mm | Housing tolerances, in, ABEC 1 precision | Bearing OD, mm | Housing tolerances, in, ABEC 7 precision |
| $16 - 30$ | $+0.0008$ -0.0000 | $16 - 80$ | $+0.0002$ -0.0000 |
| $32 - 47$ | $+0.0010$ -0.0000 | $85 - 120$ | $+0.0003$ -0.0000 |
| $52 - 80$ | $+0.0012$ -0.0000 | $125 - 225$ | $+0.0004$ -0.0000 |
| $85 - 120$ | $+0.0014$ -0.0000 | | |
| $125 - 180$ | $+0.0016$ -0.0000 | | |

Mounted units such as **ball-bearing pillow blocks** (Fig. 8.5.23) are frequently used for fans and conveyors. Three common methods are used to attach the bearing to the shaft; setscrew, eccentric locking collar, and taper-sleeve adapter.

Fig. 8.5.23

Setscrew Figure 8.5.24 illustrates the use of an extended inner-ring bearing held to the shaft with a setscrew. This is a simple method and is suitable only for lightly loaded bearings.

Fig. 8.5.24 Fig. 8.5.25

Eccentric Locking Collar Figure 8.5.25 illustrates the use of an extended inner-ring bearing held to the shaft with an eccentric collar. This method tends to keep the shaft centered in the bearing more concentrically than the setscrew method. It is suitable for light to moderate loads. **Taper-Sleeve Adapter** Figure 8.5.26 illustrates the use of a taper-

sleeve adapter to mount the bearing on the shaft. It provides uniform concentric contact between the shaft and bearing bore. However, skill is required to tighten the locking nut enough to keep the sleeve from spinning on the shaft and yet not so tight that the inner race of the bearing is expanded to the point where the clearance is removed from the bearing. It is very difficult to obtain the correct setting with light-series bearings. They are excellent for heavy-duty spherical roller bearings.

LUBRICATION

Rolling-contact bearings need a **fluid lubricant** to obtain or exceed their rated life. In the absence of high-temperature environment, only a small amount of lubri-

cant is required for excellent performance. Excess lubricant will cause heating of the bearing and accelerate the deterioration of the lubricant. Optimum lubrication of rolling-contact bearings can be predicted by

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elastohydrodynamic theory (EHD). It has been shown that film thickness is sensitive to bearing speed of operation and lubricant viscosity properties and, moreover, that the film thickness is virtually insensitive to load.

Grease is commonly used for lubrication of rolling-contact bearings because of its convenience and minimum maintenance. A high-quality lithium-based NLGI 2 grease should be used for temperatures up to 180°F (82°C), or polyurea-based grease for temperatures up to 300°F (150°C). In applications involving high speed, oil lubrication is often necessary. Table 8.5.9 can be used as a general guide in selecting oil of the proper viscosity for rolling-contact bearings.

 $*$ ISO identification number = midpoint viscosity in centistokes at 40 $^{\circ}$ C.

Table 8.5.10 Ball-Bearing Grease Relubrication Intervals (Hours of operation)

In applications using grease, it is necessary to replenish the lubricant. Relubrication intervals in hours of operation are dependent on temperature, speed, and bearing size. Table 8.5.10 is a general guide which represents the time after which it is advisable to add a small amount of grease in order to safeguard the bearings. The intervals are valid up to 160°F (71°C) and should be divided by 2 for cylindrical roller bearings and by 10 for spherical roller bearings.

8.6 PACKINGS AND SEALS

by John W. Wood, Jr.

REFERENCES: Staniar, ''Plant Engineering Handbook,'' McGraw-Hill. Thorn, Rubber and Plastic Packings, *Rubber Age,* Jan. 1956. Roberts, Gaskets and Bolted Joints, *Jour. Applied Mechanics,* June 1950. Nonmetallic Gaskets, *Mach. Des.,* Nov. 1954. Elonka, Basic Data on Seals, a *Power* reprint, McGraw-Hill. Fluidtec Engineered Products, Training Manuals.

Packings are materials used to control or stop leakage of fluids (liquids and/or gases) or solid dry products through mechanical clearances when the contained material is under static or dynamic pressure.

Gaskets are compressible materials installed in static clearances which normally exist between parallel flanges or concentric cylinders. Sealing of flat flange gaskets is effected by compressive loading achieved through bolting or other mechanical means. The full face gasket [\(Fig. 8.6.1\)](#page-138-0) is not recommended because the material outside the bolt holes is ineffective. The simple ring gasket [\(Fig. 8.6.2\)](#page-138-0) is more efficient and economical. With irregularly contoured flanges, bolt holes may serve to locate the gasket, in which case they should be placed in lobes with full sealing flange width maintained between the inner edge of the holes and the inside of the gasket. **Metal-to-metal** fits require a recess whose volume is greater than that of the gasket to be used. The gasket, such as an O ring [\(Fig. 8.6.13\)](#page-138-0), either rectangular or round cross section, extends above the groove sufficiently to provide a minimum cross-sectional compression of 15 percent for initial seating. In service, the fluid load automatically provides additional sealing force. **Warped, wavy,** or irregular flanges, often resulting from welding, other fabrication, or as found in glass-lined equipment, require gaskets that are softer or thicker than normal in order to compensate for surface imperfections. Excessive thickness or volume of gasket material, even though the gasket is installed in a groove, must be avoided to prevent distortion or ''mushrooming,'' which will result in inadequate loading. Tongue and groove joints [\(Fig. 8.6.4\)](#page-138-0) confine the gasket material and may adapt to the extra thickness, within limits.

In addition to the types [\(Figs. 8.6.5](#page-138-0) to 8.6.7) shown, as defined in the

table [\(Fig. 8.6.37\)](#page-139-0), there are the machined metal profile gasket [\(Fig.](#page-138-0) [8.6.8\)](#page-138-0) and solid metal designs in flat, round, and either octagonal or oval API ring joint gaskets for extreme pressures and temperatures to seal against steam, oil, and gases. These types have very low compressibilities, and their behavior depends on their cross sections. The envelope gasket [\(Fig. 8.6.3\)](#page-138-0), usually polytetrafluoroethylene with a variety of cores, is particularly useful for extremely corrosive or noncontaminating service under average pressure.

Cylindrical or **concentric** gasketing uses a retaining gland follower and is mechanically loaded, e.g., the standard mechanical joint for cast-iron pipe [\(Fig. 8.6.10\)](#page-138-0) or the condenser tube-sheet ferrule [\(Fig. 8.6.11\)](#page-138-0). Cup-shaped gaskets are designed to be self-tightening under pressure [\(Fig. 8.6.12\)](#page-138-0). The O ring [\(Fig. 8.6.13](#page-138-0)) located in an annular groove and precompressed as in the grooved flange, is a self-energized gasket. A cylindrical ring with internal single lip or double lips, also automatic in action, is quite common in pipe joints.

Beyond these types are many specialty gaskets designed for specific or proprietary use, e.g., a seal for a removable drumhead.

The compressibility of various gasketing materials is shown in [Fig.](#page-138-0) [8.6.37,](#page-139-0) and their common usage is listed in [Table 8.6.1.](#page-139-0) Beyond rubber are many elastomeric materials generally similar in mechanical behavior but varying as to temperature limits and fluid compatibility (see Sec. 6).

The **proper design** of a gasketed joint requires flange rigidity to avoid distortion, surface finish commensurate with gasket type and good sealing pressure, and adequate bolt loading. The load must seat the gasket, i.e., cause the material to flow into and fill flange irregularities. It must seal sufficiently that the residual fluid pressure on the gasket exceeds the pressure of the fluid being contained. These values, known respectively as the *seating load y* in lb/in2 and the *gasket factor m*, vary with gasket material and thickness. The ASME Code for Unfired Pressure Vessels, section VIII, gives sufficient detail for typical joint design and tabulates values for *y* and *m* for various gasketing materials.

Fig. 8.6.1–8.6.36 Packings.

High bolt loading is desirable for tight and enduring gasket joints, but it must not crush the gasket material. Crushing-strength values, which will vary with thickness and temperature, can be obtained from the gasket manufacturers. Consistent with the condition of the flanges, the thinner the gasket, the more efficient the joint.

Data on the design of **O-ring joints** are available from suppliers. The nominal pressure limit for O rings, based on typical mechanical clearances, is 1,500 lb/in² (10 MN/m²) without backup rings and 3,000 lb/in² (20 MN/m2) with backup rings. If clearances can be eliminated, as in a flanged joint with close metal-to-metal contact, no limit can be set. Other self-energizing joints, such as the boiler hand-hole plate (Fig. 8.6.9), need only sufficient load to effect an initial seal.

Valve disks are specialized gaskets designed for joints that are frequently broken and reseated. Disks for globe valves (Fig. 8.6.14) are usually encased in a disk holder with a swivel mounting, which ensures precise reseating without abrasion during the closing and opening cycles. They are made of firm rubber for bib washers, hard rubber and phenolics for more severe service, and plastics such as nylon and polytetrafluoroethylene. Pump valves (Fig. 8.6.15) are described in Sec. 14. Rubber **valve seats** are used with metal valve disks on some pumps, e.g., the rotary drilling pump valve (Fig. 8.6.16). Plastics are also used for seats, notably in ball valves.

Dynamic packings include all packings that operate on moving surfaces. To retain fluid under pressure, they are subjected to the hydraulic

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load. When no pressure exists, as in many oil-seal applications, the packing is mechanically loaded by a sprin[g \(Fig. 8.6.28](#page-138-0)) or by its own resiliency. Dynamic packings operate like bearings, wherein the lubricant serves as both a separating film and a coolant. The film is vital for satisfactory service life, but some leakage will occur. Low-viscosity

Fig. 8.6.37 Compressibility of gaskets. (See Table 8.6.1.)

fluids and high pressures add to leakage problems, as both require thin films to minimize leakage. This causes higher friction and generates heat, which is the single most detrimental factor in packing life. Deep packings reduce leakage but increase frictional heat, particularly at high speeds. Normally the fluid being sealed serves as the lubricant. Maximum efficiency is attained when oil is the fluid being sealed; in decreasing order of efficiency are clean water, solvents, and fluids containing solids. These are progressively more unsatisfactory unless supplemental lubrication is provided. Lubrication may be provided by using a lantern ring in the center of the packing set through which lubricant is fed to the packings [\(Fig. 8.6.27\)](#page-138-0). The preferred method of introducing the lubricant is to supply it at a pressure slightly higher than that of the fluid being sealed, say, 5 to 10 lb/in² (3.5 to 7 kN/m²) higher. The choice of lubricant is governed by the fluid being sealed, since the two should be compatible. In cases of extreme contamination, the lantern ring is moved to the bottom of the packing set to introduce clean lubricant and to prevent abrasives from migrating along the dynamic sealing surface. Use of a lantern ring also seals against air being drawn into the system when equipment is operating at negative head or starts under vacuum. Centrifugal pumps equipped in this manner are said to have a **water seal**.

Dynamic packings are classified in three ways:

1. On the basis of shape of the surfaces: cylindrical, conical, spherical, or flat. Cylindrical packings are in turn classified according to whether they pack on the outside perimeter, as in piston packings [\(Fig.](#page-138-0) [8.6.17](#page-138-0) to 8.6.20) or inside perimeter, as on rods or shafts [\(Figs. 8.6.21](#page-138-0) to 8.6.28). Other examples are: conical, the plug cock lining [\(Fig. 8.6.29\)](#page-138-0); spherical, the ball joint [\(Fig. 8.6.30\)](#page-138-0); and flat, the mechanical seals [\(Figs. 8.6.31](#page-138-0) and 8.6.32).

2. On the basis of the type of motion: rotary, oscillating, reciprocating, or helical (as in a rising-stem valve packing).

3. On the basis of being nonautomatic soft or jamb packings/compression packings (tightened by external means, usually a gland follower); or automatic preformed, molded shapes (self-tightening under pressure).

The **selection of a packing** is a matter of economics. In most cases several types are available, some of which, though expensive in the first place, yield exceptional service. A cheaper packing could yield degraded service. Service requirements often dictate the final choice of a packing material, and they must reflect and balance the fluid being sealed, compatibility between fluid and gasket material, operating pressure in the system, and ease of maintenance and replacement.

For **reciprocating elements,** the **O ring** [\(Fig. 8.6.20](#page-138-0)) is extremely simple. It is a precision part manufactured to close tolerances, as must be the seat into which it is placed. As an elastomeric material completely exposed to the operating fluid, it is subject to chemical degradation. The O-ring material must be carefully chosen to ensure compatibility with the fluid being sealed; the wrong choice will lead to either shrinkage or swelling, with premature failure of the O ring. It is best suited to medium-pressure service from 1,500 to 3,000 lb/in2 (10 to 20 MN/m2) with backup rings and intermittent movement, as in hydraulic cylinder or valve stem service. It is not recommended for pump service. Backup rings are preferably of heavy blocklike cross section in either tetrafluoroethylene or similar material, avoiding the thin spiral type. The split **piston ring** [\(Fig. 8.6.17\)](#page-138-0), usually cast iron, is widely used in gas, oil, and steam engines and compressors. Large pistons frequently employ segmental rings similar to floating metal rod packings [\(Fig. 8.6.24\)](#page-138-0) but facing outward. **Floating metal packing rings** are made of numerous radial or tangential segments, making it possible for them to contract on the shaft; they are assembled in sets of two to break the joints and are held together with garter springs. They are used for steam, gas, or air, in either engines or compressors under the most severe operating conditions and at pressures up to 35,000 lb/in2 (241 MPa). Normally oil lubrication is provided; for less severe service, filled polytetrafluoroethylene (PTFE) rings perform very well in dry gases without auxiliary lubrication. Step-, scarf-, or butt-cut rings of laminated cotton fabric, bonded with an elastomer or phenolic resin, are employed in water pumps, gasoline pumps, etc. They may float similar to cast iron piston rings, or be retained by a gland follower, as in [Fig. 8.6.18.](#page-138-0) **Cups** [\(Fig.](#page-138-0) [8.6.19\)](#page-138-0) are fully automatic and very tight; cups in their inverted form, with the lip on the ID, are known as **flange packings** and are also fully automatic and very tight. They are used principally for slow-speed applications. **Nested V and conical rings** [\(Figs. 8.6.](#page-138-0)22 and 8.6.23) are automatic, though often provided with a gland follower to effect initial fit. They are made of a wide range of materials from homogeneous elastomers and polymers, through reinforced woven fibers (cotton, aramid, or fiberglass) for severe duty. They range in hardness from soft and

* Asbestos bearing material is found generally in older equipment; current, new, and/or replacement parts are compounded of other materials suitable to the service application. Fiberglass is a common substitute for asbestos in these applications.

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flexible to semirigid. Use of multiple rings allows them to be of the cut or split type for ease of installation and replacement. **Soft or jamb packings** are best suited for rod or plunger service, since an adjustable gland followe[r \(Fig. 8.6.21](#page-138-0)) is required. They are normally formed in rectangular section with a butt joint staggered from ring to ring at installation. Many materials are employed, such as braided flax saturated with wax or viscous lubricants for water and aqueous solutions; braided fiberglass similarly treated or often impregnated with PTFE/graphite suspensoid for more severe service; laminated rubberized cotton fabric for hot water, low-pressure steam, and ammonia; rolled rubberized fiberglass or aramid fabric for steam; and rolled or twisted metal foil for high-temperature and high-pressure conditions. Packings containing woven or braided fibers are also made from wire-inserted yarns to gain additional strength. For pipe expansion joints, see Sec. 8.

Rotary shafts are generally packed with adjustable soft packings, with the notable exception of the mechanical seals [\(Figs. 8.6.31](#page-138-0) and 8.6.32); where pressures are low, nested V or conical styles may be used. At zero or negligible pressures, the oil seal, a spring-loaded flange packing [\(Fig.](#page-138-0) [8.6.28\)](#page-138-0), is very widely used. Where some leakage can be tolerated, the labyrinth [\(Fig. 8.6.25\)](#page-138-0) and controlled-gap seals are used, particularly on high-speed equipment such as steam and gas turbines. **Soft packings** are of the same general type as those used for reciprocating service, with the fiber braid lubricated with grease and graphite or with polytetrafluoroethylene fibers and suspensoid. Aramid, carbon, and graphite fibers filled with various lubricants and reinforcements are used at higher speeds and fluid pressures. Fiber braid with PTFE suspensoid is widely applied on valve stems operating below 500°F (260°C) and on centrifugal pumps. This material is an insulator, however, and results in high heat buildup on the dynamic surface; a better choice lies in use of a packing with better heat-transfer characteristics, such as one containing carbon or graphite. For continuous rotary service, **automatic packings** are best restricted to low pressure because their tightness under high pressure results in overheating. For intermittent service, as on valve stems, they are excellent.

Oil seals [\(Fig. 8.6.28\)](#page-138-0) are unique flange packings having an elastomer lip generally bonded to a metal cup which is press-fitted into a smooth cylindrical bore. Basically, an oil seal is a flange packing with a flexible lip and a narrow contact area about $\frac{1}{16}$ in (1.6 mm) wide which, under pressure, causes extreme local heating and wear. They are recommended only for nonpressure service and perform best in good lubricating media. To accommodate shaft runout up to 0.020 in (0.5 mm) depending on the rotating speed, the lip is spring-loaded with a coil spring or a finger spring. Coil springs are safer inasmuch as they are molded into the elastomer and are less likely to become dislodged and cause shaft damage. Since the lip is completely exposed to the sealed fluid, particular care should be taken to ensure compatibility between the elastomer and the fluid. Temperature is another operating condition which must be taken into consideration when one is using oil seals.

Mechanical, Rotary, or End Face Seals

The greatest advancements in the design of end face mechanical seals have come about in response to environmental regulations; requirements to minimize energy consumption and operating costs; safety; and concerns over loss of the product which is being sealed. The application of seals to replace packing in rotary equipment has increased dramatically and continues.

All end face mechanical seals [\(Figs. 8.6.31](#page-138-0) and 8.6.32) consist of four parts: a stationary flat face, a rotating flat face, secondary sealing elements (usually elastomeric), and a flexible loading device. The assembled seal is placed and effects proper leak control. The two flat-face seal rings (one stationary, one rotating) rub and create the primary seal. Normally, the flat seal rings have different hardness values, and the soft one is narrower than the hard one. Secondary sealing elements prevent leakage between the rotating shaft and the rotating seal ring, and they block the leakage path around the outside of the stationary seal face. They also serve as gaskets between the assembled parts (i.e., gland plate and housing). The flexible loading device usually consists of one or more springs which press the flat seal rings together. Spring loading ensures a seal when there is little or no hydraulic pressure available to press the faces together and helps maintain constant pressure between the faces as the soft (sacrificial) face wears down. The springs also act as vibration dampers to mitigate against the intrusion of transmitted vibrations, which may affect the efficient operation of the seal assembly.

Types of End Face Mechanical Seals

1. *Inside-mounted.* The seal head is mounted inside the stuffing box (Fig. 8.6.38*a*).

Fig. 8.6.38 Rotary end face seal. (*a*) Inside the seal chamber/stuffing box; (*b*) outside the seal chamber/stuffing box.

2. *Outside-mounted.* The seal head is mounted outside the stuffing box (Fig. 8.6.38*b*).

3. *Unbalanced seal.* The full hydraulic pressure in the seal chamber is transmitted to the seal faces (Fig. 8.6.39*a*).

Fig. 8.6.39 Rotary end face seals showing (*a*) unbalanced and (*b*) balanced configurations.

4. *Balanced.* The seal elements are designed to reduce the hydraulic forces transmitted to the seal faces (Fig. 8.6.39*b*). A complete balance is not practical.

5. *Rotary seal.* In this design, the springs rotate with the shaft.

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6. *Stationary seal.* In this design, the springs do not rotate with the shaft.

7. *Metal bellows.* Welded or formed metal bellows exert a spring load; there is no dynamic secondary seal element (Fig. 8.6.40).

Fig. 8.6.40 Rotary end face seal with metal bellows and "t" clamp stationary.

8. *Double seal.* Two mechanical seals are mounted back to back, face to face, or in tandem, between which a barrier fluid (liquid or gas) can be introduced for environmental control (Fig. 8.6.41).

Fig. 8.6.41 Back-to-back double seal. Barrier fluid must have an inlet and an outlet.

End face mechanical seal materials must satisfy a number of design requirements, including chemical compatibility between the sealed fluid and the seal materials, ability of the seal materials to remain serviceable under the worst operating conditions, and ability to provide a reasonably long life in service at the operating conditions. Mating faces of the seals can be made from ordinary materials like bronze and PTFE

with sleeve

Fig. 8.6.42 High-performance lip seal with modified PTFE elastomer. Illustration shows single and staged elements.

for mild service on up to carbon, carbides, stainless steels, and other exotic alloys as service conditions become more severe. Hard faces can utilize ceramics, tungsten and silicon carbides, and hard coatings over base metals (chromium oxide over stainless steel 316SS, subsequently lapped flat).

Secondary seal materials are usually elastomeric and include these:

Environmental controls as applied to seals are special techniques used to control the environment in which the seal operates. Some examples include discharge return recirculation, suction return, flush from an outside source, flush, and quench and drain. The controlling techniques often require supplementary equipment such as heaters, coolers, pumping rings, external circulation devices, various special solenoids and valves compatible with the working environment, and so on. Sealed products that solidify, vaporize, abrade, or carry contaminants are successfully sealed with end face seals augmented by environmental controls.

High Performance Lip Seals The nature of some sealed products is such that end face mechanical seals are not applicable. In many difficult instances of that type, sealing can be achieved with high-performance modified PTFE lip seals (Fig. 8.6.42). Gylon is such a material which can serve in seals operating over a wide range of pressures, temperatures, and rotating speeds. It is particularly useful to seal against dry products, viscous resins, heavy slurries, salting solutions, and products which tend to solidify on seal faces. Dry running is possible under some circumstances. Unlike conventional lip seal material, modified PTFE lip seals in multiples can operate from high vacuums $(10^{-3}$ inHg) up to 10 bar (150 lb/in²), within a temperature range of -130 to $+500^{\circ}$ F $(-90$ to $+ 260^{\circ}$ C), and exhibit excellent compatibility with a wide range of sealed fluids. Manufacturers' literature will provide data showing the effect of temperature and rotating speed on the permissible operating pressure.

For extremely high speeds, where it is desirable to eliminate all rubbing contact, the **labyrinth** seal [\(Fig. 8.6.25\)](#page-138-0) is chosen. This seal is not fluid-tight but restricts serious flow by means of a torturous path and induced turbulence. It is widely used on steam turbines (Sec. 9.4). Where no leakage is permissible, a liquid seal based on the U-tube principle [\(Fig. 8.6.26\)](#page-138-0) may be used. The natural weight of the liquid is amplified by centrifugal force so that under high rotating speed a fair pressure differential can be sealed. Another noncontacting seal is the **controlled gap seal** which is being used on gas turbines where pressure differentials are not excessive and a small amount of leakage can be tolerated. The seal consists of a ring with a shaft clearance in the range of 0.0005 to 0.0015 in (0.013 to 0.038 mm) and is made of exotic heatresisting materials capable of maintaining that clearance at all operating temperatures. Usually one end of the ring is faced to form an axial seal against the inside of its housing.

Diaphragms are a form of dynamic packing but include the requirements of a gasket where they are gripped or held in position. In service they are leakless, although generally limited in travel. By literally rolling one cylinder inside another, considerable increase in travel is possible. This type is often called a bellows, and a simple application is the mechanical seal suspension shown i[n Fig. 8.6.31.](#page-138-0) In the diaphragm valve [\(Fig. 8.6.33\)](#page-138-0) the diaphragm replaces both the conventional stem packing and valve disk. **Diaphragms** of fabric such as cotton or nylon (except friable materials such as glass) covered with an elastomer suitable for the fluids and temperatures involved are used in pumps (fuel pump, [Fig. 8.6.35\)](#page-138-0) and in motors [\(Fig. 8.6.34\)](#page-138-0) to operate valves, switches, and other controls. Correctly designed diaphragms are made with slack to permit a natural rolling action. Flat sheet stock should be used only where limited travel is desired. An unusual application is shown in [Fig. 8.6.36,](#page-138-0) where the diaphragm is under balanced fluid pressure on both sides and is unstressed. Thin sheet metal, usually with concentric corrugations, is used where movement is limited and long life is desired. Where considerable movement is involved, the possibility of fatigue must be considered.

PTFE and Glyon diaphragms are used with chemically aggressive fluids. Experience shows that PTFE has a tendency toward cold flow, which leads to leaking at the clamp areas; Gylon has proved more dimensionally stable and serviceable.

8.7 PIPE, PIPE FITTINGS, AND VALVES by Helmut Thielsch

REFERENCES: M. L. Nayyar, ''Piping Handbook,'' McGraw-Hill. ANSI Code for Power Piping. ASTM Specifications. Tube Turns Division, Natural Cylinder Gas Co., catalogs. Crane Co., catalogs and bulletins. Grinnell Co., Inc., ''Piping Design and Engineering.'' M. W. Kellogg Co., ''Design of Piping Systems,'' Wiley. United States Steel Co., catalogs and bulletins.

EDITOR'S NOTE: The several piping standards listed in this section are subject to continuing periodic review and/or modification. It is suggested that the reader make inquiry to the issuing organizations (se[e Table 8.7.1](#page-143-0)) as to the currency of a given standard as listed.

PIPING STANDARDS

Codes for various piping services have been developed by nationally recognized engineering societies, standardization bodies, and trade associations. The sound engineering practices incorporated in these codes generally cover minimum safety requirements for the selection of materials, dimensions, design, fabrication, erection, and testing of piping systems. By means of interpretation and revision these codes continually reflect the knowledge gained through experience, testing, and research.

Generally, piping codes form the basis for many state and municipal safety laws. Compliance with a code which has attained this status is mandatory for all systems included within the jurisdiction. Although some of today's piping installations are not within the scope of any mandatory code, it is advisable to comply with the applicable code in the interests of safety and as a basis for contract negotiations. Contracts with various agencies of the federal government are regulated by federal specifications or rules. These often do not have a direct connection with the codes enumerated below.

The reader is cautioned that the **piping standards** are changing more often than in previous years. Although the formulas and other data provided are in accordance with the code rules in effect at the time of publication, it must be recognized that code rules may change, and piping engineering and design work performed in accordance with information contained herein does not provide complete assurance that all extant code requirements have been met. The reader is urged to become familiar with the specific code edition and addenda applicable in a particular project, for they may contain mandatory requirements applicable to the particular project.

The **ASME Boiler and Pressure Vessel Code** is mandatory in many cities, states, and provinces in the United States and Canada. Local application of this code into law is not uniform, making it necessary to investigate the city or state laws which have jurisdiction over the installation in question. Compliance with this code is required in all locations to qualify for insurance approval.

Section I: ''Power Boilers'' concerns all piping connections to power boilers or superheaters including the first stop valve on single boilers, or including the second stop valve for cross-connected multiple-boiler installations. Section I refers to ASME B31.1 which contains rules for design and construction of ''boiler external piping.'' ''Boiler external piping'' is under the jurisdiction of Section I and requires inspection and code stamping in accordance with Section I even though the rules for its design and construction are contained in the ASME Code for Pressure Piping, section B31.1.

Section II ''Material Specifications'' provides detailed specifications of the materials which are acceptable under this code. (These specifications generally are identical to the corresponding ASTM Standards.)

Section III: ''Nuclear Components'' includes all nuclear piping. It is the responsibility of the designer to determine whether or not a particular piping system is ''nuclear'' piping, since Section III makes this determination the responsibility of the designer. In general, piping whose failure could result in the release of radiation which would endanger the public or plant personnel is considered ''nuclear'' piping.

Section VIII: ''Unfired Pressure Vessels'' concerns piping only to the extent of the flanged or threaded connections to the pressure vessel, except that the entire section will apply in those special cases where unfired pressure vessels are made from pipe and fittings.

Section IX: ''Welding and Brazing Qualifications'' establishes the minimum requirements for ASME Code welding.

Section XI: ''Rules for Inservice Inspection of Nuclear Power Plant Components'' contains rules for the examination and repair of components throughout the life of the plant.

The ASME Code for Pressure Piping B31 is, at present, a nonmandatory code in the United States except where U.S. state legislative bodies and Canadian provinces have adopted this code as a legal requirement. The minimum safety requirements of these codes have been accepted by the industry as a standard for all piping outside the jurisdiction of other codes. The piping systems covered by the separate sections of this code are listed below:

Several other engineering societies and trade associations have also issued standards covering piping. Foremost among these is the American Society for Testing and Materials (ASTM), the American National Standards Institute (ANSI), the American Water Works Association (AWWA), the American Petroleum Institute (API), and the Manufacturers Standardization Society of the Valve and Fitting Industry (MSS).

Additional piping specifications have been issued by the American Welding Society (AWS), the Pipe Fabrication Institute (PFI), the National Fire Protection Association (NFPA), the Copper Development Association (CDA), the Plastics Pipe Institute (PPI), and several others.

The piping standards issued by the ASTM are most commonly referred to in specifications covering piping for power plants, chemical plants, refineries, pulp and paper mills, and other industrial plants. The large majority of ASTM Standards has also been issued by the ASME in Section II of the ASME Boiler and Pressure Vessel Code. The same specification numbers are applied by the ASME as were originally assigned by the ASTM.

The ANSI formerly prepared the various standards of the B31 Code for Pressure Piping. These standards are now issued by the ASME. The ANSI, however, continues to prepare and issue various standards covering pipe fittings, flanges, and other piping components. Note that ASME B16 prepares and issues standards for fittings, flanges, etc.

The AWWA has issued various standards for waterworks applications. The majority of these involve ductile iron pipe, ductile iron and cast iron pipe fittings, etc.

The MSS has prepared various standards for valves, hangers, and fittings, generally involving the lower range of pressures and temperatures.

[Table 8.7.1](#page-143-0) gives the most **commonly used piping standards** and the organizations from which the standards are available.

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NOTE: Footnotes appear at the end of the table.
Table 8.7.1 Commonly Used Piping Standards (*Continued***)**

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The referenced standards are available from the listed organizations:

* Indicates that the standard has been approved as an American National Standard by the American National Standards Institute.

[†] Including supplements to these API Standards through spring 1981.
NOTE: The issue date shown immediately following the hyphen after the number of the standard (e.g., B16.9-1978, C207-1978, and A 47-77) is the effective

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PIPING, PIPE, AND TUBING

The term **piping** generally is broadly applied to pipe, fittings, valves, and other components that convey liquids, gases, slurries, etc.

The term **pipe** is applied to tubular products of dimensions and materials commonly used for pipelines and connections, formerly designated as **iron pipe size (IPS)**. The outside diameter of all weights and kinds of IPS pipe is of necessity the same for a given pipe size on account of threading. Nevertheless, the large majority of pipe is furnished unthreaded with butt-weld ends.

The word **tube** (or **tubing**) is generally applied to tubular products as utilized in boilers, heat exchangers, instrumentation, and in the machine, aircraft, automotive, and related industries.

Pipe and Tube Products—General

Commercial pipe and tube products are grouped into various classifications generally based on the application or use and not on the manufacturing method. Most tubular products fall into one of three very broad classifications: (1) pipe, (2) pressure tubes, and (3) mechanical tubes. Each classification falls into various subgroupings, which may have been defined and standardized differently by the different trade or user groups. The same standard materials specifications may apply to several of the (user) classifications. For example, ASTM A120 or A53 pipe may be used for applications representing refrigeration, pressure, and nipple service.

Cost considerations enter into the selection of specific piping materials. In some sizes, prices of pipe made to different materials specifications may vary, whereas in other sizes, they may be identical.

Within the broad **use classifications** listed above, the **production method classifications** are also recognized. These are primarily (1) seamless wrought pipe, (2) seamless cast pipe, and (3) seam-welded pipe or tubes. The large variety of single and combination pipe- or tube-forming methods can produce different characteristics and properties in essentially identical pipe materials. In addition, the final finishing can result in hot-finished or cold-finished products. Cold-finishing may be accomplished by reducing or by expanding. Heat treatments may also affect the properties of the finished product.

Piping

On the basis of user classification, the more commonly used types of pipe are tabulated in Table 8.7.2. This listing ignores method of manufacture, size range, wall thickness, and finish, for which the different user groups may have developed different standard requirements.

Table 8.7.2 Major Pipe Classification and Examples of Applications

| Identification of pipe | Uses | | | | |
|---------------------------|---|--|--|--|--|
| Standard | Mechanical (structural) service pipe, low-pres- sure service pipe, refrigeration (ice-machine) pipe, ice-rink pipe, dry-kiln pipe | | | | |
| Pressure | Liquid, gas, or vapor service pipe, service for elevated temperature or pressure, or both | | | | |
| Line | Threaded or plain end, gas, oil, and steam pipe | | | | |
| Water well | Reamed and drifted, water-well casing, drive pipe, driven well pipe, pump pipe, turbine- pump pipe | | | | |
| Oil country tubular goods | Casing, well tubing, drill pipe | | | | |
| Other pipe | Conduit, piles, nipple pipe, sprinkler pipe, bed- stead tubing | | | | |

Standard Pipe Mechanical service pipe is produced in three classes of wall thickness—standard weight, extra strong, and double extra strong. It is available as welded or seamless pipe of ordinary finish and dimensional tolerances, produced in sizes up to 12-in nominal OD. This pipe is used for structural and mechanical purposes. Certain applications have other requirements for size, surface finish, or straightness.

Refrigeration Pipe This pipe is also known as ice-machine pipe or ammonia pipe. It may be butt-welded, lap-welded, electric-resistancewelded, or seamless and is intended for use as a conveyor of refrigerants. This pipe is suitable for coiling, bending, and welding. The sizes commonly used range from 3⁄4 to 2 in. The piping is produced in random and double random lengths in standard line pipe sizes and weights. Double random lengths are used as ice-rink pipe. It can be produced with plain ends, with threaded ends only, or with threaded ends and line pipe couplings, as desired.

Dry-Kiln Pipe This pipe is butt-welded, electric-resistance-welded, or seamless pipe for use in the lumber industry. It is produced in standard-weight pipe sizes of $\frac{3}{4}$, 1, and $\frac{1}{4}$ in. Joints are designed to permit subsequent ''makeup'' after expansion has occurred. Dry-kiln pipe is commonly produced with threaded ends and couplings and in random lengths.

Pressure Pipe Pressure pipe is used for conveying fluids or gases at normal, subzero, or elevated temperatures and/or pressures. It generally is not subjected to external heat application. The range of sizes is $\frac{1}{8}$ -in nominal size to 36-in actual OD. It is produced in various wall thicknesses. Pressure piping is furnished in random lengths, with threaded or plain ends, as required. Pressure pipe generally is hydrostatically tested at the mill.

Line Pipe Line pipe is seamless or welded pipe produced in sizes from 1⁄8-in nominal OD to 48-in actual OD. It is used principally for conveying gas, oil, or water. Line pipe is produced with ends which are plain, threaded, beveled, grooved, flanged, or expanded, as required for various types of mechanical couplers, or for welded joints. When threaded ends and couplings are required, recessed couplings are normally supplied.

Water-Well Pipe Water-well pipe is welded or seamless steel pipe used for conveying water for municipal and industrial applications. Pipelines for such purposes involve flow mains, transmission mains, force mains, water mains, or distribution mains. The mains are generally laid underground. Sizes range from 1⁄8- to 106-in OD in a variety of wall thicknesses. Pipe is produced with ends suitably prepared for mechanical couplers, with plain ends beveled for welding, with ends fitted with butt straps for field welding, or with bell-and-spigot joints with rubber gaskets for field joining. Pipe is produced in double random lengths of about 40 ft, single random lengths of about 20 ft, or in definite cut lengths, as specified. Wall thicknesses vary from 0.068 in for 1⁄8-in nominal OD to 1.00 in for 106-in actual OD.

When required, water-well pipe is produced with a specified coating or lining or both. For example, cement-mortar lining and coatings are extensively used.

Oil Country Goods Casing is used as a structural retainer for the walls of oil or gas wells. It is also used to exclude undesirable fluids, and to confine and conduct oil or gas from productive subsurface strata to the ground level. Casing is produced in sizes 41⁄2- to 20-in OD. Size designations refer to actual outside diameter and weight per foot. Ends are commonly threaded and furnished with couplings. When required, the ends are prepared to accommodate other types of joints.

Drill Pipe Drill pipe is used to transmit power by rotary motion from ground level to a rotary drilling tool below the surface and also to convey flushing media to the cutting face of the tool. Drill pipe is produced in sizes 23⁄8- to 65⁄8-in OD. Size designations refer to actual outside diameter and weight per foot. Drill pipe is generally upset, either internally or externally, or both, and is furnished with threaded ends and couplings, threaded only, or prepared to accommodate other types of joints.

Tubing is used within the casing of oil wells to conduct oil to ground level. It is produced in sizes 1.050- to 4.500-in OD in several weights per foot. Ends are threaded and fitted with couplings and may or may not be upset externally.

Other Pipe Classifications Rigid conduit pipe is welded or seamless pipe intended especially for the protection of electrical wiring systems. Conduit pipe is not subjected to hydrostatic tests unless so specified. It is furnished in standard-weight pipe sizes from 1⁄4- to 6-in OD in 10-ft lengths,* with plain ends or with threaded ends and couplings, as specified.

Piling pipe is welded or seamless pipe for use as piles, where the cylinder section acts as a permanent load-carrying member or where it acts as a shell to form cast-in-place concrete piles. Specifications provide for the choice of three grades by minimum tensile strength, in which the sizes listed are 8⁵/8- to 24-in OD in a variety of wall thicknesses and in two length ranges. Ends are plain or beveled for welding.

Nipple pipe is standard-weight, extra-strong, or double-extra-strong welded or seamless pipe produced for the manufacture of pipe nipples. Standard-weight pipe with threaded ends is also used in sprinkler systems. Nipple pipe is commonly produced in random lengths with plain ends in nominal sizes 1/8- to 12-in OD. Close OD tolerances, sound welds, good threading properties, and surface cleanliness are essential in this product. It is commonly coated with oil or zinc and well protected in shipment. When reference is made to ASTM Specifications for this application, Specification A120 is generally used for diameters to 5-in OD and A53 for diameters of 5 in and over.

Standard Pipe Sizes Standard pressure, line, and other pipe with plain ends for welding or with threaded ends is standardized in two ranges. Diameters of 12 in and less have a nominal size which represents approximately that of the inside diameter of standard-weight pipe. The nominal outside diameter is standard, regardless of weight. Increase in wall thickness results in a decrease of the inside diameter.

The standardization of pipe sizes over 12 in is based on the actual outside diameter, the wall thickness, and the weight per foot.

The principal dimensions, weights, and characteristics of commercial piping materials are summarized i[n Table 8.7.3.](#page-147-0)

The weights of butt-welding elbows, tees, and laterals and flanges are given in [Tables 8.7.4](#page-154-0) to 8.7.9 for several common pipe sizes. The weights of reducing fittings are approximately the same as for full-size fittings.

The weights of welding reducers are for one size reduction and are thus only approximately correct for other reductions.

Hot-finished or cold-drawn seamless low-alloy steel tubes generally are process-annealed at temperatures between 1,200 and 1,350°F.

Austenitic stainless-steel tubes are usually annealed at temperatures between 1,800 and 2,100°F, with specific temperatures varying somewhat with each grade. This is generally followed by pickling, unless bright-annealing was done.

Mechanical Tubing

Unlike pipe and pressure tubes, mechanical tubing is generally classified by the method of manufacture and the degree of finish. Examples of classifications are ''seamless hot-finished,'' ''cold-drawn welded,'' ''flash-in-grade,'' etc.

Seamless Tubes Seamless tubes are available as either hot- or cold-finished. They are normally made in sizes from 0.187-in OD to 10.750-in OD.

Dimensions for hot-finished mechanical tubes are provided in [Table](#page-166-0) [8.7.11.](#page-166-0) Dimensions for cold-finished tubes are listed i[n Table 8.7.12.](#page-167-0)

Welded Tubes Welded tubes generally are produced by electric resistance methods. Where required, the welding flash is removed with a cutting tool. Industry practice normally recognizes a number of finish conditions which are summarized i[n Table 8.7.13.](#page-168-0)

Flash-in Type Tubing This tubing is generally limited to applications where nothing is inserted in the tube.

Flash-Controlled Tubing This tubing is used where moderate control of the inside diameter is required. Generally, the outside and inside diameters are specified.

For special materials, the equations listed below for weights of tubes and weights of contents of tubes are helpful.

Weight of tube, $1b/ft = F \times 10.68 \times T \times D - T$

* Although some specifications of rigid conduit pipe list lengths to 20 ft, the National Electric Code, 1965, limits lengths to 10 ft.

where $T =$ wall thickness, in; $D =$ outside diameter, in; $F =$ relative weight factor.

The weight of tube calculation is based on low-carbon steel weighing 0.2833 lb/in3 and is extended to other materials through the factor *F.*

Weight of contents of tube, $\frac{1}{b}$ /ft = $G \times 0.3405 \times (D - 2T)^2$

where $G =$ specific gravity of contents; $T =$ tube wall thickness, in; $D =$ tube outside diameter, in.

The weight per foot of steel pipe is subject to the tolerances listed in [Table 8.7.10.](#page-166-0)

The designation *sink-draw tubes* is specified where close control over the outer diameter is required with normal tolerance applying to the wall thickness. Smoothness of the inside surface is not controlled, except that the flash is generally controlled to a height of 0.005 or 0.010 in maximum.

Mandrel-drawn tubes usually are normalized after welding by passing the tubes through a continuous atmosphere-controlled furnace. After descaling, the tubes are cold-drawn through a die with a mandrel on the inside of the tube. These tubes provide maximum control over surface finish, outside or inside diameters, and wall thickness. The normalizing heat treatment removes the effects of welding and provides a uniform microstructure around the tube circumference.

The different finish classifications may result in substantial differences in the mechanical properties of the steel material.

Typical examples for low-carbon steel material are given in [Table](#page-168-0) [8.7.14.](#page-168-0) Differences in carbon content and other chemistry, heat treatment, etc., may significantly change these typical values.

Other Tubing Types Among other tube classifications are sanitary tubing usually made of 18% Cr-8% Ni stainless steel and available as seamless or welded tubing. This tubing is used extensively in the dairy, beverage, and food industries. Sanitary tubing is generally available in sizes from 1- to 4-in OD. It may be furnished either hot- or cold-finished. The tubes are normally annealed at temperatures above 1,900°F.

Some welded tube is also produced by fusion-welding methods utilizing either the inert-gas tungsten-arc-welding or gas-shielded consumable metal-arc-welding process. This tubing is generally more expensive than the resistance-welded types.

The butt-welded cold-finished tubes are made from hot-rolled or cold-rolled strip and fusion-welded. This tubing is usually furnished as sink-drawn or mandrel-drawn.

Butt-welded tubing is made in heavier wall thicknesses than the resistance-welded tube.

Several tubing materials used in the automobile industry are covered by specifications of the Society of Automotive Engineers, ''SAE Handbook.''

Pressure Tubing

Pressure-tube applications commonly involve external heat applications, as in boilers or superheaters.

Pressure tubing is produced to the actual outside diameter and minimum wall or average wall thickness specified by the purchaser. Pressure tubing may be hot- or cold-finished.

The wall thickness is normally given in decimal parts of an inch rather than as a fraction or gage number. When gage numbers are given without reference to a gage system, Birmingham wire gage (BWG) is implied.

Pressure tubing is usually made from steel produced by the openhearth, basic oxygen, or electric-furnace processes.

Table 8.7.3 Properties of Commercial Steel Pipe

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NOTE: See footnotes at end of table.

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Table 8.7.3 Properties of Commercial Steel Pipe (*Continued***)**

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Table 8.7.3 Properties of Commercial Steel Pipe (*Continued***)**

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NOTE: See footnotes at end of table.

Table 8.7.3 Properties of Commercial Steel Pipe (*Continued***)**

NOTE: The following formulas are used in the computation of the values shown in the table:

where A_m = area of metal, in²; d = inside diameter, in; D = outside diameter, in; R_g = radius of gyration, in; t = pipe wall thickness, in.
* Schedule numbers: Standard-weight pipe and schedule 40 are the same 8 in through 24 in, extra-strong-weight pipe has a wall thickness of $\frac{1}{2}$ in. Double-extra-strong-weight pipe has no corresponding schedule number.

a: ANSI B36.10 steel pipe schedule numbers b: ANSI B36.10 steel pipe nominal wall thickness designation

c: ANSI B36.19 stainless steel pipe schedule numbers

† The ferritic steels may be about 5% less and the austenitic stainless steels about 2% greater than the values shown in this table, which are based on weights for carbon steel.

Table 8.7.4 Weight of Standard Pipe Fittings and Materials, 3-in Size (3.500-in OD) (Continued)

NOTES: Boldface type is weight in pounds. Lightface type beneath weight is weight factor for insulation.

Insulation thicknesses and weights are based on average conditions and do not constitute a recommendation for specific thicknesses of materials. Insulation weights are based on 85% magnesia and hydrous calcium silicate at thicknesses and weights of combination covering are the sums of the inner layer of diatomaceous earth at 21 lb/ft³ and the outer layer at 11 lb/ft³.

Insulation weights include allowances for wire, cement, canvas, bands and paint, but no special surface finishes.

To find the weight of covering on flanges, valves or fittings, multiply the weight factor by the weight per foot of covering used on straight pipe.

Valve weights are approximate. When possible, obtain weights from the manufacturer.

Cast-iron valve weights are for flanged end valves; steel weights for welding end valves.

All flanged fitting, flanged valve and flange weights include the proportional weight of bolts or studs to make up all joints.

* 16 lb/ft3 density. (Existing installations only.)

Table 8.7.5 Weights of Standard Pipe Fittings and Materials, 4-in Size (4.500-in OD)

| | | Schedule no. Wall designation Thickness, in Pipe, lb/ft Water, lb/ft | 40 Std 0.237 10.79 5.51 | 80 XS 0.337 14.98 4.98 | 120 0.438 18.96 4.48 | 160 0.531 22.51 4.02 | XXS 0.674 27.54 3.38 | | | | | | |
|------------------|--------------------------------------|--|-------------------------------------|------------------------------------|-------------------------------|-------------------------------|--------------------------------------|------------------------|------------------------|------------------------|------------------------|-------------------------|-------------------------|
| Welding fittings | G | L.R. 90° elbow | 8.7 1 | 11.9 | | 17.6 1 | 21 -1 | | | | | | |
| | | S.R. 90° elbow | 5.8 0.7 | 7.9 0.7 | | | | | | | | | |
| | | L.R. 45° elbow | 4.3 0.4 | 5.9 0.4 | | 8.5 0.4 | 10.1 0.4 | | | | | | |
| | | Tee | 12.6 | 16.4 | | 23 $\mathbf{1}$ | $\bf 27$ $\mathbf{1}$ | | | | | | |
| | | Lateral | 21 2.1 | 33 2.1 | | | | | | | | | |
| | | Reducer | 3.6 0.3 | 4.9 \cdot 3 | | 6.6 \cdot 3 | 8.2 0.3 | | | | | | |
| | | Cap | 2.6 0.6 | 3.4 0.6 | | 6.5 0.6 | 6.7 0.6 | | | | | | |
| | Temperature range, °F | | $100 - 199$ | $200 - 299$ | $300 - 399$ | $400 - 499$ | $500 - 599$ | $600 - 699$ | $700 - 799$ | $800 - 899$ | $900 - 999$ | $1,000 - 1,099$ | $1,100-1,200$ |
| Insulation | 85% magnesia calcium silicate | Nom. thick., in 1b/ft | 1 1.62 | 1.62 | $1\frac{1}{2}$ 2.55 | \overline{c} 3.61 | $2\frac{1}{2}$ 4.66 | $2\frac{1}{2}$ 4.66 | 3 6.07 | 3 6.07 | $3\frac{1}{2}$ 7.48 | $3\frac{1}{2}$ 7.48 | $\overline{4}$ 9.10 |
| | Combination | Nom. thick., in 1b/ft | | | | | | $2\frac{1}{2}$ 6.07 | 3 8.30 | \mathfrak{Z} 8.30 | $3\frac{1}{2}$ 10.6 | $3\frac{1}{2}$ 10.6 | $3\frac{1}{2}$ 10.6 |
| | Asbestos fiber-sodium silicate | Nom. thick., in 1b/ft | $\mathbf{1}$ 2.04 | 2.04 | 1 2.04 | $1\frac{1}{2}$ 3.28 | $1\frac{1}{2}$ 3.28 | $\overline{2}$ 4.70 | $\overline{2}$ 4.70 | $\mathbf{3}$ 8.29 | 3 8.29 | $3\frac{1}{2}$ 10.25 | $3\frac{1}{2}$ 10.25 |

Table 8.7.5 Weights of Standard Pipe Fittings and Materials, 4-in Size (4.500-in OD) (Continued)

NOTE: See footnotes to [Table](#page-154-0) [8.7.4](#page-154-0).

Table 8.7.6 Weights of Standard Pipe Fittings and Materials, 8-in Size (8.625-in OD) (Continued)

NOTE: See footnotes to [Table](#page-154-0) [8.7.4](#page-154-0).

Table 8.7.7 Weights of Standard Pipe Fittings and Materials, 12-in Size (12.750-in OD)

NOTE: See footnotes to [Table](#page-154-0) [8.7.4](#page-154-0).

Table 8.7.8 Weights of Standard Pipe Fittings and Materials, 24-in Size (24-in OD)

Table 8.7.8 Weights of Standard Pipe Fittings and Materials, 24-in Size (24-in OD) (Continued)

NOTE: See footnotes to [Table](#page-154-0) [8.7.4](#page-154-0).

Table 8.7.9 Weights of Standard Pipe Fittings and Materials, 36-in Size (36-in OD) (Continued)

NOTE: See footnotes to [Table](#page-154-0) [8.7.4](#page-154-0).

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| Specification | Size | Tolerance, % | | |
|------------------------|-------------------------|--------------|--------|--|
| ASTM A53 | Std wt | $+5$ | -5 | |
| | XS wt | $+5$ | -5 | |
| ASTM A120 | XXS wt | $+10$ | -10 | |
| ASTM A106 | Sch $10-120$ | $+6.5$ | -3.5 | |
| | Sch 140-160 | $+10$ | -3.5 | |
| ASTM A335 | 12 in and under | $+6.5$ | -3.5 | |
| | Over 12 in | $+10$ | -5 | |
| ASTM A312 ASTM A376 | 12 in and under | $+6.5$ | -3.5 | |
| | Std. wt | | | |
| | Reg wt | | | |
| | XS wt | $+10$ | -3.5 | |
| API _{5L} | XXS wt | | | |
| | Spec. plain end pipe | $+10$ | - 5 | |

Table 8.7.10 Weight Tolerances of Steel Piping

Seamless pressure tubing may be either hot-finished or cold-drawn. Cold-drawn steel tubing is frequently process-annealed at temperatures above 1,200°F. To ensure quality, maximum hardness values are frequently specified. For example, in ASME Specification SA192,* Specification for Seamless Carbon Steel Boiler Tubes for High-Pressure Service, the following maximum hardness values are given.

Piping Fabrication Methods Commercial steel pipe is furnished most commonly as seamless pipe. Seamless pipe can be produced by (1) piercing, (2) hollow forging, and (3) forging, turning, and boring. Commercial pipe is also produced by welding involving (1) electric resistance welding, (2) electric fusion welding, or (3) submerged arc welding. Some mills are prepared to extrude small-diameter pipe and tubing in a variety of geometric shapes or to cast large-diameter steel pipe.

Electric-Fusion Welding Flat plate, known as **skelp,** is prepared in proper width and thickness for the desired pipe inside and outside diameters. It is then charged into an electric furnace and, when the proper welding temperature has been reached, is drawn through a funnel-

* Specifications for boiler tubes generally reference the ASME Standards such as SA178, SA192, SA210, etc.

shaped die so shaped that the plate is gradually formed into the shape of a tube, with the edges of the plate being forced squarely together and fused. The formed pipe then passes through a series of rolls in which it is sized or drawn to final dimensions.

Electric-Resistance Welding For pipes or tubes sized 4-in (10.2 cm) OD and under, strip is fed onto a set of forming rolls which consists of horizontal and vertical rollers so placed as to gradually form the flat strip into a tube. The tube form then passes to the welding electrodes. The electrodes are copper disks connected to the secondary of a revolving transformer assembly. The copper-disk electrodes make contact on each side of the seam of the tube form; a flow of current takes place across the seam, and temperature is raised to the welding point. Outside flash is removed by a cutting tool as the tube leaves the electrodes; inside flash is removed either by an air hammer or by passing a mandrel through the welded tube after the tube has been cooled.

Submerged-Arc Electric Welding This process is used for pipes from 24-in to 36-in (61.0- to 9.1.4-cm) OD. Flat plate is first pressed into a U and later into an O shape. The O shape is placed in an automatic welder and backed up on the inside by a water-cooled copper shoe. Two electrodes in close proximity are used. The electrodes are not in actual contact with the pipe. The current passes from one electrode through a granular flux and across the gap in the pipe to the second electrode. The high temperature of the arc heats the edges of the plate; a welding rod placed just over the seam is thereby melted and metal is deposited in the groove. After the outside weld has been made, the pipe is conveyed to an inside welder where a similar operation is carried on, except that no backup shoe is needed.

Seamless Tubing and Pipe A heated billet is brought into contact with tapered revolving rolls in such a way that the billet is pulled into the space allowed between the rolls. A piercing mandrel is placed in this space; the soft center of the billet makes it possible for the rolls to draw the billet over the mandrel, producing a hollow shell. When the billet has entirely passed over the mandrel, it is in the form of a thick-walled seamless tube. The heavy-walled tube is then passed to a rolling mill which reduces the tube to pipe of proper outside diameter and wall thickness.

The method of fabrication described above is limited as to diameter and thickness. For seamless alloy tubes and for heavy-wall carbon-steel tubes or pipe, a process known as **cupping and drawing** is frequently used. A circular flat plate of proper diameter and thickness is heated, placed in a hydraulic press, and pressed by a ram through a die. The cup so formed is reheated and pressed through a smaller die, thus elongating the cup so that it becomes a short cylinder with one closed end. This short cylinder is then placed in a horizontal drawbench, and with reheating as necessary, is pushed by a ram through dies of successively smaller diameters until the desired outer diameter is reached.

Forged, Turned, and Bored Tubing In this process, the ingot is heated and forged to a rough cylindrical shape, oversize in both diameter and length. The forging is then placed in a lathe and the outside turned down to the desired outer diameter. Rough ends are then removed so that the finally desired length is obtained. The cylinder is then placed in a boring mill, and the inside bored out until the desired wall

* The common range of sizes of hot-finished tubes is 11⁄2 to and including 103⁄4 in outside diameter with wall thickness not less than 0.095 in (no. 13 BWG) or 3% or more of the outside diameter. For sizes under 11/2 or over 103⁄4 in outside diameter, the tolerances are commonly negotiated between the purchaser and producer.

SOURCE: AISI, ''Steel Products Manual.''

Table 8.7.12 Diameter and Wall-Thickness Tolerances for Seamless Cold-Worked Mechanical Tubing of Carbon and Alloy Steel (AISI)*

* For tolerances closer than those indicated, availability, and applicable tolerances for tubing less than 3⁄16 in OD or larger than 103⁄4-in OD, the producer should be consulted.

† For those tubes with inside diameter less than ½ in (or less than % in when the wall thickness is more than 20% of the outside diameter), which are not commonly drawn over a mandrel. Note § is not applicable. Unless othe and producer, the wall thickness may vary 15% over and under that specified, and the inside diameter is governed by the outside diameter and wall-thickness tolerances shown.

t For tubes with inside diameter less than 1/2 in (or less than 7/8 in when the wall thickness is more than 20% of the outside diameter), which can be produced by the rod or bar mandrel process, the tolerances are as shown wall-thickness tolerances are 10% over and under the specified wall thickness.

§ Many tubes with inside diameter less than 50% of outside diameter, or with wall thickness more than 25% of outside diameter, or with wall thickness over 1/4 in, or weighing more than 90 lb/ft are difficult to draw over a by the purchaser and producer the inside diameter may vary over or under by an amount equal to 10% of the wall thickness and the wall thickness may vary 121/2% over and under that specified.

Tubing having a wall thickness less than 3% of the outside diameter cannot be straightened properly without a certain amount of distortion. Consequently, such tubes, while having an average outside diameter and inside diam the above table, require an ovality tolerance of 0.5% over and under nominal outside diameter, this being in addition to the tolerances indicated in the above table.

SOURCE: AISI, ''Steel Products Manual.''

Table 8.7.13 Finish Classifications Normally Recognized as Welded Mechanical Tubing

thickness is secured. Because of the relatively high cost, this process is now rarely used.

Hollow-Forged Pipe and Tubing In this process, ingots are cast and their ends cropped; then they are placed in a furnace and heated to a specified temperature. The heated ingot is placed in a press where it is pierced. This hollow cylinder, open at one end, is then descaled and drawn over a mandrel on a horizontal drawbench. The closed end is then burned off, and the hollow forging is chemically descaled. Following this, the forging is straightened, placed in a lathe, and the outer diameter machined to a true dimension. The inside is dressed to remove scale, but no machining is done on the inside.

Carbon-steel piping is most frequently used as manufactured in accordance with ASTM Specifications A106 and A53 (or ASME Specifications SA106 and SA53). The chemical compositions of these two materials are identical except for the deoxidation practice which applies to the A106 pipe. Both are subjected to physical tests, but those for A106 are more rigorous. A53 and A106 are made in grades A and B; grade B has higher strength properties but is less ductile and, for this reason, grade A is permitted only for cold bending or close coiling. When carbon steel is intended for use in welded construction at temperatures in excess of 775°F (413°C), consideration should be given to the possibility of graphite formation.

Chromium-molybdenum steel has been used for temperatures up to 1,100°F (593°C). In the small diameters, the material is usually available in the seamless construction; because of the inability of the seamless mills to fabricate large-diameter and heavy-walled pipe, it may be necessary to resort to the more expensive hollow-forged or forged-andbored piping for higher pressures and temperatures. The material for a high-temperature piping system should be selected after a careful review of technical and economic considerations; the following is intended only as being indicative of recent and current practice.

For temperatures up to 1,000°F, 1¼% Cr-1⁄2% Mo (A335, grade Pll) is used. For temperatures from 950 to 1050°F, 21⁄4% Cr-1% Mo (A335, P22) generally is used. Where there is a combination of high temperatures and erosive action, 5% Cr-1⁄2% Mo (A335, grade 5) or other more highly chromium-molybdenum or chromium stainless steels have been used.

Stainless-steel piping is available in a variety of compositions, most popular of which are ASTM A213, grade TP304 (16% Cr–8% Ni), and ASTM A213, grade TP316 (18% Cr–12% Ni and 3% Mo). For hightemperature service, type 34 stainless steels are used (18% Cr–8% Ni and stabilized with columbium). This material may be used up to 1,200°F (649°C); particular care must be given to choice of welding filler metal to avoid brittleness in the welds.

The permissible stress values for a large variety of piping materials at low and elevated temperatures are provided i[n Table 8.7.15.](#page-169-0)

PIPE FITTINGS

The various major piping materials are also produced in the form of standard fittings. Among the more widely used are wrought-steel fittings, welded-steel fittings, cast-steel fittings, cast-iron fittings, ductileiron fittings, malleable-iron fittings, brass and copper fittings, aluminum fittings, etc. Other major nonferrous piping materials are also produced in the form of cast and wrought fittings.

Cast-iron, ductile-iron, and malleable-iron fittings are made by conventional founding methods for a variety of joints including bell-andspigot, flanged, and mechanical (gland-type), or other proprietary joint designs.

Schedule Designations Over 100 years ago piping was designated as standard, extra-strong, and double extra-strong. There was no provision for thin-walled pipe, and no intervening standard thicknesses between the three schedules, which covered too great a spread to be economical without intermediate weights. [Table 8.7.3](#page-147-0) lists piping as a function of the schedule number which is given, approximately, by the following relationship: Schedule no. $= 1,000 P/(SE)$, where *P* is operating pressure, lb/in2 gage, *S* is allowable stress, lb/in2 [\(Table 8.7.15\)](#page-169-0), and *E* is the quality factor [\(Tables 8.7.16](#page-182-0) and 8.7.17).

Commercial sizes of steel pipe are known by their nominal inside diameter (ID) from $\frac{1}{8}$ in (0.3175 cm) to 12 in (30.5 cm). Above 12-in ID, pipe is usually known by its outside diameter (OD). All classes of pipe of a given nominal size have the same OD, the extra thickness for different weights being on the inside.

Thickness of Pipe The following notes, covering power piping systems, have been abstracted from Part 2 of the Code for Power Piping (ASME B31.1).

For inspection purposes, the minimum thickness of pipe wall to be used for piping at different pressures and for temperatures not exceeding those for the various materials liste[d in Table 8.7](#page-169-0).15 shall be determined by the formula

$$
t_m = \frac{PD}{2(SE + Py)} + A \tag{8.7.1}
$$

where t_m = minimum pipe-wall thickness, in, allowable on inspection; $P =$ maximum internal service pressure, lb/in² gage (plus water-

Table 8.7.14 Typical Mechanical Properties of Resistance-Welded Mechanical Carbon-Steel Tubing

| Type | Yield strength, 1 ^b /in ² | Tensile strength, 1 ^b /in ² | Elongation, % | Hardness. Rockwell B |
|---|--|--|------------------|-------------------------|
| Flash-in or flash-controlled, hot-rolled | 48,000 | 58,000 | 29 | 68 |
| Flash-in or flash-controlled, cold-rolled | 68,000 | 76,000 | | 84 |
| Normalized | 34,000 | 52,000 | 39 | 61 |
| Sink-drawn | 73,000 | 76,000 | 20 | 84 |
| Mandrel-drawn- | 80,000 | 83,000 | | 86 |

8-170 PIPE, PIPE FITTINGS, AND VALVES

A 299 (> 1 in thick) A 672 1 N75 (57) (67) - 20 75 40
A 299 (≤ 1 in thick) A 672 1 N75 (57) (67) - 20 75 42

NOTE: Footnotes appear at the end of the table.

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8-172 PIPE, PIPE FITTINGS, AND VALVES

PIPE FITTINGS 8-173

8-174 PIPE, PIPE FITTINGS, AND VALVES

Table 8.7.15 Basic Allowable Stresses in Tension for Metals (*Continued***)**

PIPE FITTINGS 8-175

8-176 PIPE, PIPE FITTINGS, AND VALVES

PIPE FITTINGS 8-177

8-178 PIPE, PIPE FITTINGS, AND VALVES

PIPE FITTINGS 8-179

8-180 PIPE, PIPE FITTINGS, AND VALVES

SOURCE: Adapted from ASME B31.3-1984 with permission.

† Numbers in parentheses refer to notes at end of table. All specifications are ASTM unless noted otherwise.

‡ In the table, SMTS = standard minimum tensile stress, S
PIPE FITTINGS 8-181

8-182 PIPE, PIPE FITTINGS, AND VALVES

Table 8.7.15 Basic Allowable Stresses in Tension for Metals (*Continued***)**

NOTES: These notes are requirements of the Code. Those marked with an asterisk (*) restate requirements found in the text of the Code. The other notes are limitations or special requirements applicable to particular materials. At this time, metric equivalents have not been provided in the stress tables for metals. (P-number groupings, tables, and appendixes cited in these notes fo[r Table](#page-169-0)
[8.7.15](#page-169-0) will be found i

(1)* The stress values in Table A-1 and the design stress values in Table A-2 are basic allowable stresses in tension in accordance with 302.3.1(a). For pressure design, the stress values from Table A-1 are multiplied by the appropriate quality factor $E(E_c$ from Table A-1A, or E_j from Table A-1B). Stress values in shear and bearing are stated in 302.3.1(b); those in compression in 302.3.1(c).
(2)* The quality facto with 302.3.4(a). See 302.3.3(c) and 302.3.4(b) for enhancement of quality factors. See also 302.3.1(a), footnote 9.

(3)* This casting quality factor can be enhanced by supplementary examination in accordance with 302.3.3(c) and Table 302.3.3C. The higher factor from Table 302.3.3C may be substituted for this factor in pressure design equations.

(4)* In shaded areas, stress values printed in *italics* exceed two-thirds of the expected yield strength at temperature. All other stress values in shaded areas are equal to 90% of expected yield strength at temperature. See $302.3.2(d)(4)$ and $302.3.2(d)$ [Note (3)].

(5)* See 327.5.2 for description of P-number groupings.

(6)* The minimum temperature shown is that design minimum temperature for which the material is normally suitable without impact testing other than that required by the material specification.
However, the use of a materi

 $(7)*$ A single bar (|) in these stress tables indicates there are conditions other than stress which affect usage above or below the temperature, as described in other referenced notes. A double bar (||) after a tabled stress indicates that use of the material is prohibited above that temperature. A double bar (||) before the stress value for "Min. temp. to 100°F" indicates that the use of the material is prohibited below (8)* There are restrictions on the use of this material in the text of the Code.

(9)* Pressure-temperature ratings of cast and forged parts as published in standards referenced in this Code section may be used for parts meeting requirements of these standards. Allowable stresses
for castings and forgin

(10)* These casting quality factors are applicable only when proper supplementary examination has been specified (see 302.3.3).

(11) For use under this Code, radiography shall be performed after heat treatment.
(12)* Certain forms of this material, as stated in Table 323.2.2, must be impact-tested to qualify for service below – 20°F (–29°C). Altern material specification as supplementary requirements and are invoked, the material may be used down to the temperature at which the test was conducted in accordance with the specification.

(13) Properties of this material vary with thickness or size. Stresses are based on minimum properties for the thickness listed.

(14) For use in Code piping at the stated stress values, the required minimum tensile and yield properties must be verified by tensile test at the mill. If such tests are not required by the material specification, they shall be specified in the purchase order. (15) These stress values are established from a consideration of strength only and will be satisfactory for average service. For bolted joints where freedom from leakage over a long period of time

without retightening is required, lower stress values may be necessary as determined from the flexibility of the flange and bolts and corresponding relaxation properties.
(16) This joint factor shall be applied to stress v (17)* Filler metal shall not be used in the manufacture of this pipe or tube.

(18)* This specification does not include requirements for 100% radiographic inspection. If this higher joint factor is to be used, the material shall be purchased to the special requirements of Table
327.4.1A for longitud

(19)* This specification includes requirements for random radiographic inspection for mill quality control. If the 0.90 joint factor is to be used, the welds shall meet the requirements of Table 327.4.1A for longitudinal butt welds with spot radiography in accordance with Table 302.3.4. This shall be a matter of special agreement between purchaser and manufacturer.
(20) For pipe sizes NPS 8 and larger and for wall

(22) The minimum tensile strength for weld (qualification) and stress values shown shall be multiplied by 0.90 for pipe having an outside diameter less than 2 in (51 mm) and a *D*/*t* value less than 15.

This requirement may be waived if it can be shown that the welding procedure to be used will consistently produce welds that meet the listed minimum tensile strengths of 24.0 ksi (165 MPa).
(23) Stress values apply only t construction.

(24) Yield strengths listed are not included in the material specifications. The value shown is based on yield strengths of materials with similar characteristics.

(26) These unstabilized grades of stainless steel have increasing tendency to intergranular carbide precipitation as the carbon content increases above 0.03%.
(27) For temperatures above 800°F (425°C), these stress values

(28) For temperatures above 1,000°F (538°C), these stress values apply only when the carbon content is 0.04% or higher.
(29) The higher stress values at 1,050°F (568°C) and above for this material shall be used only when t

(30) For temperatures above 1,000°F (538°C), these stress values may be used only if the material has been heat-treated at a temperature of 2,000°F (1,090°C) minimum.
(31) For temperatures above 1,000°F (538°C), these stre water or rapidly cooling by other means.

(32) Stress values shown are for the lowest-strength base material permitted by the specification to be used in the manufacture of this grade of fitting. If a higher strength base material is used, the higher stress values for that material may be used in design.

 (33) For welded construction with work-hardened grades, use the stress values for annealed material; for welded construction with precipitation hardened grades, use the special stress values for welded construction given in the table.

(34) After use above the temperature indicated by a single bar (|), use at a lower temperature shall be based on the stress values allowed for the annealed condition of the material.

(35) These steels are intended for use at high temperatures; however, they may have low ductility and/or low impact properties at room temperature after being used above the temperature indicated by the single bar (|).

(36) The specification permits this material to be furnished without solution heat treatment or with other than a solution heat treatment. When the material has not been solution heat-treated, the minimum temperature shall be - 20°F (- 29°C) unless the material is impact tested per 323.3.
(37) Impact requirements for seamless fittings shall be governed by those listed in this table for the particular basic material

A 276 materials are used in the manufacture of these fittings, the notes, minimum temperatures, and allowable stresses for comparable grades of A 240 materials shall apply.

(38) For use at temperatures below - 20°F through - 50°F (- 29°C through - 45°C), this material must be quenched and tempered.
(39) This material when used below - 20°F (- 29°C) requires impact testing if the carbon conten

(40) The stress values for austenitic stainless steels in this table may not be applicable if the material has been given a final heat treatment other than that required by the material specification and

any overriding requirements of this Code called for by note (30) or (31). (41) Design stresses for the cold-drawn temper are based on hot-rolled properties until required data on cold-drawn are submitted.

(42) This is a product specification. No design stresses are necessary. Limitations on metal temperature for materials covered by this specification are:

(43)* The stress values given for this material are not applicable when either welding or thermal cutting is employed [see 323.4.2(c)].

(44) This material shall not be welded.

(45) Stress values shown are applicable for ''die'' forgings only.
(46) The letter ''a'' indicates alloys which are not recommended for welding and which, if welded, must be individually qualified. The letter ''b'' indicat individually qualified.

(47) If no welding is employed in fabrication of piping from these materials, the stress values may be increased to 33.3 ksi (230 MPa).
(48) The stress value to be used for this gray cast iron material at its upper tempera

(51) Special P-numbers SP-1, SP-2, and SP-3 of carbon steels are not included in P no. 1 because of possible high-carbon, high-manganese combination which would require special consideration in

qualification. Qualification of any high carbon, high manganese grade may be extended to other grades in its group.
(52) Copper-silicon alloys are not always suitable when exposed to certain media and high temperature, par satisfactory for the service for which it is to be used.

(53) Stress relief heat treatment is required for service above 450°F (232°C).

Table 8.7.15 Basic Allowable Stresses in Tension for Metals (*Continued***)**

(54) The maximum operating temperature is arbitrarily set at 500°F (260°C) because harder temper adversely affects design stress in the creep rupture temperature ranges.
(55) Pipe produced to this specification is not inte normalized, or normalized and tempered condition.

(56) Because of thermal instability, this material is not recommended for service above 800°F (425°C).
(57)* Conversion of carbides to graphite may occur after prolonged exposure to temperatures over 800°F (425°C) (see App

(58)* Conversion of carbides to graphite may occur after prolonged exposure to temperatures over 875°F (468°C) (see App. F).
(59)* For temperatures above 900°F (480°C), consider the advantages of killed steel (see App. F)

across, prepared by removing threads. No more material than necessary shall be removed to prepare the area. Hardness determination shall be made at the same frequency as tensile tests.

(63) Annealed at approximately 1,800

(65) The minimum temperature shown is for the heaviest wall permissible by the specification. The minimum temperature for lighter walls shall be as shown in the following tabulation:

Temp. for plate thicknesses shown $Spec.$ $^{\circ}F$ $^{\circ}C$ and $^{\circ}C$ grade 1 in max 2 in max Over 2 to 3 in 25 mm max 50 mm max Over 50 to 76 mm A 203, A -90 -90 -75 -68 -68 -60 A 203, B -90 -90 -75 -68 -68 -60 A 203, D -150 -150 -125 -101 -101 -87 A 203, E -150 -150 -125 -101 -101 -87

(66) Stress values shown are 90% of those for the corresponding core material.

67) For use under this Code, the heat treatment requirements for pipe manufactured to ASTM A 671, A 672, and A 691 shall be as required by 331 for the particular material being used. In some
cases, 331 does not require hea required by the plate thickness or by the engineering design, the designation shall be class 23 (no radiography) or class 22 (100% radiography).

(68) The tension test specimen from plate 0.500 in (12.7 mm) and thicker is machined from the core and does not include the cladding alloy; therefore, the stress values listed are those for materials less than 0.500 in (12

Table 8.7.17 Basic Quality Factors for Longitudinal Weld Joints in Pipes, Tubes, and Fittings, *Ej*

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* See Notes at end o[f Table 8.7.15.](#page-169-0)

SOURCE: Abstracted from ASME B31.3 (1984) with permission

hammer allowance in case of cast-iron conveying liquids); $D = OD$ of pipe, in; $S =$ maximum allowable stress in material due to internal pressure, lb/in²; $E =$ quality factor, $y =$ a coefficient, values for which are listed in Table 8.7.18; $A =$ allowance for threading, mechanical strength, and corrosion, in, with values of *A* listed in Table 8.7.19.

The thickness of ductile-iron pipe conveying liquid may be taken fro[m Table 8.7.24](#page-187-0), using the pressure class next higher than the maximum internal service pressure in pounds per square inch. Where

Table 8.7.18 Values of *y*

(Interpolate for intermediate values) (ASME B31.1)

Table 8.7.19 Values of *A*

ductile-iron pipe is used for steam service, the thickness should be calculated by Eq. (8.7.1).

Plain-end pipe includes pipe joined by flared compression couplings, lapped joints, and by welding, i.e., by any method that does not reduce the wall thickness of the pipe at the joint.

Physical and Chemical Properties of Pipes, Tubes, etc. The design of piping for operation above 750°F (399°C) presents many problems not encountered at lower temperatures. For the properties of steel applicable to high-temperature service (as well as to ordinary service) for pipes, tubes, fittings, bolting material, etc., see Sec. 6. For a discussion of creep properties, see Sec. 5.

Piping of thickness designed in accordance with Eq. (8.7.1) may be used for any combination of pressure and temperature for which *S* and *E* values are listed in [Tables 8.7.15](#page-169-0) to 8.7.17. The following summarizes piping industry practice.

Steam Pressures above 250 lb/in2 (1,724 kPa), and Not above 2,500 lb/in2 (17,238 kPa), Temperatures Not above 1,100°F (593°C) For pressures in excess of 100 lb/in2 (690 kPa), the pipe may be seamless steel (A106), (A312), (A335), or (A376); or electric-fusionwelded steel (A691); or forged-and-bored steel (A369); or automaticwelded steel (A312). For pressures between 250 and 600 lb/in2 $(9,224 \text{ and } 22,137 \text{ N/m}^2)$ the pipe may be seamless steel $(A106)$ or (A53); electric-fusion-welded steel (A155); electric-resistancewelded steel (A135) or (A53). For pressures of 250 lb/in2 (1,724 kPa) and lower and for service up to 750°F (399°C), any of the following may be used: electric-fusion-welded steel (A134) or (A139); electricresistance-welded steel (A135); seamless or welded steel (A53). Grade A seamless pipe (A106) or (A53); or grade A electric-welded pipe (A53), (A135), or (A139) is used for close coiling or cold bending. Pipe permissible for services specified may be used for temperatures higher than 750°F (399°C), unless otherwise prohibited, if the *S* and *E* values o[f Tables 8.7.15](#page-169-0) to 8.7.17 are used when calculating the required wall thickness.

Because of several failures in seam-welded 11⁄4% Cr–1⁄2% Mo or 21⁄4% Cr–1% Mo piping produced to ASTM Specification A155 operating at temperatures above 950°F, a preference has developed for seamless piping in these applications. Nevertheless, in general, seamwelded piping has provided entirely satisfactory service in high-temperature applications above 950°F.

Valves and fittings must have flange openings or welded ends, and valves must have external stem threads. Valves must be of cast or forged steel or may be fabricated from plate and pipe. Valves of nonferrous materials are generally cast or forged. Forged and caststeel threaded valves and fittings may be used up to 300 lb/in2 and 500°F for 3 (2) [11⁄2] in pipe, and pressure from 250 to 400 (400 to 600) [600 to 2,500] lb/in2. Malleable-iron threaded fittings (300 lb/in2) may be used for pressures not greater than 300 lb/in2 and temperatures not over 500°F. Valves 8 in and larger should have the bypass of at least 3⁄4 in, commercial size.* Welded fittings may be used of the same material and thickness as the pipe to which they are to be connected.

Steam Pressures from 125 to 250 lb/in2 (862 to 1,724 kPa), Temperature Not above 450°F (232°C) Pipe may be electric-fusion-welded steel (A134 or A139). Copper and brass may be used if the temperature does not exceed 406°F. Cast iron may also be used. For close coiling or cold bending, grade A seamless steel (A53); or grade A electric-welded steel (A53), (A135), or (A139) is suitable. Pipe permissible for this service may be used for temperatures above 450°F (232°C) if the proper *S* and *E* are used in calculating the pipe-wall thickness.

Valves below 3 in may have inside stem screws. Stop valves 8 in and over must be bypassed. Bodies, bonnets, and yokes are of cast iron, malleable iron, steel, bronze, brass, or Monel. Flanged-steel fittings must conform to the class 300 ANSI Standard B16.5; if of cast iron, to the class 250 ANSI Standard B16.1; or, for threaded fittings, to the ANSI Standard B16.4. Malleable-iron threaded fittings must conform to the class 300 ANSI B16.3 standard, except that the class 150

* See Manufacturers Standardization Society SP-45 for recommended size of bypass valves.

ANSI Standard B16.3 may be used for pressures not greater than 150 lb/in2. Welded fittings may be used.

Steam Pressures from 25 to 125 lb/in2 (172 to 802 kPa) Temperatures Not above 450°F Pipe may be of steel, ductile iron, copper, or brass; valve bodies of cast iron, malleable iron, ductile iron, steel, or brass. Fittings are of class 125 or class 150 American Standard cast iron with screwed or flanged ends, or of ductile or malleable iron with screwed ends.

Steam Pressures 25 lb/in2 (172 kPa) and Less, Temperature up to 450°F Pipe may be of steel, brass, copper, or cast iron. Flanged fittings conform to the class 25 ANSI Standard B16.1. Screwed fittings are of the class 125 ANSI Standard B16.4 or of the class 150 ANSI Standard B16.3 for malleable iron, or conform to B16.15 for cast bronze. Welded-steel fittings are extensively used.

Pipe coils are made from any of the commercial sizes of iron, steel, brass, and copper pipe and tubing. Limiting center-to-center dimensions, to which pipe coils can be fabricated in sizes 3⁄4 to 2 in, are given in Table 8.7.20. Steel tubing cannot be bent to the absolute limits of brass or copper.

Seamless mechanical tubing is obtainable in outside diameters ranging from $\frac{1}{4}$ to 10 $\frac{3}{4}$ in and in wall thickness from 20 gage to 2 in (0.091 to 5.08 cm). Oval, square, rectangular, and other special shapes can be obtained in various sizes and wall thicknesses. Mechanical tubing is available either hot-finished or cold-drawn, but is furnished principally cold-drawn. It is readily adaptable to varied treatment by expansion, cupping, tapering, swaging, flanging, coiling, welding, and similar manipulations. Typical of the many uses are aircraft tubing, automobile axle housings, driveshafts, drive-shaft housings, tie rods, steering columns, piston rods and pins, gear rings, roller-bearing cases and cones, cylinders for various purposes, machine parts, sleeves, bushings, spacers, surgical instruments, and hypodermic needles. [Table 8.7.21](#page-185-0) lists weights and dimensions of round seamless-steel tubing for sizes that have by common usage become standard. Detailed information on mechanical tubing for any particular applications can be obtained from manufacturers.

Dimensions and weights of **condenser** and **heat-exchanger tubes** are given i[n Table 8.7.22](#page-185-0) and of **boiler** tubes in [Table 8.7.23.](#page-186-0)

Spiral Pipe Spiral pipe is strong lightweight steel pipe with a single continuous welded helical seam from end to end stiffening it throughout. It is listed in sizes 6- to 42-in ID (15.24- to 106.7-cm), in various thicknesses, and in lengths up to 40 ft (12.19 m). It is used for high- and low-pressure water lines, vacuum lines, exhaust-steam lines, low-pressure air lines, sand and gravel slurry conveying and similar services. It is also used extensively by the petroleum industry, for oil and gas lines, for low-pressure steam lines, etc.

Spiral pipe may be asphalt-coated or galvanized. The pipe is designed for special joints, flanges, and lightweight fittings, but the ANSI flanges and fittings can be furnished, if desired.

The **sleeve-type coupling** illustrated i[n Fig. 8.7.1](#page-186-0) is particularly suitable for plain-end pipe and is widely used. A gasket is used to make a tight joint. Advantages of this coupling are low cost, the use of unskilled labor in making the connections, and the fact that small changes in alignment and grade can be made with regular straight lengths of pipe by a movement in the coupling. This type of coupling is used extensively in long oil lines.

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Table 8.7.21 Approx Weight of Round Seamless Cold-Finished Carbon-Steel Mechanical Tubing, Ib/ft*
(Carbon 0.25% max. Standard sizes for warehouse stocks random lengths. United States Steel Corporation)

* Other standard sizes, in certain standard wall thicknesses, vary by 1⁄8-in increments for 21/2 to 31/2 in; by 1/4-in increments from 31/2 to 71/2 in; 1/2-in increments from 71/2 to 101/2 in OD. There are also standard sizes for every $\frac{1}{16}$ in from $\frac{3}{8}$ to $\frac{15}{8}$ in OD.

To obtain weights in kg/m, multiply tabular values shown by 1.42.

Table 8.7.22 Steel Condenser and Heat-Exchanger Tubes (Dimensions and weights. United States Steel Corporation)

* Multiply values shown by 0.0645 to obtain areas in cm2. † Multiply values shown by 1.42 to obtain weights in kg/m.

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* Multiply values shown by 1.42 to obtain weights in kg/m.

SOURCE: United States Steel Corporation.

Fig. 8.7.1 Sleeve type, plain end coupling.

CAST-IRON AND DUCTILE-IRON PIPE

Cast-iron pipe was extensively produced since before the turn of the century until approximately 1960. Even though cast-iron pipe generally has given excellent service, the manufacture of cast-iron pipe was discontinued at that time.

Since then, **ductile-iron pipe** has replaced cast-iron pipe because of its improved ductility. Ductile-iron pipe is now extensively utilized for water, gas, sewage, culverts, drains, etc. It is produced in a wide range of sizes for varying pressures. Ductile-iron pipe is particularly adaptable to underground and submerged service because of its comparatively superior corrosion resistance compared to steel pipe. Nevertheless, steel pipe, when properly coated and wrapped, can also provide adequate resistance to corrosion when placed in certain soils.

Pipe fittings are available as cast-iron pipe fittings and ductile-iron pipe fittings. Both types of fittings are used with ductile-iron pipe.

Ductile-iron pipe may be obtained in various thicknesses and weights with (1) flanges cast on, (2) ends threaded for screwed-on flanges, (3) ends prepared for mechanical joint, (4) ends grooved or shouldered for patented coupling, (5) one end bell, other end spigot, and (6) one end hub, other end spigot. **Bell-and-spigot** ends are most popular for underground work; hub-and-spigot ends are most frequently used for sewage systems in enclosed spaces. Spigot-end joints are prepared by tightly tamping in hemp or jute at the bottom of the recess with a yarning iron and then pouring in molten lead; the lead, when cooled, is caulked in tightly with a caulking iron and makes a gastight joint. For exposed piping, flanged ends are used, the joints being made up with gaskets. Flanged pipe has superior strength and tightness of the joint and is used where pipelines can be well supported. The bell-and-spigot joint possesses greater flexibility and provides for expansion and contraction. It is therefore suitable for water pipe and is largely used for that purpose.

Figure 8.7.2 shows a typical form of this joint for ordinary pressures. Figure 8.7.3 shows one form of this joint for ordinary pressures. Figure 8.7.3 shows one form of **mechanical joint** suitable for water, gas, or oil. Other forms of joint, plain-end pipe with couplings, and threaded pipe also are manufactured. Cast-iron and ductile-iron pipe, fittings, and valves have been found unsuitable for superheated steam service. The Code for Pressure Piping, B31.1 (Power Piping), states that cast iron or ductile-iron pipe may be used for steam service not over 250 lb/in2 or 406°F (1,724 kPa or 208°C) provided that it meets the requirements as dictated by Eq. (8.7.1).

Fig. 8.7.2 Standard bell-andspigot joint.

Fig. 8.7.3 Mechanical joint.

Wall thicknesses for the various conditions which ductile-iron pipe is designed to meet are determined in accordance with the requirements of ANSI 21.50 (AWWA C150).

Ductile-iron pipe is made by **centrifugal casting,** in which molten iron is admitted to the interior of a sand-lined or metal-lined mold, the mold being rotated at high speeds so that the molten metal is thrown by centrifugal force against the lining. ANSI specifications have been prepared for the various combinations of fabrication procedure and intended end use.

[Table 8.7.24](#page-187-0) lists thicknesses and weight data for centrifugally cast ductile-iron pipe intended for use with water or other liquids.

The employment of ductile-iron pipe for gas supply and distribution is second in importance only to its use for carrying water. Bell-andspigot gas pipe is similar in design to bell-and-spigot water pipe (Fig. 8.7.2). For flanged gas pipe, the class 25 ANSI B16.1 Standard flanges are approved for maximum gas pressures of 25 lb/in2 (172 kPa). The class 125 ANSI B16.1 Standard flanges are approved for gas pressures of 125 lb/in2 (862 kPa), up to 4 in nominal pipe size; 100 lb/in2 (689 kPa), 6 to 12 in; and 80 lb/in² (552 kPa), 16 to 48 in. The type of joint shown in Fig. 8.7.2 is also widely used for gas.

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Pipe weights indicated are approximate and include allowance for bell based on a 16-ft laying length. Calculations are for pipe laid without blocks, on flat-bottom trench, with tamped backfill under
5 ft of cover. Thicknes

manufacturers.

To obtain weights in kg/m, multiply values shown in lb per avg ft by 1.42. SOURCE: Condensed from Table 8.2 of Specification AWWA C 108-70.

Flexible-Joint Pipe The necessity for crossing streams and other waterways and of laying pipelines into them has led to the development of various forms of flexible-joint pipe adapted to laying under water, which are capable of motion through several degrees without leakage. Figure 8.7.4 shows one style of such joint which has an adjustment of about 15° in standard sizes.

Fig. 8.7.4 Flexible joint. (See Table 8.7.25 for dimensions.)

In selecting the thickness of a pipe for a submerged line, the internalservice pressure is seldom the determining factor, as ample allowance should be made to minimize the risk of breakage in laying and to with-

* United States Pipe and Foundry Co.

† Weights do not include follower rings, bolts, or gaskets. For sizes above 12 in, see manufacturers' catalogs. Multiply weights shown by 38.7 to obtain weight in kg per m or by 0.4536 to obtain weight in kg per 12-ft length.

stand external shocks from floating ice or other objects. The dimensions and weights given in Table 8.7.25 are typical of those listed by several

''Universal'' pipe (Fig. 8.7.5) is ductile-iron pipe with hub-and-spigot ends, the contact surfaces of which are machined on a taper, giving an iron-to-iron joint, By making the tapers of slightly different pitch, the joint provides for flexibility while remaining tight. Two bolts to the

Fig. 8.7.5 Universal ductile-iron pipe and joint.

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* Multiply wts. by 0.4536 to obtain wt. in kilograms.

joint are sufficient, except for pressures above 175 lb/in2 (1,207 kPa). Universal ductile-iron pipe is used largely for carrying gas and water and is suitable for all pressures and services. The pipe is tested with hydrostatic pressure of 300 to 500 lb/in² (2,067 to $3,448$ kPa). All universal pipe and special castings of a given diameter and of any class are interchangeable with those of a different class. Standard laying lengths are 6 ft (1.83 m). Thicknesses and weights of standard types up to 16 in are given in Table 8.7.26. Information on other types and sizes and on fittings may be obtained from pipe producers.

Fittings for Ductile-Iron Water Pipe Flanged fittings of the dimensions of the ANSI standard for steam are not often used with ductileiron water pipe. The longer fittings of the AWWA are generally preferred because of low friction loss. The dimensions of the flanged fittings of this class conform very closely to the dimensions of the bell-and-spigot fittings of the AWWA. The flange thicknesses and drillings conform to those of the ANSI standards. These fittings, both flange and bell-and-spigot type, are made in a great variety of forms known as ''standard special fittings.'' For dimensions and weights, see manufacturers' catalogs or standard specifications of the AWWA.

Cast-iron soil pipe and fittings are of the hub-and-spigot form, similar in design to the pipe shown in [Fig. 8.7.2.](#page-186-0) Tapped openings and pipe plugs are threaded in accordance with the taper pipe thread requirements of ANSI B1.20.1-1983.

The ANSI standard, Threaded Cast-Iron Pipe for Drainage, Vent, and Waste Services, ANSI A40.5-1943, covers two types of pipes having threaded joints in nominal pipe sizes $1\frac{1}{4}$ to 12 in and in lengths 5 to 27 ft. One type has external threads on both ends; the other type has external threads on one end and an internal threaded drainage hub on the other end.

PIPES AND TUBES OF NONFERROUS MATERIALS

Brass tubing is commercially available in the form known as yellow brass, an alloy consisting of approximately 65 percent copper and 35

* The values in the table above are based on the formula in The Code for Pressure Piping, ANSI B31:

$$
t_m = \frac{PD}{2S + 0.8P} + C \qquad \text{or when } C \text{ is } O \qquad P = \frac{2St_m}{D - 0.8t_m}
$$

where t_m = minimum pipe wall thickness, in; P = maximum rated internal working pressure, lb/in²; D = outside diameter of pipe, in; S = allowable stress in material due to internal pressure, at operating temperature, lb/in²; $C =$ allowance for threading, mechanical strength and/or corrosion, in. The allowable internal pressures apply to the pipe itself after brazing. SOURCE: Copper Development Association.

| | Pipe with threaded ends | | | | | | | Pipe with plain ends for use with welded, brazed, or soldered fittings | | | | | | | | |
|----------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|--|--------------------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|
| | | | Red brass | | | | Copper | | Red brass | | | Copper | | | | |
| Standard size, in | 100° F $S = 8,000$ | 200° F $S = 8,000$ | 300° F $S = 8,000$ | 400° F $S = 5,000$ | 100° F $S = 6,000$ | 200° F $S = 4,800$ | 300° F $S = 4,700$ | 400° F $S = 3,000$ | 100° F $S = 8,000$ | 200° F $S = 8,000$ | 300° F $S = 8,000$ | 400° F $S = 5,000$ | 100° F $S = 6,000$ | 200° F $S = 4,800$ | 300° F $S = 4,700$ | 400° F $S = 3,000$ |
| | | | | | | | | Regular | | | | | | | | |
| $1\!/\!s$ | 370 | 370 | 370 | 230 | 280 | 210 | 210 | 130 | 2,640 | 2,640 | 2,640 | 1,650 | 1,980 | 1,570 | 1,540 | 980 |
| $\frac{1}{4}$ | 870 | 870 | 870 | 550 | 650 | 510 | 510 | 320 | 2,610 | 2,610 | 2,610 | 1,640 | 1,960 | 1,560 | 1,530 | 970 |
| $\frac{3}{8}$ | 890 | 890 | 890 | 570 | 670 | 530 | 510 | 320 | 2,280 | 2,280 | 2,280 | 1,440 | 1,710 | 1,350 | 1,330 | 840 |
| $\frac{1}{2}$ | 900 | 900 | 900 | 570 | 670 | 530 | 520 | 320 | 2,160 | 2,160 | 2,160 | 1,350 | 1,620 | 1,280 | 1,260 | 800 |
| $^{3}/_{4}$ | 810 | 810 | 810 | 520 | 610 | 480 | 470 | 300 | 1,800 | 1,800 | 1,800 | 1,130 | 1,350 | 1,070 | 1,050 | 670 |
| | 630 | 630 | 630 | 400 | 480 | 370 | 370 | 230 | 1,580 | 1,580 | 1,580 | 1,000 | 1,190 | 940 | 920 | 590 |
| $1\frac{1}{4}$ | 690 | 690 | 690 | 430 | 520 | 410 | 400 | 250 | 1,440 | 1,440 | 1,440 | 900 | 1,080 | 890 | 840 | 530 |
| $1\frac{1}{2}$ | 630 | 630 | 630 | 400 | 480 | 370 | 370 | 230 | 1,280 | 1,280 | 1,280 | 800 | 960 | 750 | 740 | 470 |
| \overline{c} | 540 | 540 | 540 | 350 | 410 | 320 | 310 | 190 | 1,050 | 1,050 | 1,050 | 670 | 790 | 620 | 610 | 380 |
| $2\frac{1}{2}$ | 450 | 450 | 450 | 280 | 340 | 260 | 250 | 160 | 1,040 | 1,040 | 1,040 | 650 | 780 | 620 | 610 | 380 |
| 3 | 510 | 510 | 510 | 320 | 380 | 300 | 290 | 180 | 1,000 | 1.000 | 1.000 | 630 | 750 | 590 | 580 | 370 |
| $3\frac{1}{2}$ | 570 | 570 | 570 | 370 | 430 | 330 | 330 | 200 | 1,000 | 1,000 | 1,000 | 630 | 750 | 590 | 580 | 370 |
| $\overline{4}$ | 510 | 510 | 510 | 320 | 380 | 300 | 290 | 180 | 880 | 880 | 880 | 550 | 660 | 530 | 520 | 320 |
| 5 | 410 | 410 | 410 | 270 | 310 | 230 | 240 | 140 | 710 | 710 | 710 | 450 | 540 | 420 | 410 | 260 |
| 6 | 340 | 340 | 340 | 220 | 260 | 190 | 200 | 120 | 600 | 600 | 600 | 380 | 450 | 350 | 340 | 220 |
| 8 | 360 | 360 | 360 | 230 | 270 | 270 | 210 | 130 | 560 | 560 | 560 | 350 | 420 | 320 | 320 | 200 |
| 10 | 360 | 360 | 360 | 230 | 270 | 210 | 210 | 130 | 520 | 520 | 520 | 330 | 390 | 300 | 300 | 190 |
| 12 | 320 | 320 | 320 | 200 | 240 | 190 | 200 | 120 | 450 | 450 | 450 | 280 | 340 | 260 | 250 | 160 |
| | | | | | | | | Extra-Strong | | | | | | | | |
| $1\!/\!s$ | 1,960 | 1,960 | 1,960 | 1,240 | 1,470 | 1,160 | 1,140 | 720 | 4,630 | 4,630 | 4,630 | 2,900 | 3,470 | 2,750 | 2,710 | 1,730 |
| $\frac{1}{4}$ | 2,210 | 2,210 | 2,210 | 1,340 | 1,660 | 1,310 | 1,290 | 820 | 4,200 | 4,200 | 4,200 | 2,640 | 3,150 | 2,500 | 2,460 | 1,570 |
| $\frac{3}{8}$ | 1,840 | 1,840 | 1,840 | 1,150 | 1,380 | 1,090 | 1,070 | 680 | 3,360 | 3,360 | 3,360 | 2,100 | 2,520 | 2,000 | 1,960 | 1,250 |
| $1/2$ | 1,760 | 1.760 | 1.760 | 1.100 | 1.320 | 1.040 | 1,030 | 660 | 3,130 | 3,130 | 3,130 | 1,970 | 2,350 | 1.860 | 1,830 | 1,160 |
| $^{3}/_{4}$ | 1,510 | 1,510 | 1,510 | 950 | 1,130 | 900 | 880 | 560 | 2,560 | 2,560 | 2,560 | 1,600 | 1,920 | 1,520 | 1,500 | 960 |
| | 1,340 | 1,340 | 1,340 | 850 | 1,010 | 790 | 780 | 490 | 2,360 | 2,360 | 2,360 | 1,490 | 1,770 | 1,400 | 1,370 | 880 |
| $1\frac{1}{4}$ | 1,160 | 1,160 | 1,160 | 730 | 880 | 730 | 680 | 430 | 1,950 | 1,950 | 1,950 | 1,220 | 1,460 | 1,160 | 1,140 | 720 |
| $1\frac{1}{2}$ | 1.090 | 1,090 | 1,090 | 680 | 820 | 660 | 640 | 410 | 1,770 | 1,770 | 1,770 | 1,120 | 1,330 | 1,050 | 1,030 | 660 |
| \overline{c} | 1,000 | 1,000 | 1,000 | 630 | 750 | 590 | 570 | 360 | 1,520 | 1,520 | 1,520 | 950 | 1,140 | 910 | 890 | 560 |
| $2\frac{1}{2}$ | 970 | 970 | 970 | 620 | 730 | 580 | 560 | 360 | 1,600 | 1,600 | 1,600 | 1,000 | 1,200 | 950 | 930 | 590 |
| $\overline{3}$ | 910 | 910 | 910 | 570 | 680 | 530 | 530 | 340 | 1,420 | 1,420 | 1,420 | 900 | 1,070 | 840 | 830 | 530 |
| $3\frac{1}{2}$ | 860 | 860 | 860 | 550 | 650 | 510 | 500 | 310 | 1,300 | 1,300 | 1,300 | 820 | 980 | 790 | 760 | 480 |
| 4 | 840 | 840 | 840 | 530 | 630 | 490 | 480 | 300 | 1,230 | 1,230 | 1,230 | 770 | 920 | 730 | 710 | 460 |
| 5 | 770 | 770 | 770 | 480 | 580 | 450 | 440 | 340 | 1,080 | 1,080 | 1,080 | 680 | 810 | 640 | 630 | 400 |
| 6 | 800 | 800 | 800 | 500 | 600 | 470 | 460 | 290 | 1,060 | 1,060 | 1,060 | 670 | 800 | 620 | 610 | 380 |
| 8 | 710 | 710 | 710 | 450 | 530 | 430 | 410 | 260 | 910 | 910 | 910 | 570 | 680 | 540 | 540 | 340 |
| 10 | 550 | 550 | 550 | 350 | 420 | 340 | 330 | 200 | 710 | 710 | 710 | 450 | 540 | 440 | 420 | 240 |

Table 8.7.28 Allowable Internal Pressures, Ib/in², for Temperatures up to 400°F for Red Brass and Copper Pipe*

* The values above are based on the formula in The Code for Pressure Piping, ANSI B31:

$$
t_m = \frac{PD}{2S + 0.8P} + C
$$
 or $P = \frac{2S(t_m - C)}{D - 0.8(t_m - C)}$ or when C is O $P = \frac{2St_m}{D - 0.8t_m}$

SOURCE: Copper Development Association.

where t_m = minimum pipe wall thickness, in; P = maximum rated internal working pressure, lb/in²; D = outside diameter of pipe, in; S = allowable stress in annealed material due to internal pressure, at operating limitations which may be imposed by the type of joint and the joining material.

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percent zinc, and is used principally for ornamental work and hand railings, It has a density of approximately 0.3 lb/in³ (8.31 g/cm³), the exact density being dependent upon the specific chemical composition. **Brass piping** is most frequently furnished as red brass, an alloy consisting of approximately 85 percent copper and 15 percent zinc. This alloy, having a density of about 0.32 lb/in³ (8.86 g/cm³), has been found to be structurally superior to the yellow brasses and is used where the fluid being conveyed has corrosive properties.

Copper is available either as pipe or as tubing. In the form of piping, it has the same outer diameter as that of standard steel pipe [\(Tables 8.7.27](#page-188-0) and 8.7.28). As tubing, it is used for a variety of purposes, such as for compressed-air instrumentation lines, hydraulic control lines around machinery, domestic oil-burner and heating systems, and for general plumbing purposes. **Copper tubing** (Table 8.7.29) is furnished in 12-ft (3.7-m) and 20-ft (6.1-m) straight lengths or in coils of 100-ft (30.5-m) length. **Type K** tubing, in coils, is used for underground work where the minimum number of joints, combined with greater thickness of type K tubing, is of distinct advantage. **Type L** tubing, usually in straight lengths, is used as a principal piping material for plumbing systems in homes and buildings; this is largely due to the economy of installation made possible by the use of soldered fittings. Copper deteriorates rapidly under high temperatures and repeated stresses. At a temperature of 360°F (182°C) its strength is reduced 15 percent, and on this account it should never be used for high steam pressures and temperatures.

Commercial sizes of **aluminum tubing** are listed by the manufacturers in even outside diameters and in wall thicknesses conforming to Stubs gage. Aluminum pipe is available as listed i[n Table 8.7.30.](#page-191-0) To obtain the approximate weight per foot of aluminum pipe or tubing, a weight of 0.098 lb/in³ (2.71 g/cm³) may be used.

Lead pipe is supplied in straight lengths, in coils, or in reels.

Block tin is a term used in the metal trade to refer to products made wholly from strictly pure high-grade tin. While tin pipe has many and varied uses, its most important applications are in types of equipment handling liquids intended for human consumption. Tin pipe does not corrode, and therefore does not contaminate most of the liquids passing through it.

Plastic pipes and **tubes** are available in a wide range of diameters and thicknesses, with [Table 8.7.31](#page-192-0) generally representative. The plastic used is resistant to attack by many chemicals, light in weight, flexible, and available in coiled form so that installation time is low. It is used for a variety of purposes including drainage, irrigation, sewage, and for conveying chemical solutions or waters that would attack metal piping.

Table 8.7.29 Sizes and Weights of Copper Tubes

Plastic pipe used in gas service is listed in [Table 8.7.32.](#page-192-0) Caution should be used in selection of plastic piping insofar as service temperature is concerned: e.g., polyethylene is suitable for a maximum temperature of 120°F (49°C[\). Table 8.7.3](#page-193-0)3 lists corrosion-resistance data for polyethylene plastic piping.

Pipes with Special Linings For use in lines through which are passed solutions containing more or less free acid or other corrosive agents, standard pipe, valves, and fittings may be **lead-lined, tin-lined,** or **rubber-lined,** to resist corrosive action. This lining prolongs the life of the pipe and also gives it additional strength. For mine service in coal districts where the drainage water is more or less impregnated with sulfur or free sulfuric acid, **wood-lined pipe** and fittings are sometimes used. For special service, **seamless-copper-lined pipe** is also used. The **cement lining** of ductile-iron and steel pipe for water and other services is advantageous because of its protection against unusual destructive agencies and its ability to prevent tuberculation. Standard **hard-rubber pipe** and fittings have been developed for working pressures of 50 lb/in2 (345 kPa) at normal temperatures. Standard sizes run from 1⁄4- to 4-in diam (0.635- to 10.2-cm), in 10-ft (3.05-m) lengths. For temperature above 120°F (49°C), the use of hard-rubber-lined steel pipe is recommended. This pipe is suitable for conveying strong acids and chemicals.

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Vitrified pipe is used extensively for drains and sewerage systems. Burnt-clay tile, being rendered impervious to water by glazing, is by far the best material for sewage purposes as it is not attacked by acids. Dimensions are given i[n Table 8.7.34](#page-193-0) (see als[o Fig. 8.7.6\)](#page-192-0). For sizes larger than 36 in (91.4 cm) and other data, refer to the publications of the Clay Products Assoc., Chicago (see ASTM Standard C-700).

Wood-stave pipe [\(Fig. 8.7.7\)](#page-194-0) is used to a large extent for municipal water supply, outfall sewers, mining, irrigation, and various other uses providing for the transportation of water. The water carried may be hot, cold, or acid. It is made either untreated or creosoted by a vacuum and pressure process. This process uses 8 lb of creosote per cubic foot of wood treated. The untreated pipe is most used where the pipe is constantly full of water, and the wood therefore completely saturated, although in many such instances the creosoted wood is used to give assurance of permanence. (See also Sec. 6.)

Wood-stave pipe is made in two types: machine-banded pipe and continuous-stave pipe. **Machine-banded pipe** is banded with wire and is

* Type K recommended for underground service and general plumbing. Type L suitable for interior plumbing and other services.

† Multiply these values by 1.48 to obtain weight in kg/m.

SOURCE: American Brass Co.

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Table 8.7.30 Aluminum Piping

* Aluminum Co. of America.
† Weights calculated for 6061 and 6063. For 3003 multiply by 1.010.
‡ Also designated as standard pipe.
§ Also designated as extra-heavy or extra-strong pipe. All calculations based on nominal di

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| Nominal | | Wall thickness,* | OD, | ID, | Theoretical weight,† | Calculated min bursting pressure, $1b/in^2$ | | |
|----------------|----------|---------------------|-------|-------|-------------------------|---|--------|--|
| size, in | Schedule | in | in | in | 1 _b /ft | Note 1 | Note 2 | |
| $\frac{1}{4}$ | 40 | 0.088 | 0.540 | 0.364 | 0.076 | 2,490 | 1,950 | |
| | 80 | 0.119 | 0.540 | 0.302 | 0.096 | 3,620 | 2,830 | |
| $\frac{1}{2}$ | 40 | 0.109 | 0.840 | 0.622 | 0.153 | 1,910 | 1,490 | |
| | 80 | 0.147 | 0.840 | 0.546 | 0.185 | 2,720 | 2,120 | |
| $^{3}/_{4}$ | 40 | 0.113 | 1.050 | 0.824 | 0.203 | 1,540 | 1,210 | |
| | 80 | 0.154 | 1.050 | 0.742 | 0.265 | 2,200 | 1,720 | |
| 1 | 40 | 0.133 | 1.315 | 1.049 | 0.305 | 1,440 | 1,130 | |
| | 80 | 0.179 | 1.315 | 0.957 | 0.385 | 2,020 | 1,580 | |
| $1\frac{1}{4}$ | 40 | 0.140 | 1.660 | 1.380 | 0.409 | 1,180 | 920 | |
| | 80 | 0.191 | 1.660 | 1.278 | 0.550 | 1,660 | 1,300 | |
| $1\frac{1}{2}$ | 40 | 0.145 | 1.900 | 1.610 | 0.489 | 1,060 | 830 | |
| | 80 | 0.200 | 1.900 | 1.500 | 0.653 | 1,510 | 1,180 | |
| \overline{c} | 40 | 0.154 | 2.375 | 2.067 | 0.640 | 890 | 690 | |
| | 80 | 0.218 | 2.375 | 1.939 | 0.910 | 1,290 | 1,010 | |
| 3 | 40 | 0.216 | 3.500 | 3.068 | 1.380 | 840 | 660 | |
| | 80 | 0.300 | 3.500 | 2.900 | 1.845 | 1,200 | 940 | |
| $\overline{4}$ | 40 | 0.237 | 4.500 | 4.026 | 1.965 | 710 | 560 | |
| | 80 | 0.337 | 4.500 | 3.826 | 2.710 | 1,040 | 810 | |

Table 8.7.31 Commerical Sizes (IPS) and Weights of Polyvinyl Chloride (PVC) Pipe*

* Thicknesses listed are minimum values. Tolerance is generally $-0 + 10\%$.

† These representative values are not specified in ASTM D1785-85.

NOTES:

1. Materials are PVC 1120, 1220, and 4116. A fiber stress of 6,400 lb/in2 was used in bursting pressure calculations.

2. Materials are PVC 2112, 2116, and 2120. A fiber stress of 5,000 lb/in2 was used in bursting pressure calculations. SOURCE: Abstracted from ASTM Specification D1785-85.

Table 8.7.32 Dimensions of Plastic Pipe for Gas Service (AGA Requirements)

| Nominal size, in | Nominal OD, in | Nominal ID, in | Sleeved weight, 1b | Max working pressure at 73° F, lb/in ² |
|---------------------|-------------------|-------------------|--------------------------|--|
| $\frac{1}{2}$ | 0.625 | 0.500 | 0.054 | 250 |
| $\frac{3}{4}$ | 0.875 | 0.750 | 0.079 | 175 |
| | 1.125 | 1.000 | 0.103 | 125 |
| $1\frac{1}{4}$ | 1.375 | 1.250 | 0.127 | 110 |
| $1\frac{1}{2}$ | 1.625 | 1.500 | 0.152 | 90 |
| $1^{3}/_{4}$ | 1.875 | 1.750 | 0.177 | 80 |
| \overline{c} | 2.125 | 2.000 | 0.200 | 75 |
| $2\frac{1}{2}$ | 2.660 | 2.500 | 0.320 | 75 |
| 3 | 3.190 | 3.000 | 0.457 | 75 |
| 4 | 4.250 | 4.000 | 0.800 | 75 |

made with wood or metal collars, or with inserted joints. **Continuousstave pipe** is manufactured in units consisting of staves, bands, and shoes, shipped in knocked-down form, and constructed in the trench. In building this type of pipe, the staves are laid so as to break joints and the completed pipe is without joints. Continuous-stave pipe is banded with individual bands, ranging in size from 3⁄8 to 1 in (0.95 to 2.54 cm), depending upon the size of the pipe. A factor of safety of 4 is maintained in the band, based on an ultimate strength of 60,000 lb/in2 (414 MPa) of cross section. The maximum pressure to which a continuous-stave pipe may be subjected depends upon the size of the pipe. The head for small pipes may run as high as 400 ft (121.9 m) while in the largest sizes the head would be less than 200 ft (61 m).

Machine-banded pipe is made for pressures of 50 to 400 ft (15.2 to 121.9 m). The staves are made from redwood or Douglas-fir lumber, dried and carefully selected. The inside and outside of the staves are dressed to conform to the circumferential lines, and the edges of the staves dressed to conform to the radial lines.

Wooden pipe is largely built in western sections of the United States, close to the natural lumber market. The sizes of machine-banded pipe range from 2 to 24 in (5.08 to 61 cm), and of the continuous-stave pipe from 6- to 20-ft (15.2-cm to 6.1-m) inside diameter.

Pipe made from **plywood** is molded in lengths up to 11 ft (3.35 m) in diameters 3 in (7.62 cm) and up, and in wall thicknesses to specifications. Tubes made from fiber, by a molding process, are obtainable in a variety of sizes and lengths.

Concrete pipe is an important factor in sewer, conduit, railroad, culvert, and water-pipe construction. The pipe, as usually made, is constructed of concrete reinforced longitudinally with bars and transversely with wire mesh or steel bands. It is made in sections of definite length, with the longitudinal reinforcement so disposed as to provide for the interlocking of one section with another, and so formed that when these are locked together and cemented they form a continuous line of pipe free from leakage or seepage. Various forms of joints are used, all capable of taking care of expansion[. Figure 8.7.8](#page-194-0) shows one type of construction. Concrete pipe is manufactured in a great variety of diameters, thicknesses, and lengths to suit almost any requirement arising in practice. (See also Sec. 6.)

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Corrosion-resistance data given in this table based on laboratory tests conducted by the manufacturers of the materials covered, and are indicative only of the conditions under which the tests were
made. This information m $E =$ excellent, $G =$ good, $F =$ fair, $NG =$ not good.

* Polyethylene is permeable to acetic acid.

Asbestos-cement pipe, known by the trade name **Transite** pipe in this country, was developed initially in Europe. It was widely used in the United States for many years in a large variety of services. It was made of a mixture of portland cement and asbestos fiber, was highly resistant to corrosion, and provided outstanding service in mine drainage systems, waterworks systems, gas lines, and sewerage systems. It was manufactured in diameters from 3 to 36 in (7.6 to 91 cm), in stock

lengths of 13 ft (4 m), and in pressure classes of 50, 100, 150, and 200 lb/in2 (349, 689, 1,034, and 1,379 kPa). While it is no longer manufactured, it is still in place in some of the above-cited applications. Repairs to existing Transite piping generally devolves into replacing it with pipe made of a material compatible with its service, often with fiberglass-reinforced pipe, plastic pipe, or some form of metal pipe.

Table 8.7.34 Standard-Strength Vitrified Clay Pipe (Dimensions refer t[o Fig. 8.7.6\)](#page-192-0)

When ordering standard-strength vitrified-clay pipe, give the size of pipe (ID) and the laying strength wanted, and refer to ASTM Specification C-700. Standard lengths of pipe shown meet normal practice in various sections of the country. Manufacturers' stocks include those lengths conforming to local practice.

* There is no limit for plus variation.

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Fig. 8.7.7 Wood-stave pipes.

Fig. 8.7.8 Reinforced-concrete pipe.

FITTINGS FOR STEEL PIPE

American National Standard Cast-Iron Pipe Flanges and Flanged Fittings for Maximum Working Saturated Steam Pressure of 25, 125, and 250 lb/in2 (172, 862, and 1,724 kPa)

INTRODUCTORY NOTES

Sizes The sizes of the fittings in the following tables are nominal pipe sizes. In the class 25 standard, the nominal pipe size is the same as the port diameter of the fittings, for *all* sizes. In the class 125 and class 250 standards the nominal pipe size is the same as the port diameter of fittings for pipe having inside diameters of 12 in (30.5 cm) and smaller. For pipe 14 in (35.6 cm) and larger, the corresponding outside diameter of the pipe is given, and consequently the fittings will have a smaller port diameter.

Pressure Rating In the class 25 standard the sizes 36 in (91.4 cm) and smaller may also be used for maximum nonshock working hydraulic pressures of 43 lb/in² gage (296 kPa) or a maximum gas pressure of 25 lb/in2 gage (172 kPa), at or near the ordinary range of air temperatures. In the class 125 standard, the sizes 12 in (30.5 cm) and smaller may also be used for maximum nonshock working hydraulic pressure of 175 lb/in2 gage (1,207 kPa) at or near the ordinary range of air temperatures. In the class 250 standard, the sizes 12 in and smaller may be used for maximum nonshock working hydraulic pressures of 400 lb/in2 gage (2,758 kPa) at or near the ordinary range of air temperatures.

Facing All class 25 and class 125 cast-iron flanges and flanged fittings are plain faced, i.e., without projection or raised face. All class 250 cast-iron flanges and flanged fittings have a raised face $1/16$ (0.16 cm) high, of the diameters given in [Table 8.7.35.](#page-195-0) The raised face is included in the minimum flange thickness and center-to-face dimensions.

An **inspection limit** of $\pm \frac{1}{32}$ in (0.08 cm) is allowed on all center-tocontact-surface dimensions for sizes up to and including 10 in (25.4 cm) and \pm 1/8 in on sizes larger than 10 in.

Dimensions In the class 25 standard, the flange diameters, bolt circles, and number of bolts are the same as in the class 125 ANSI Standard B16.1-1975, with a reduction in the thickness of flanges and bolt diameters, thereby maintaining interchangeability between the two standards.

The center-to-face and face-to-face dimensions of class 25 standard fittings are the same as for the class 125 standard.

Bolting Drilling templates are in multiples of four, so that fittings may be made to face in any quarter. **Bolt-holes** straddle the centerline. For bolts smaller than $1\frac{3}{4}$ in (4.45 cm) the bolt-holes are drilled $\frac{1}{8}$ in larger in diameter than the nominal size of the bolt. Holes for bolts $1\frac{3}{4}$ in and larger are drilled $\frac{1}{4}$ in (0.64 cm) larger than nominal diameter of bolts. **Bolts** of steel are with standard ''rough square heads'' and the nuts are of steel with standard ''rough hexagonal'' dimensions; all as given in the American Standard on Wrench Head Bolts and Nuts and Wrench Openings of the National Screw Thread Commission. For bolts, 13⁄4-in (4.45-cm) diam and larger, bolt studs with a nut on each end are recommended.

Hexagonal nuts for pipe sizes 1 to 48 in (2.54 to 122 cm) in the class 125 standard and 1 to 16 in (40.6 cm) in the class 250 standard can be conveniently pulled up with open wrenches of minimum design of heads. Hexagonal nuts for pipe sizes 48 to 96 in (244 cm) in the class 125 standard and 18 to 48 in (45.7 to 122 cm) in the class 250 standard can be conveniently pulled up with box wrenches.

Spot Facing The bolt-holes of classes 25, 125, and 250 cast-iron flanges and flanged fittings are not spot-faced for ordinary service. When required, the flanges and fittings in sizes 30 in (76.2 cm) and larger may be spot-faced or back-faced to the minimum thickness of flange with a plus tolerance of $\frac{1}{8}$ in (0.32 cm).

Reducing Fittings Reducing elbows and side-outlet elbows carry same dimensions center to face as straight-size elbows corresponding to the size of the larger opening.

Tees, side-outlet tees, crosses, and laterals sizes 16 in (40.6 cm) and smaller, reducing on the outlet or branch, have the same dimension center to face and face to face as straight-size fittings corresponding to the size of the larger opening. Sizes 18 in (45.7 cm) and larger, reducing on the outlet or branch, are made in two lengths depending on the size of the outlet as given in the tables of dimensions.

Tees, crosses, and laterals, reducing on the run only, have the same dimensions center to face and face to face as straight-size fittings corresponding to the size of the larger opening.

Reducers and eccentric reducers for all reduction have the same faceto-face dimensions for the larger opening.

Special double-branch elbows whether straight or reducing have the same dimension center to face as straight-size elbows corresponding to the size of the larger opening.

Side-outlet elbows and side-outlet tees have all openings on intersecting centerlines.

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* To obtain linear dimensions in cm, multiply tabular values in in by 2.54. To obtain areas in cm², multiply tabular values in in² by 6.45. To obtain stress in N/m², multiply values in lb/in² by 36.895.
† The stres

25-lb standard. SOURCE: ANSI B16.1-1975.

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Elbows Special degree elbows ranging from 1 to 45° have the same center-to-face dimensions given for 45° elbows, and those over 45° and up to 90° have the same center-to-face dimensions given for 90° elbows. The angle designation of an elbow is its deflection from straight-line flow and is the angle between its flange faces.

Threaded Companion Flanges Threaded companion flanges in the class 25 standard should not be thinner than those in the class 125 standard on sizes 24 in (61 cm) and smaller. Other types of flanges may have thicknesses as given i[n Table 8.7.35.](#page-195-0)

Laterals Laterals (Y branches) both straight and reducing sizes 8 in and larger are reinforced to compensate for the inherent weakness in the casting design.

The American National Standard B16.1-1975 covers also dimensions (not included in the tables) of base elbows and base tees and anchorage bases for straight tees and reducing tees.

American National Standard cast-iron pipe flanges and flanged fittings are available for maximum nonshock working hydraulic pressure of 800 lb/in2 gage (5,516 kPa) at ordinary air temperatures.

Assembly of Flanged Joints The optimum degree of tightening occurs when a stress of 30,000 lb/in2 (207 MPa) is uniformly reached in each flange stud or bolt. For a modulus of elasticity of 30,000,000 lb/in2 (207 GPa) a stress of 30,000,000 lb/in2 occurs when the elongation, determined with a dial indicator or micrometer, is 0.001 in/in of stud length measured between centers of nuts. Uniform tension in flange bolts may also be obtained by use of a torque wrench; bearing surfaces of nuts must have a good machine finish, and threads must be properly lubricated for reliable results with a torque wrench. The following torque values have been found to give 30,000 lb/in2 stress in studs:

* Multiply by 0.149 to obtain torque in kilogram-metres.

American National Standard Steel Pipe Flanges and Flanged Fittings

INTRODUCTORY NOTES

Pressure Ratings and Tests These standards are known as ''American Class 150, 300, 400, 600, 900, 1,500, and 2,500 Steel Flange Standards'' (ANSI B16.5-1981), said pressure designation being the recommended rating at the temperatures given in [Table 8.7.35.](#page-195-0) This table shows recommended ratings for various temperatures. For other tables, refer to ANSI B16.5-1981.

Sizes The size of the fittings and companion flanges in the tables is identified by the corresponding nominal pipe size. For pipe NPS 14 (35.6 cm) and larger, the corresponding outside diameter of the pipe is given.

Materials The flanged fittings and flanges should be either steel castings or steel forgings of the grade complying with the ASTM specifications recommended under these standards for the various pressure-

* Ratings shown apply to other material groups where columns dividing lines are omitted.

† Permissible but not recommended for prolonged use above about 800°F.

§ Not to be used over 850°F

Not to be used over $1,000^{\circ}$ F

Not to be used over 1,000 T.
SOURCE: Abstracted from ASME B16.5-81 with permission.

Not to be used over 650°F.

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temperature ratings for which these standards are designed. A few of these characteristics from ANSI B16.5-1981 are given i[n Table 8.7.36.](#page-196-0)

Bolting material including nuts and washers are based on a high-grade product equal to that given in ASTM Standard Specifications for Alloy-Steel Bolting Material for High Temperature Service [\(Table 8.7.37\)](#page-198-0) and with physical and chemical requirements in accordance with the tables given under ANSI B16.5-1981. **Commercial steel bolts should not be used at steam pressures over 250** lb/in2 (1,724 kPa) and temperatures over 450°F (232°C). Nuts should be of carbon or alloy steel. Washers when used under nuts should be of forged or rolled carbon steel.

Bolting Drilling templates are in multiples of four, so that fittings may be made to face in any quarter. Bolt-holes straddle the centerlines. Bolt-holes are drilled $\frac{1}{8}$ in (0.32 cm) larger in diameter than the nominal size of bolt. Bolts or bolt studs threaded at both ends may be used and should be equipped with cold-punched or cold-pressed semifinished nuts of American National Standard rough dimensions, chamfered and trimmed.

All bolts and bolt studs having diameters 1 in and smaller, and the corresponding nuts are threaded with the American National Standard screw thread, coarse thread series, medium fit, class 3, while those bolts and bolt studs whose diameters are $1\frac{1}{8}$ in (2.86 cm) and larger have special threads of the American National form whose pitch is $\frac{1}{8}$ in (8) threads per inch). It is recommended that these special threads be allowed a pitch-diameter tolerance of -0.006 in and a lead tolerance of ± 0.002 in.

Bolt studs with a nut at each end are recommended for high-temperature service.

The allowable working fiber stress, considering internal allowable working pressure only, in bolting material for valve bonnet flanges, cleanout flanges, etc., is not to exceed 9,000 lb/in2 (62 MPa) assuming the pressure to act upon an area circumscribed by the periphery of the outside of the contact surface.

Metal Thickness Minimum metal thicknesses specified in the tables are based on an allowable fiber stress of 7,000 lb/in2 (48 MPa), using the modified Barlow formula of the ASME Boiler Construction Code for cylindrical sections and adding 50 percent to the thickness thus determined to compensate for the shape of the fittings. The minimum commercial casting thickness is considered to be 1⁄4 in; therefore, the standards do not show thicknesses less than this. The minimum thickness in these standards means the minimum thickness in any part of the finished casting.

The modified Barlow formula is as follows: For pipes having nominal diameters of $\frac{1}{4}$ to 5 in, $P + 125 = 2S(t - 0.065)/D$. For pipes of nominal diameters over 5 in, $P = 2S(t - 0.1)/D$, where *P* is the working pressure, lb/in2, *t* is the thickness of wall of pipe, in; *D* is the actual outside diameter of pipe, in; and *S* is 7,000 lb/in2 (48 MPa).

Ring Joints The dimensions used for ring and groove joint facings were developed by a committee of the API. The corresponding dimensions and ring numbers incorporated in the ANSI Standard are identical with those given in API Standard 5G. The dimension for the depth of groove is added to the basic flange thickness, which makes it necessary to include separate tables of dimensions for fittings having the ring joint facing.

Fitting Dimensions An inspection limit of $\pm \frac{1}{32}$ in is allowed on all center-to-contact surface dimensions for sizes up to and including 10 in, and \pm 1/16 in on sizes larger than NPS 10. An inspection limit of \pm 1/16 in is allowed on all contact-surface to contact-surface dimensions for sizes up to and including NPS 10, and $\pm \frac{1}{8}$ in, on sizes larger than NPS 10.

When elbows having longer radii than specified in the standards are required, the use of pipe bends is recommended.

Laterals The 45° laterals of the larger sizes may require additional reinforcement to compensate for the inherent weakness in this shape of casting.

Valve Dimensions Face-to-face and end-to-end dimensions of ferrous valves for the various pressures are in accordance with the requirements of ANSI B16.10-1973 for ferrous flanged valves.

Reducing Fittings Reducing fittings have the same center-to-flange edge dimensions as those of straight-size fittings of the largest opening.

Side-Outlet Fittings All side-outlet fittings have all openings on the intersecting centerlines.

Welding Neck Flanges The materials, facings, spot facings, etc., conform to the requirements given for other flanges, with the additional provision that the carbon content of the steel shall not exceed 0.35 percent.

Templates for drilling and center to contact-surface dimensions of the American Standard class 150 steel flanges and flanged fittings are the same as for the American Standard class 125 cast-iron flanged fitting standard.

Templates for drilling and center to contact-surface dimensions of the ANSI class 300 steel flanges and flanged fittings are the same as for the ANSI class 600 steel flanged fitting standard for sizes NPS $\frac{1}{2}$ to $1\frac{1}{2}$ [\(Table 8.7.38](#page-199-0)); and the same as for the ANSI class 250 cast-iron flanged fitting standard for sizes NPS 2 to NPS 24.

Flanged Pipe Joints

The usual form of pipe joint is that made up by bolting together flanges cast or forged integral with the pipe or fitting, threaded flanges, loose flanges on pipes with lapped ends, and flanges arranged for welding. These forms are illustrated i[n Tables 8.7.39](#page-200-0) and 8.7.40 and in [Fig. 8.7.9.](#page-202-0) The threaded joint is satisfactory for low and medium steam pressures. The lapped joint is permitted in the same sizes and service ratings as for joints with integral flanges. It is extensively used in high-class work. With the ring joint a higher pressure can be maintained with the same total bolt stress than is possible with the flat gasket type of joint. The welded joint eliminates possibility of leakage between flange and pipe. It is very successful in lines subject to high temperatures and pressures and heavy expansion strains. The welding-neck flange is available in the various pipe sizes. Specific requirements covering the application of all the types of joints in common use are outlined in the Code for Power Piping (ASME B31.1 and B31.3).

Facing of Flanges Various styles of finish are used on the faces of flanges, for the purpose of the retention of the gasket used to make a tight joint. Those in general use are as follows (see [Table 8.7.39\)](#page-200-0): plain straight face, plain face corrugated or scored, male and female, tongue and groove, and raised face.

The **plain straight face** has the entire face of the flange faced straight across and may be used with either a full face or ring gasket. The **plain face, serrated or V-grooved,** is a plain face upon which concentric grooves have been cut with either a round-nose or V-shaped tool. This finish is sometimes of advantage when the service demands an exceptionally thick, loosely woven fibrous or soft metallic gasket, because the roughening of the faces of the flanges tends to keep the gasket from blowing out. The **male-and-female** facing consists of a recess in one flange and a corresponding raised face or projection on the other mating flange extending from the inside of the pipe nearly to the inside of the bolt holes. In the **tongue-and-groove** facing, the tongue or raised face and the groove or recess are narrow rings located between the bolt holes and the port. The male-and-female and the tongue-and-groove facing have been extensively used, particularly on hydraulic lines. To a more limited extent they have been used also on high-pressure steam lines. Both these types, however, have in common several objectionable features from the standpoint of manufacture, erection, and maintenance. These objections are removed by the use of the **raised-face** facing, which consists of a high narrow raised ring on each of the mating flanges, whose inside diameters is the same as that of the pipe or port. It is particularly recommended for high-pressure steam and hydraulic lines. **Gaskets** used in this type of joint are either soft fibrous material or soft metal and extend from the inside of the pipe to the bolt holes. Only the small portion in contact with the narrow raised face is subjected to the compressive effect of the bolts.

The following advantages are claimed for the raised-face type of facing: all mating of flanges has been eliminated; any valve or fitting may be removed from the line without springing the line apart; the gasket is automatically centered by its outer edge coming in contact with the bolts; the outside edges of the flanges are far enough apart to make it possible to determine whether the joint has been properly made.

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Table 8.7.37 Mechanical Properties of Alloy Steel Bolting Material for High-Temperature Service

Austenitic steels

* For sizes 3⁄4 in. in diameter and smaller, a maximum hardness of 241 HB (100 HRB) is permitted.

† To meet the tensile requirements, the Brinell hardness shall be over 201 HB (94 HRB).
‡ Class 1 is solution treated. Class 1A is solution treated in the finished condition for corrosion resistance: heat treatment is crit and strain-hardened. Austenitic steels in the strain-hardened condition may not show uniform properties throughout the section particularly in sizes over 3/4 in (19.05 mm) in diameter.

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Table 8.7.38 Templates for Drilling, American National Standard Steel Pipe Flanges and Flanged Fittings (ANSI B16.5-1981) (All dimensions in inches)

8-200

Table 8.7.39 Facing Dimensions for the American Class 150, 300, 400, 600, 900, 1,500, and 2,500 Steel Flanges (ANSI B16.5-1981)

Small male-female Large tonque - aroove

* Included in the minimum flange thickness dimensions. A $\frac{1}{6}$ -in raised face is also permitted on the class 400, 600, 900, 1,500, and 2,500 flange standards, but it must be added to the minimum flange thicknesse. Reg A tolerance of $\frac{1}{64}$ in is allowed on the inside and outside diameters of all facings.

Gaskets for male-female and tongue-groove joints should cover the bottom of the recess with minimum clearance taking into account the tolerances stated above.

Unions may be classified as **screw** and **flange**. Typical designs are shown i[n Fig. 8.7.10,](#page-202-0) where at the top left is represented a female screw union of the gasket type, at the top right a female screw union having a brass to iron seat that is noncorrosive and a ground joint that eliminates the need for a gasket, and at the bottom a flange union of the gasket type. As in the case of other pipe fittings, unions and union fittings are available in the various pipe sizes and in materials and designs suitable for any service conditions. Very large flange unions can be made by bolting together two screwed companion flanges.

Threaded Fittings

Threaded fittings are made of cast iron, malleable iron, cast steel, forged steel, or brass. Plain standard fittings are generally used for lowpressure gas and water, as in house plumbing and railing work, while the beaded fitting is the standard steam, air, gas, or oil fitting. Screwed fittings are supplied with a large factor of safety. The questions of strength involve much more than the pressure from within the pipe which induces a comparatively low stress in the material. The greater strains come from expansion, contraction, weight of piping, settling, water hammer, etc. Dimensions of cast-iron and malleable-iron screwed fittings of the American National Standard are given in [Tables 8.7.41](#page-202-0) and 8.7.42.

 -0 roc

The dimensions of ferrous plugs, bushings, locknuts, and caps with pipe threads are covered by ANSI B16.14-1983. The dimensions of pipe plugs from this standard are given in [Table 8.7.43.](#page-203-0)

The normal **amount of thread engagement** necessary to make a tight

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Table 8.7.40 Dimensions of American National Standard Companion Flanges (ANSI B16.5-1981)*

| Threaded | apped |
|----------|-------|

* Other dimensions are given in [Tables](#page-199-0) [8.7.38](#page-199-0) and 8.7.39. Finished bore on lapped flange to be such as method of attachment of pipe requires.

FITTINGS FOR STEEL PIPE 8-203

Table 8.7.41 Dimensions of ANSI Class 150 Standard Malleable-Iron Threaded Fittings* (All dimensions in inches)

* The complete standard (ANSI B16.3-1977) covers also reducing couplings, elbows, tees, crosses, and service or street elbows and tees. SOURCE: ANSI B16.3-1977.

Fig. 8.7.9 Welded flange joints and ring joint. (*a*) Forged steel, screwed flange, back-welded and refaced; (*b*) forged steel, slip-on welding flange, welded front and back, refaced; (*c*) forged steel, welding neck flange, butt-welded to pipe; (*d*) lap-welding nipple, butt-welded to pipe; (*e*) ring joint.

Flange union

Fig. 8.7.10 Types of pipe unions.

joint for ANSI Standard pipe thread joints as recommended by Crane Co. is as follows:

8-204 PIPE, PIPE FITTINGS, AND VALVES

Table 8.7.42 Dimensions of Class 125 and Class 250 Standard Cast-Iron Threaded Fittings*

(All dimensions in inches)

* This applies to elbows and tees only.

The class 125 standard covers also reducing elbows and tees. The class 250 standard covers only the straight sizes. SOURCE: ANSI B16.4-1971.

Table 8.7.43 Dimensions of Class 125, 150, and 250 Pipe Plugs*

(All dimensions in inches)

* The material of (ANSI B16.14-1983) is to be cast iron, malleable iron, or steel, for use in connection with fittings covered by the American National Standard class 125 cast-iron threaded fittings (ANSI B16.4) and the American National Standard class 150
malleable-iron screwed fittings (ANSI B16.3).
†Hexagon sockets (sizes ¼ to 1 in) have dimensions to

SOURCE: ANSI B16.14-1983.

The Manufacturers' Standardization Society of Valve and Fitting Industry (MSS) has standardized malleable-iron and brass threaded fittings for several pressures.

Cast-bronze threaded fittings are made in both the class 125 and 250 standards. They are used for any water pipe where bad water makes steel pipe undesirable. Bronze fittings may be had in iron pipe sizes. Forged-steel threaded fittings are made for cold water or oil-working pressures up to 6,000 lb/in2 (41.4 MPa) hydrostatic. The ANSI has approved standard B16.26-1983 for cast copper alloy fittings for flared copper tubes for maximum cold-water service pressure of 175 lb/in2 (1,207 kPa).

Railing Fittings Fittings of special construction and of tighter weight than standard steam, gas, and water pipe fittings are widely used for hand railings around areaways, on stairs, for office enclosures with gates, and for permanent ladders. Railing fittings are made in various styles, generally globe-shaped in body, with ends reduced to take thread and recessed to cover all threads. They are furnished in malleable iron, black and galvanized, and in brass.

Special railing-fitting joints are available, such as the slip-andscrewed joint, where the post connection is screwed and the rim of the fitting is so made that the rail will slip into the fitting and allow for an angular variation of several degrees, being fastened by pins which are riveted over and filed smooth. The flush-joint stair-rail fitting is another special style of fitting which provides a hand rail with even surfaces at the joints.

Drainage fittings, as shown in the figures accompanying Table 8.7.44, have no pockets for the lodgment of solids, and the length of the thread chamber is such that when the pipe is threaded to the American National Standard dimensions, the end of the pipe will practically touch the shoulder when screwed in. They are especially adapted to plumbing work and vacuum-cleaning pipe installations. Dimensions in Table 8.7.44 conform to ANSI Standard B16.12-1983, Cast-Iron Threaded Drainage Fittings.

The development of standards for **cast-iron long-turn sprinkler fittings** was begun by the National Fire Protection Assoc. in 1914 with a study of the peculiar needs of fittings intended for fire-protection purposes. These fittings (screwed and flanged) are rated at 175 and 250 lb/in2 (1,207 and 1,724 kPa).

American National Standard Air Gaps and Backflow Preventers in Plumbing Systems, ANSI A40.4-1942 and A40.6-1943, was prepared to establish minimum requirements for plumbing, including water-supply distributing systems, drainage and venting systems, fixtures, apparatus, and devices, and the standardization of plumbing equipment in general.

Ammonia valves and fittings must provide a high margin of safety against accidents. Flanged valves and fittings have tongue-and-groove faces to assure tightness at the joints and against blowing out gaskets. Gaskets are compressed asbestos sheet. Threaded valves and fittings have long threads and are recessed so that the joints may be soldered. These valves and fittings are made of malleable iron, ductile iron, ferrosteel, or forged steel; depending on the size and style. Valves are all iron, with steel stems, and have special lead disk faces or steel disks. Copper or brass must not be used in their construction. Flanged valves are generally interchangeable with flanged fittings. All valves and fittings for ammonia are tested to 300 lb/in2 (2,069 kPa) air pressure under water. For dimensions of valves, fittings, and specialties for ammonia, refer to manufacturers' catalogs.

Soldered-Joint Fittings The American standard for these fittings

* Same as adopted for Class 125 Cast-iron Threaded Fittings, ANSI B16.4-1983.

† Three-way elbows have same dimensions as 90° long-radius elbows.

Double Y branches have the same dimensions as single Y branches.
Other fittings which are available are as follows: 5%, 11¼, and 60° elbows; basin tees and crosses; double 90° Y branches; double 90° long-turn Y branches; 4 traps; offsets, couplings, increasers, and reducing sizes.

SOURCE: ANSI B16.2-1983.

8-206 PIPE, PIPE FITTINGS, AND VALVES

Table 8.7.45 Soldered-Joint Fittings—Dimensions of Elbows, Tees, and Crosses (All dimensions in inches)

Wrought fittings as well as cast fittings, must be provided with a shoulder or stop at the bottom end of socket. * Dimensions for reducing elbows, reducing crosses, reducing tees, couplings, caps, bushings, adapters, and fittings with pipe thread on one end are also included in this standard.

† These dimensions may be used for wrought metal fittings as well as for cast brass fittings at manufacturer's option. ‡ This dimension is the same as the inside diameter class L tubing (ASTM B88-1983).

§ This dimension has the same thickness as class L tubing.

¶ These dimensions are minimum, but in every case the thickness of wrought fittings should be at least as heavy as the tubing with which it is to be used.

SOURCE: ANSI B16.18-1984.

(ANSI B16.18-1984) covers certain dimensions of soldered-joint wrought metal and cast brass fittings for copper water tubing including (1) detailed dimensions of the bore, (2) minimum specifications for materials, (3) minimum inside diameter of the fitting, (4) metal thickness for both wrought metal and cast brass fittings, and (5) general dimensions for cast brass fittings including center-to-shoulder dimensions for both straight and reducing cast fittings. Pressure and temperature ratings are also given. Sizes of the fittings are identified by the nominal tubing size as covered by the Specifications for Copper Water Tube (ASTM B88-1983). Dimensions of some of the fittings from this standard are given in Table 8.7.45.

Valves

The face-to-face dimensions of ferrous flanged and welding end valves are given in ANSI B16.10-1973. The types covered are:

Wedge-Gate Valves Cast iron, for 125-, 175-, and 250-lb/in2 (862, 1,207, and 1,724 kPa) steam service pressure and 800-lb/in2 (5,516 kPa) hydraulic pressure, and steel, for 150-, 300-, 400-, 600-, 900-, and 1,500-lb/in2 (1,034-, 2,068-, 2,758-, 4,137-, 6,206-, and 10,343-kPa) steam service pressures (see Fig. 8.7.11).

Double-Disk Gate Valves Cast iron, for 125- and 250-lb/in2 (862 and 1,724-kPa) steam service pressure and 800-lb/in2 (5,516-kPa) hydraulic pressure.

Globe and Angle Valves Cast iron, for 125- and 250-lb/in2 (862 and 1,724-kPa) steam service pressure, and steel, for 150-, 300-, 400-, 600-, 900-, 1,500-, and 2,500-lb/in2 (862-, 2,068-, 2,758-, 4,137-, 6,206-, 10,343-, and 17,238-kPa) steam service pressures (see Fig. 8.7.12).

Fig. 8.7.11 Wedge gate valves.

Fig. 8.7.12 Globe valve and angle valve.

Swing-Check Valves Cast iron, for 125- and 250-lb/in2 (862- and 1,724-kPa) steam service pressure and 800-lb/in2 (5,516-kPa) hydraulic pressure, and steel, for 150-, 300-, 400-, and 600-lb/in2 (1,034-, 2,068-, 2,758-, and 4,137-kPa) steam service pressures.

Except for ring-joint facings to the face-to-face dimension for flanged valves is the distance between the faces of the connecting end flanges upon which the gaskets are actually compressed, i.e., the ''contact surfaces.''

All flanges for class 125 cast-iron valves are plain-faced. The facings of the class 250 cast-iron, and the class 150 and 300 steel valves have a 1⁄16-in raised face which is included in the contact-surface to contactsurface dimensions. The contact-surface to contact-surface dimensions of steel valves for class 400 and higher pressures and for cast-iron valves for class 800 hydraulic pressure include a $\frac{1}{4}$ -in raised face.

The end-to-end dimensions for **welding-end** valves for sizes NPS 1 to 8 are the same as the contact-surface to contact-surface dimensions given in the tables for steel valves. For details of welding bevel see ANSI B16.10-1973 an[d Fig. 8.7.15.](#page-210-0)

A plus or minus **tolerance** of 1⁄16 in is allowed on all face-to-face dimensions of valves NPS 10 and smaller, and a tolerance of 1/8 on sizes NPS 12 and larger.

Cocks The ordinary plug cock operated by a handle or wrench is a form of valve in comparatively small sizes suitable for ordinary service only. The ASME Code for Pressure Piping requires that where cocks are used for high-temperature service they shall be so designed as to prevent galling, either by making the plugs of different material from the body of the cock or by treating the plugs to ensure different physical properties. By means of special design features that eliminate the tendency to leak and stick, the plug-cock type of valve has become available in large sizes and for severe service conditions. Sizes are listed as high as 30 in and are gear-operated in the larger sizes. For further details, refer to manufacturers' catalogs.

Expansion and Flexibility

Piping systems must be designed so that they (1) will not fail because of excessive stresses, (2) will not produce excessive thrusts or moments at connected equipment, or (3) will not leak at joints because of expansion of the pipe. Flexibility is provided by changes of direction in the piping through the use of bends or loops, or provision may be made to absorb thermal strains by use of expansion joints. All, or portions, of the pipe may be corrugated to improve flexibility; in many systems, however, sufficient change is provided by the geometry of the layout to make unnecessary the use of either expansion joints or corrugated sections of piping. Proper cold springing is beneficial in assisting the piping system to attain its most favorable condition. Because of plastic flow of the piping material, hot stresses tend to decrease with time while cold stresses tend to increase with time; their sum, called the stress range, remains substantially constant. For this reason no credit is warranted with regard to stresses; for calculation of forces and moments, the effect of cold spring is recognized by use of a cold-spring factor varying from 0 to 1 for cold spring varying from 0 to 100 percent.

The allowable stress range S_A is calculated by

$$
S_A = f(1.25S_c + 0.25S_h)
$$

where S_c and S_h are the *S* values for the minimum cold and maximum hot conditions, respectively, as given [in Table 8.7.1](#page-169-0)5. The stress-reduction factor f is a function of the number of hot-to-cold-to-hot (full) temperature cycles anticipated over the life of the plant, as follows:

The bending and torsional stresses calculated (see paragraph 119.6.4 of ANSI B31.1.0-1983) are used to determine the maximum computed expansion stress $S_E = \sqrt{S_b^2 + 4S_t^2}$, where S_b and S_t are bending and torsional stresses, respectively. S_E must not exceed the allowable stress range *SA*.

In recent years, many principal high-temperature steam lines have either been analyzed, tested in a model-testing machine, or both. No rigid rule is stipulated for the requirement of analysis or model test; however, the Code for Pressure Piping suggests that when the following criterion is not satisfied, need for an analysis is indicated: $DY/(L - U)^2 \leq 0.03$, where *D* is the nominal pipe size, in; *Y* is the resultant of movements to be absorbed by pipeline, in; *U* is the length of straight line joining the anchor points, ft; and *L* is the length of the developed line axis, ft.

Expansion Joints for Steam Pipelines In many instances it may be economical to care for thermal expansion by use of expansion joints. For low-pressure steam lines, the use of packed expansion joints may be feasible; experience has indicated that packed joints are difficult to maintain when used on high-pressure lines. Figure 8.7.13 shows a type of joint that has been successfully used for high-pressure, high-

Fig. 8.7.13 Expansion joint for steam line. *(Croll-Reynolds, Inc.)*

temperature service. The bellows is designed to take either axial, lateral, or combined axial and lateral deflections. The internal sleeve guides movement of the joint and also protects the flexible bellows from direct contact with the fluid being handled. Face-to-face dimensions, as well as permissible axial and lateral deflections, are indicated in [Table](#page-207-0) [8.7.46.](#page-207-0)

Where large lateral deflections are to be absorbed, two expansion joints separated by a length of pipe as shown in Fig. 8.7.14 may be used. With such an arrangement, the lateral deflection permissible with one joint only may be increased many times. Tie rods, as shown, should always be installed to protect the joint against overtravel and externally to guide movement of the joint.

Fig. 8.7.14 Arrangement of expansion joints for large lateral deflection. *(Croll-Reynolds, Inc.)*

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* Croll-Reynolds, Inc.
† For welding ends, add 4 in to face-to-face dimension shown.
‡ Consult manufacturer for permissible combined axial and lateral deflection.

Table 8.7.47 Thermal Expansion Data

 $A =$ mean coefficient of thermal expansion \times 10⁶, in/(in · °F) in going from 70°F (21°C) to indicated temperature.
 $B =$ linear thermal expansion, in/100 ft in going from 70°F (21°C) to indicated temperature.

Multip

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[Table 8.7.47](#page-207-0), extracted from the Code for Pressure Piping, lists thermal-expansion data for both ferrous and nonferrous piping. For expansion at temperatures intermediate between those shown, straight-line interpolation is permitted.

The **rubber expansion joint** has become an established part of pipeline equipment. Its special field of application is on low-pressure and vacuum lines in condenser applications, etc., and it is recommended for pressures up to 25 lb/in² (172 kPa) gage where the maximum temperature does not exceed 250°F. Standard joints for pressure installations are reinforced to withstand working pressures up to 125 lb/in2 (862 kPa) gage and temperatures up to 200°F. Joints are available in all standard pipe sizes.

Welding in Power-Plant Piping

(For dimensions of welding fittings see Tables 8.7.48 to 8.7.51; for welding techniques see also Sec. 13.3.)

The majority of main-cycle and service steel piping in modern steam power plants is of welded construction. Steel pipe of NPS 2 and smaller is generally socket-welded; larger-size piping is usually butt-welded. Frequently, depending on location and scheduling, piping larger than NPS 2 is prefabricated; smaller piping is shipped to the construction site in random lengths and is fabricated concurrently with installation. Small-sized chromium-molybdenum piping requiring bending is frequently also shop-fabricated so as to avoid high field preheat, welding, and stress-relieving costs. It is desirable to schedule shipment of

Table 8.7.48 Dimensions of Long-Radius 90° Butt-Welding Elbows (Standard weight—ANSI B16.9-1978, ASTM A234) (All dimensions in inches)

| Nominal pipe size | OD | ID | Wall thickness | Center to face | Pipe schedule numbers | Approx wt, lb |
|----------------------|-----------|--------|-------------------|-------------------|-----------------------------|------------------|
| $2\frac{1}{2}$ | 2.875 | 2.469 | 0.203 | $3^{3}/_{4}$ | 40 | 2.92 |
| 3 | 3.500 | 3.068 | 0.216 | $4\frac{1}{2}$ | 40 | 4.58 |
| $3\frac{1}{2}$ | 4.000 | 3.548 | 0.226 | $5\frac{1}{4}$ | 40 | 6.43 |
| 4 | 4.500 | 4.026 | 0.237 | 6 | 40 | 8.70 |
| 5 | 5.563 | 5.047 | 0.258 | $7\frac{1}{2}$ | 40 | 14.7 |
| 6 | 6.625 | 6.065 | 0.280 | 9 | 40 | 22.9 |
| 8 | 8.625 | 7.981 | 0.322 | 12 | 40 | 46.0 |
| 10 | 10.750 | 10.020 | 0.365 | 15 | 40 | 81.5 |
| 12 | 12.750 | 12.000 | 0.375 | 18 | $ST*$ | 119 |
| 14 | 14.000 | 13.250 | 0.375 | 21 | 30 | 154 |
| 16 | 16.000 | 15.250 | 0.375 | 24 | 30 | 201 |
| 18 | 18.000 | 17.250 | 0.375 | 27 | $ST*$ | 256 |
| 20 | 20.000 | 19.250 | 0.375 | 30 | 20 | 317 |
| 22 | 22.000 | 21.250 | 0.375 | 33 | $ST*$ | 385 |
| 24 | 24.000 | 23.250 | 0.375 | 36 | 20 | 458 |
| 26 | 26.000 | 25.250 | 0.375 | 39 | $ST*$ | 539 |
| 30 | 30.000 | 29.250 | 0.375 | 45 | $ST*$ | 720 |
| 34 | 34.000 | 33.250 | 0.375 | 51 | $ST*$ | 926 |
| 36 | 36.000 | 35.250 | 0.375 | 54 | $ST*$ | 1,040 |
| 42 | 42.000 | 41.250 | 0.375 | 63 | $ST*$ | 1,420 |

* Standard weight.

* Standard weight.

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Table 8.7.50 Dimensions of Long-Radius 45° Butt-Welding Elbows (Standard weight—ANSI B16.9-1978, ASTM A234)

|--|--|

I

* Standard weight.

hangers so that they will be available at the job site upon arrival of the prefabricated piping; this avoids the expense of providing, installing, and later removing temporary hangers and supports. Aside from the economy of welded construction, it is a virtual necessity in highpressure, high-temperature work because of danger of leakage if joints are flanged.

Shop welds are frequently made by automatic or semiautomatic submerged-arc or inert-gas shielded-arc processes; field welds are gener-

Table 8.7.51 Dimensions of Concentric and Eccentric Butt-Welding Reducers (Standard weight—ANSI B16.9-1978, ASTM A234) (Dimensions in inches)

| Nominal pipe size | Length | Approx wt, lb | Nominal pipe size | Length | Approx wt, lb | Nominal pipe size | Length | Approx wt, lb | |
|------------------------------------|----------------|------------------|----------------------|----------------|------------------|----------------------|--------|------------------|------|
| $2\frac{1}{2} \times 1$ | $3\frac{1}{2}$ | 1.30 | 8×6 | 6 | 13.4 | 22×20 | 20 | 157 | |
| $2\frac{1}{2} \times 1\frac{1}{4}$ | $3\frac{1}{2}$ | 1.47 | 8×6 | 6 | 13.9 | 24×16 | 20 | 160 | |
| $2\frac{1}{2} \times 1\frac{1}{2}$ | $3\frac{1}{2}$ | 1.51 | 10×4 | $\overline{7}$ | 21.1 | 24×18 | 20 | 163 | |
| $2\frac{1}{2} \times 2$ | $3\frac{1}{2}$ | 1.60 | 10×5 | $\overline{7}$ | 21.8 | 24×20 | 20 | 167 | |
| $3 \times 1\frac{1}{4}$ | $3\frac{1}{2}$ | 1.70 | 10×6 | $\overline{7}$ | 22.3 | 26×18 | 24 | 200 | |
| $3 \times 1\frac{1}{2}$ | $3\frac{1}{2}$ | 1.89 | 10×8 | $\overline{7}$ | 23.2 | 26×20 | 24 | 200 | |
| 3×2 | $3\frac{1}{2}$ | 2.00 | 12×5 | 8 | 30.5 | 26×22 | 24 | 200 | |
| $3 \times 2\frac{1}{2}$ | $3\frac{1}{2}$ | 2.16 | 12×6 | 8 | 31.1 | 26×24 | 24 | 200 | |
| $3\frac{1}{2} \times 1\frac{1}{4}$ | 4 | 2.35 | 12×8 | 8 | 32.1 | 30×20 | 24 | 220 | |
| $3\frac{1}{2} \times 1\frac{1}{2}$ | 4 | 2.52 | 12×10 | 8 | 33.4 | 30×24 | 24 | 220 | |
| $3\frac{1}{2} \times 2$ | 4 | 2.71 | 14×6 | 13 | 55.8 | 30×26 | 24 | 220 | |
| $3\frac{1}{2} \times 2\frac{1}{2}$ | 4 | 2.96 | 14×8 | 13 | 57.2 | 30×28 | 24 | 220 | |
| $3\frac{1}{2} \times 3$ | 4 | 3.05 | 14×10 | 13 | 60.4 | | | | |
| $4 \times 1\frac{1}{2}$ | 4 | 2.73 | 14×12 | 13 | 63.4 | | | Conc. | Ecc. |
| 4×2 | 4 | 3.17 | 16×8 | 14 | 70.2 | 34×24 | 24 | 270 | 229 |
| $4 \times 2\frac{1}{2}$ | 4 | 3.34 | 16×10 | 14 | 72.9 | 34×26 | 24 | 270 | 237 |
| 4×3 | 4 | 3.50 | 16×12 | 14 | 75.6 | 34×30 | 24 | 270 | 253 |
| $4 \times 3\frac{1}{2}$ | 4 | 3.61 | 16×14 | 14 | 77.5 | 34×32 | 24 | 270 | 261 |
| 5×2 | 5 | 5.05 | 18×10 | 15 | 86.9 | 36×24 | 24 | 340 | 237 |
| $5 \times 2\frac{1}{2}$ | 5 | 5.52 | 18×12 | 15 | 89.2 | 36×26 | 24 | 340 | 245 |
| 5×3 | 5 | 5.73 | 18×14 | 15 | 90.9 | 36×30 | 24 | 340 | 261 |
| $5 \times 3\frac{1}{2}$ | 5 | 5.86 | 18×16 | 15 | 94.0 | 36×32 | 24 | 340 | 269 |
| 5×4 | 5 | 5.99 | 20×12 | 20 | 134 | 36×34 | 24 | 340 | 277 |
| $6 \times 2\frac{1}{2}$ | $5\frac{1}{2}$ | 7.61 | 20×14 | 20 | 135 | 42×24 | 24 | 260 | |
| 6×3 | $5\frac{1}{2}$ | 8.00 | 20×16 | 20 | 138 | 42×26 | 24 | 270 | |
| $6 \times 3\frac{1}{2}$ | $5\frac{1}{2}$ | 8.14 | 20×18 | 20 | 142 | 42×30 | 24 | 285 | |
| 6×4 | $5\frac{1}{2}$ | 8.19 | 22×14 | 20 | 148 | 42×32 | 24 | 295 | |
| 6×5 | $5\frac{1}{2}$ | 8.65 | 22×16 | 20 | 151 | 42×34 | 24 | 300 | |
| $8 \times 3\frac{1}{2}$ | 6 | 12.8 | 22×18 | 20 | 154 | 42×36 | 24 | 310 | |
| 8×4 | 6 | 13.1 | | | | | | | |

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ally of the manual type and may be done by the shielded metal-arc and/or inert-gas metal-arc processes. Welding in power piping systems, whether in the shop or at the job site, must be done by welders who have qualified under provisions of the Code for Pressure Piping or the ASME Boiler and Pressure Vessel Code.

End Preparation for Butt Welds Figure 8.7.15 shows the end preparation recommended (not required) for piping whose wall thickness is 3⁄4 in or less, and Fig. 8.7.16 shows that required for piping with wall thickness above 3⁄4 in. During the welding process, to avoid entrance of welding material into the pipe, backing rings may be used as shown in Fig. 8.7.17*a, b,* and *c*.* Note that thick-walled pipes (over 3⁄4 in) are taper-bored on the inside in order that they may receive a tapered, machined backing ring.

Fig. 8.7.15 Recommended end preparation for pipe wall thickness of 3⁄4 in or less.

Fig. 8.7.16 Recommended end preparation for pipe wall thickness greater than 3⁄4 in.

Preheating Prior to start of welding, many materials require preheat to a specified temperature: preheat may be done by electrical-resistance or induction heating or by ring-type gas burners placed concentrically with the pipe. The preheat temperature is measured by indicating crayons or by thermocouple pyrometers and must be maintained during the welding operation. Table 1, Appendix D, of the Code for Pressure Piping lists materials used in piping systems and the appropriate temperatures for preheat. In general, the following is indicative of the intent only; for specific instances, the Code must be consulted.

Fig. 8.7.17 Recommended backing ring types. (*a*) Butt joint with split backing ring; (*b*) butt joint with bored pipe ends and solid machined or split backing ring; (*c*) butt joint with taper-bore ends and machined backing ring.

Carbon steel and **wrought iron** should be preheated to a ''hand-hot'' condition if the ambient temperature at time of field installation is 32°F $(0^{\circ}C)$ or less: carbon steels which have minimum tensile properties of 70,000 lb/in2 (483 MPa) or higher should be preheated to 250°F (121°C); under other conditions, preheat is not mandatory, but some purchasers insist that the contractor preheat heavy-walled piping such as boiler feed.

* Consumable inserts are also available. They are recommended for installation in piping systems which require a smooth, unobstructed interior surface.

Low-alloy steels with a chromium content not exceeding 3⁄4 percent and low-alloy steels with a total alloy content not exceeding 2 percent are required to be preheated to a minimum temperature of 300°F $(149^{\circ}C).$

Alloy steels with a chromium content between 3⁄4 and 2 percent and low-alloy steels with a total alloy content not exceeding 23⁄4 percent require preheating to 375°F (191°C) minimum. Those with a total alloy content greater than 23⁄4 percent but not exceeding 10 percent require preheating to a temperature of 450°F (232°C) minimum.

High-alloy steels containing the martensitic phase require preheating to 450°F (232°C) minimum; preheating is a matter of agreement between the purchaser and contractor in the case of welding high-alloy ferritic steels (ASTM A240 and A268). The possible advantages of preheat have not been established in the case of welding high-alloy austenitic steels, and for this reason the Code for Pressure Piping states that preheat is optional for these materials.

Welding procedure varies with material and welding process. In general, the pipe ends must be cleaned of oil or grease, and excessive amounts of scale or rust should be removed. The size and type of welding rod must be stated; the number of layers or passes is determined by the thickness of the pieces being joined. All slag or flux remaining on any bead of welding must be removed before laying down the next successive bead; any cracks or blowholes that appear on the surface of any bead must be chipped or ground away before the next bead of weld material is deposited. Throughout the welding process, it is essential that the minimum specified preheat temperature be maintained.

Stress Relieving Welded joints in all carbon-steel material whose thickness is 3⁄4 in (1.91 cm) or greater must be stress-relieved at a temperature of 1,100°F (593°C) or over for a period of time proportioned on the basis of at least 1 h/in of pipe-wall thickness (but in no case less than $\frac{1}{2}$ h) and then allowed to cool slowly (generally under a blanket) and uniformly. No stress relief is required for joints in carbon-steel piping whose wall thickness is less than $\frac{3}{4}$ in.

Welded joints in alloy steels with a wall thickness of $\frac{1}{2}$ in (1.27 cm) or greater, having a chromium content not exceeding 3⁄4 percent, and low-alloy steels with a total alloy content not exceeding 2 percent require stress-relieving at a temperature of 1,200°F (649°C) or over for a period of time proportioned on the basis of at least 1 h/in (0.4 h/cm) of wall thickness, but in no case less than 1⁄2 h.

Welded joints in alloy steels having a chromium content exceeding 3⁄4 percent, or a total alloy content exceeding 2 percent, except high-alloy ferritic (ASTM A240, A268) and austenitic steels, regardless of wall thickness, require stress relief at a temperature of 1,200°F or over for a period of time proportioned on the basis of at least 1 h/in of wall thickness, but in no case less than $\frac{1}{2}$ h. Stress relief of high-alloy ferritic steel (A240, A268) and austenitic steels is not required but may be performed as agreed upon by purchaser and contractor. In welds between austenitic and ferritic materials, stress relieving is optional and, if used, shall be a matter of agreement between the purchaser and contractor. Because of the difference between the coefficients of thermal expansion of the two dissimilar materials, careful consideration should be given to the selection of a heat treatment, if any, that will be beneficial to the welded joint.

Graphitization is precipitation of carbon at the grain boundaries in the heat-affected zone during the welding process. Such a phenomenon occurs when some metals operate at high temperatures for extended periods. It has been observed particularly in carbon-molybdenum steels that operate at 900°F (482°C) or higher.

Graphitization does not generally occur in carbon-molybdenum steels with over 1 percent molybdenum. It also has generally not occurred in the chromium-molybdenum low-alloy steels operated at temperatures between 900°F (482°C) and 1,050°F (566°C). Where graphitization has occurred, the two most commonly used methods for rehabilitation of the pipe are (1) gouging out the heat-affected zone of the weld deposit and rewelding the area with electrodes depositing carbon-molybdenum weld metal, followed by a stabilization heat treatment at 1,300 \degree F (704 \degree C) for 4 h, or (2) solution annealing the weld joints at 1,800°F (982°C), followed by a stabilization heat treatment.

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Fig. 8.7.18 Methods of supporting pipes.

Pipe Supports

The Code for Pressure Piping includes many types of supports and gives directions for their application. A proper pipe support must have a strong rigid base properly supported, and an adjustable roll construction which will maintain the alignment in any direction. It is important to avoid friction caused by the movement of the pipe in the support and to have all parts of sufficient strength to maintain alignment at all times. Wire hangers, band iron hangers, wooden hangers, hangers made from small pipe, and hangers having one vertical pipe support do not maintain alignment.

The direction of expansion in a pipe run can be predetermined by anchoring one end, both ends, or the middle. **Anchors** must be firmly fastened to a rigid and heavy part of the power-plant structure, and must also be securely fastened to the pipe; otherwise the equipment for absorbing expansion is useless, and severe stresses may be thrown on parts of the piping system. Some methods of support are shown in Figs. 8.7.18 and 8.7.19. Welded steel brackets (Fig. 8.7.18*a*) are available in light, medium, and heavy weights. Many types of supports can be mounted on these brackets, such as the anchor chair shown on the bracket at (*a*), pipe roller supports of the type at (*c*), pipe roll stands of various types such as shown in Fig. 8.7.19, pipe seats, etc. Figure 8.7.18*b* illustrates one of the many types of adjustable ring hangers in use. The split ring hanger can be applied after the pipeline is in place. At (*c*) in Fig. 8.7.18 is shown a spring cushion pipe roll hanger recommended for service where constant support* is required and compensation must be made for movement of the piping. The springs provide an efficient means of absorbing the vibration. Figure 8.7.18*d* shows one of the many types of pipe saddle supports available. Figure 8.7.19 shows a cast-iron pipe roll stand designed for cases where vertical adjustment is not necessary but where provision must be made for expansion and contraction of the pipeline. Several designs of such stands with provision for vertical adjustment and of the same general dimensions are also available. One type of cast-iron roll and plate, illustrated in Fig. 8.7.19, provides for expansion and contraction where vertical adjustment is not

* The support afforded by the hanger of Fig. 8.7.18*c* is constant only in the sense that some degree of support is always present. It might be more appropriately termed a variable-support device.

necessary. If necessary, the baseplate can be raised or lowered by use of shims. Detailed information and dimensions of a great variety of pipe supports can be found in manufacturers' catalogs.

In supporting a high-temperature piping system, it is necessary to provide for expansion and contraction due to cyclic changes. It is often possible to find a point of zero movement along the run of a long line and to support a considerable portion of the total load by a rigid hanger or support of the type shown in Figs. 8.7.18 and 8.7.19. However, for other portions of the run, some form of spring support is often indicated. For relatively light lines, which are not subjected to excessive movements from hot to cold positions, a variable spring hanger will frequently suffice; for heavy lines, or those in which expansion movements are great, it is advisable to use constant support of counterweighted hangers so that transfer of weight to other hangers or equipment connections is prevented. Parts (*a*) and (*b*) of Fig. 8.7.20 indicate, respectively, a horizontal and vertical run of piping supported by a **constant-support hanger**. Figure 8.7.20*c* and 8.7.21*a* indicate horizontal runs supported by **variable-spring hangers**[. Figure 8.7.21](#page-212-0)*b* shows a riser supported by a variable spring beneath a base elbow[. Figure 8.7.21](#page-212-0)*c* indicates a **sway brace** that is used to control vibration and undesirable movement in a piping system.

The principal supports utilized for the support of critical piping in-

Fig. 8.7.20 Constant support and variable-spring hangers.

Fig. 8.7.19 Pipe supports on cast-iron rolls.

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Fig. 8.7.21 Spring hangers and sway brace.

volve constant-support hangers, variable-spring hangers, rigid hangers, and restraints.

Constant-Support Hangers This type of hanger provides a constant supporting force for the piping system throughout its full range of vertical pipe movement. This is accomplished through use of a spring coil working in conjunction with a lever in such a way that the spring force times its distance to the lever pivot is always equal to the pipe load times its distance to the lever pivot. This type of support is ''thermally invisible,'' as the supporting force equals the pipe weight throughout its entire expansion or contraction cycles.

These hangers are used on systems or at locations where stresses are considered critical. Pipe weight reactions or transfer of loads are not imposed in the system or connections with this type of device.

As the load is considered constant with the unit in travel, readings from inspections are based on travel. The readings are taken from the position of an indicator and its relation to the numbers on the travel scale. The scale is divided into 10 divisions. H or high on the scale is equal to (0.0), M or midway on the scale is equal to (5.0), and L or low on the scale is equal to 10.

The design settings were obtained from the position of the factoryinstalled buttons that are placed adjacent to the travel scale.

''Perfect'' readings would be if the indicator were to line up with the white button (cold) and the red (hot); however, this is rarely the case. Generally, readings are considered acceptable and not noteworthy as long as they reflect movement consistent with design in both direction and length. A general rule is that when the hot setting is higher than the cold setting, then movement is down from cold to hot. If the cold setting is higher, movement is up.

The following terms are normally applied to these devices:

Actual travel: Anticipated movement of the pipe from design. The hot and cold position stickers are a function of this movement.

Total travel: The maximum movement a support can accept without danger of topping or bottoming out. The scale from $H(0.0)$ to $L(10.0)$ is a function of this.

Topped out: The indicator is above the high point and in contact with the end of the slot. This condition means the support is unloaded or is in the process of unloading.

Bottomed out: The indicator is below the (10.0) point and in contact with the end of the travel slot; the support is overloaded.

Variable-Spring Hangers These devices are installed at locations where stresses are not considered to be critical or where movement and economics permit their use.

The inherent characteristics of a variable are such that the supporting force varies with the spring's deflection. Movement of the pipe causes

In addition, as it is desirable to support the actual weight of the pipe when the system is hot, when the stresses tend to become most critical, the hot load is the dead weight of the pipe. The cold load is actually under- or oversupporting the pipe, depending on the movement from cold to hot.

The general rule for determining movement is similar to that of constant supports. If the hot load is higher than the cold, then pipe movement is down from cold to hot. If the cold load is higher, then movement is up.

Unlike constant supports, the readings from variables are measured in pounds. The readings are taken by noting the position of the indicator relative to a load scale that is adjacent to the travel slot.

The **distance between supports** will vary with the kind of piping and the number of valves and fittings. Supports should be provided near changes in direction, branch lines, and particularly near valves. The weight of piping must not be carried through valve bodies. In establishing the location of pipe supports, the designer should be guided by two requirements: (1) the horizontal span must not be so long that sag in the pipe will impose an excessive stress in the pipe wall and (2) the pipeline must be pitched downward so that the outlet of each span is lower than maximum sag in the span. Otherwise entrapped water can result in severe water hammer and pipe swings, particularly during plant start-up of steam piping.

Fabrication and installation practices are provided in MSS Standard Practice SP-89. Table 8.7.52 lists spacing for standard-weight pipe supports.

Pipe Insulation

(see Secs. 4 and 6 for heat-transmission data.)

The value of a steam-pipe covering is measured by its ability to reduce heat losses. This might range from 50 percent for small, low-temperature lines to 90 percent for large, high-temperature lines. Many **pipeinsulating materials** are available: 85 percent magnesia, foam glass, calcium silicate, and various forms of diatomaceous earths. Some of these materials are suited for relatively low temperatures only, others are best suited for high temperatures, and still others are suitable over a considerable temperature range.

Pipe insulation is applied in molded sections 3 ft long. For high-temperature work, the insulation is applied in at least two layers with the

Table 8.7.52 Maximum Spacing of Pipe Supports at 750°F (399°C)*

* This tabulation assumes that concentrated loads, such as valves and flanges, are separately supported. Spacing is based on a combined bending and shear stress of 1,500 lb/in2 when pipe is filled with water; under this condition, sag in pipeline between supports will be approximately 0.1 in.

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joints staggered so as to prevent a direct channel for heat loss. Because of its maximum-temperature limitation of about 600°F (316°C), 85 percent magnesia is used as the second layer with a high-temperature-resistant material placed in direct contact with the pipe. The molded insulation is fastened securely in place with copper or galvanized wire and is then given a surface finish; indoor pipes are first sheathed with resin paper and covered with canvas, either pasted or sewed; outdoor pipes may be weather-protected by a coating of asphaltic-type waterproofing compound, they may be sheathed and canvased and then given a weatherproof surface, so they may be encased in metallic (steel or aluminum) jackets.

The heat loss from an insulated pipe appears in three phases: heat passes by *conduction* through the metallic pipe walls and through the insulating material; it then is dissipated from the outdoor surface of the insulation by *convection* and by *radiation.* Extremely accurate calculations must also take into account the temperature drop by convection through the film on the inside surface of the pipe. The task of accurately calculating heat losses is somewhat tedious, since the convection and radiation losses are related to the surface temperature (outside of insulation), which is unknown until conduction losses are balanced against surface losses.

For combined convection and radiation coefficients for bare pipes, and all necessary formulas to permit trial-and-error calculations, see Sec. 4. Insulation manufacturers publish data which give heat losses for wide ranges of pipe size and temperature.

Identification of Piping

The American National Standards Institute has approved a **Scheme for the Identification of Piping Systems** (ANSI A13.1-1981). This scheme is limited to the identification of piping systems in industrial plants, not including pipes buried in the ground, and electric conduits. Fittings, valves, and pipe coverings are included, but not supports, brackets, or other accessories.

Classification by Color All piping systems are classified by the nature of the material carried. Each piping system is placed, by the nature of its contents, in the following classifications:

Method of Identification At conspicuous places throughout a piping system, color bands should be painted on the pipes to designate to which one of the five main classes it belongs. If desired, the entire length of the piping system may be painted the main classification color. Further, the actual contents of a piping system may be indicated by,

preferably, a stenciled legend of standard size giving the name of the contents in full or abbreviated form. These legends should be placed on the color bands. The identification scheme may be extended by the use of colored stripes placed at the edges of the colored bands.

The bands, legends, and stripes should be placed at intervals throughout the piping system, preferably adjacent to valves and fittings to ensure ready recognition during operation, repairs, and at times of emergency.

A recommended classification, under this color scheme of materials carried in pipes, includes, as dangerous, combustible gases and oils, hot water and steam above atmospheric pressure; as safe, compressed air, cold water, and steam under vacuum.

Pressure Hose

Hose with durable rubber lining may be obtained to withstand any needed pressure. If the rubber compound is properly made, the life of a hose will be 7 to 10 years, while a cheaper hose, lined with inferior material, will probably not last more than 3 or 4 years. See also Secs. 3 and 12.

American National Fire-Hose Coupling Screw Thread (ANSI B1.20-7-1966) This standard is intended to cover the threaded part of fire-hose couplings, hydrant outlets, standpipe connections, and at other special fittings on fire lines, where fittings of the nominal diameters given in Table 8.7.53 are used. It also includes the limiting dimensions of the field inspection gages. The American National Standard form of thread must be used.

SOURCE: ANSI B1.20.7-1966.

American National Standard Hose-Coupling Screw Threads (ANSI B1.20.7-1966) These standards apply to the threaded parts of hose couplings, valves, nozzles, and all other fittings used in direct connection with hose intended for fire protection or for domestic, industrial, or general service in nominal sizes given in Table 8.7.54. The American

Table 8.7.54 Dimensions of Standard Hose Couplings (A) l dimensions in inches. Letters refer t[o Fig. 8.7.22\)](#page-214-0)

| Service and nominal size | Inside diam, C | Diam of thread, D | No. of threads per inch | L | I | H | T |
|--|---------------------|------------------------|-------------------------------|----------------|----------------|-------|----------------|
| Garden: $\frac{1}{2}$, $\frac{5}{8}$, $\frac{3}{4}$ | 25/32 | $1\frac{1}{16}$ | $11\frac{1}{2}$ | $\frac{9}{16}$ | $\frac{1}{8}$ | 17/32 | $\frac{3}{8}$ |
| Chemical: $\frac{3}{4}$, 1 | $1\frac{1}{32}$ | $1\frac{3}{8}$ | 8 | $\frac{5}{8}$ | $\frac{5}{32}$ | 19/32 | 15/32 |
| Fire: $1\frac{1}{2}$ | $1^{17}/_{32}$ | \overline{c} | 9 | $\frac{5}{8}$ | $\frac{5}{32}$ | 19/32 | 15/32 |
| Other connections: | | | | | | | |
| $\frac{1}{2}$ | 17/32 | 13/16 | 14 | $\frac{1}{2}$ | $\frac{1}{8}$ | 15/32 | $\frac{5}{32}$ |
| $^{3/4}$ | 25/32 | $1\frac{1}{32}$ | 14 | $\frac{9}{16}$ | $\frac{1}{8}$ | 17/32 | $\frac{3}{8}$ |
| 1 | $1\frac{1}{32}$ | $1\frac{9}{32}$ | $11\frac{1}{2}$ | $\frac{9}{16}$ | $\frac{5}{32}$ | 17/32 | $\frac{3}{8}$ |
| $1\frac{1}{4}$ | $1\frac{9}{32}$ | $1\frac{5}{8}$ | $11\frac{1}{2}$ | $\frac{5}{8}$ | $\frac{5}{32}$ | 19/32 | 15/32 |
| $1\frac{1}{2}$ | $1^{17}/_{32}$ | $1\frac{7}{8}$ | $11\frac{1}{2}$ | $\frac{5}{8}$ | $\frac{5}{32}$ | 19/32 | 15/32 |
| \overline{c} | $2\frac{1}{32}$ | $2^{11}/_{32}$ | $11\frac{1}{2}$ | $\frac{3}{4}$ | $\frac{3}{16}$ | 23/32 | 19/32 |

SOURCE: ANSI B1.20.7-1966.

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National Standard thread form is used. This coupling is similar in design to the fire-hose couplings illustrated in Fig. 8.7.22. **Flexible metal hose and tubing** are avail-

in either bronze or steel.

able for a wide range of conditions of temperature, pressure, vibration, and corrosion, and are made in two basic constructions, corrugated or interlocked, and

The corrugated type (Fig. 8.7.23) may have either annular or helical corrugated formations, usually covered with metal braid, and is adapted to high-pressure high-temperature leak-proof service. Some typical applications include dieselengine exhaust hose, reciprocating flexi-

Fig. 8.7.22 Typical form of standard coupling.

ble connections, loading and unloading hose, saturated and superheated steam lines, lubricating lines, gas and oil lines, vibration connections, etc.

The interlocked type is made in several ways; the fully interlocked type is illustrated in Fig. 8.7.24. Typical applications include wiring conduit, cable armor, decorative wiring covering, dust-collective tubing, grease and oil connections, flexible spouts, and moderate-pressure oil lines.

Standard couplings and fittings can be attached to flexible metal hose or tubing by various methods such as brazing or welding. Each type of

Fig. 8.7.23 Flexible metal hose.

Fig. 8.7.24 Interlocked flexible metal hose.

hose construction has limits of service use and proved application usages. Information and recommendations as to the type and size to use under any given conditions should be obtained from the manufacturers.

8.8 PREFERRED NUMBERS

by C. H. Berry

REFERENCES: Hirshfeld and Berry, Size Standardization by Preferred Numbers, *Mech. Eng.,* Dec. 1922. Schlink, A New Tool for Standardizers, *Am. Mach.,* July 12, 1923. ANSI Standard Z17.1.

Many manufactured articles are made in several sizes which may be designated by some dimension, speed, capacity, or other feature. Each such series of products may be paralleled by a series of numbers.

It is generally agreed that such number series should be **geometric progressions;** i.e., each term should be a fixed percentage larger than the preceding. A geometric series provides small steps for small numbers, large steps for large numbers, and this best meets most requirements. The small steps in the diameter of the numbered twist drills would be absurd in drills of 1 in diameter and larger.

In the case of sized objects that are used principally as raw material, e.g., steel rod, an arithmetic progression may be preferable because it tends to reduce the cost of machining. It is desirable to be able to buy raw material a fixed amount (rather than a fixed percentage) larger than the finished article.

Preferred numbers is the name given to various series proposed for general use. These are either geometric progressions or approximations thereto. A geometric series is defined by one term and the ratio of each term to the preceding one. On the choice of these elements for a preferred number series, there is as yet no general agreement. The same value would hardly be satisfactory for all cases. The idea of preferred numbers is to provide a master series from which terms can be chosen to suit any needs. This would ultimately lead to a comprehensive plan in all fields of manufacture, so that, for example, the sizes of shafting would be in accord with the sizes of bearings, and indeed with all manner of cylindrical machine elements.

An advantage of a geometric series is that if linear dimensions are chosen in the series, areas, volumes, and other functions of powers of dimensions are also members of the same series.

In one of the most carefully considered systems of preferred numbers the base term is 1, and the ratio is $\sqrt[80]{10}$. In this series, the 81st term is 10, and accordingly the series from 10 to 100 or from 0.01 to 0.1, or, in general, from 10^n to 10^{n+1} is identical with the series from 1 to 10 with the decimal point shifted. This series will rarely be used in full; some will choose alternate terms, some every fourth, fifth, tenth, or twentieth

SOURCE: American National Standard Preferred Numbers Z17.1, reproduced with permission of ANSI.

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term. The index of the root, 80, has as factors, 24 and 5, so that the series readily yields subseries having as ratios the roots of 10 with indices 2, 4, 8, 16, 5, 10, 20, 40, thus giving a wide range of choice. See [Table](#page-214-0) [8.8.1.](#page-214-0)

The strict logic of this series has been somewhat impaired by the adoption of rounded values that are slightly different in the 1-to-10 and 10-to-100 intervals. For the United States, ANSI has adopted a Table of Preferred Numbers (ANSI Z17.1) which differs slightly from the system described in the preceding paragraph.

Another type of series is the **semigeometric series** consisting of a basic geometric series with 1 as the base term and a ratio of 2, giving a series \ldots 1/8, 1/4, 1/2, 1, 2, 4, \ldots . Between consecutive terms are inserted arithmetic series of 2, 4, 8, or 16 terms, in general using different numbers of terms in different intervals.

A similar procedure is used to establish the numbers of teeth in a prescribed number of gears that are intended for use in a gear train to provide a stepped gradation of rotational speeds within an upper and lower bound.